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A Study of Extensive Air Showers

at Sea Level

bу

S.J.Fatemi, B.Sc.

A thesis submitted to the University of Durham for the Degree of Doctor of Philosophy

APRIL 1981

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CONTENTS

			Page
ALSTRAC	Т		i
PREFACE			ii
ACKNÓWLI	EDGEMEN	TS	iii
CHAPTER	1	INTRODUCTION	ן.
	1.1	HISTORICAL REVIEW	1
	1.2	THE NATURE AND ENERGY SPECTRUM OF THE PRIMARY COSMIC RAYS	2
	1.3	OKIGIN OF COSMIC RAYS	4
	1.4	SECONDARY PARTICLES IN THE ATMOSPHERE	5
	1.5	THE QUARK SEARCH	6
	1.6	THE SIGNIFICANCE OF COSMIC RAY STUDIES	7
CHAP TE R	2	THE DURHAM E.A.S.ARRAY AND THE FLASH TUBE CHAMBER	9
	2.1	INTRODUCTION	9
	2.2	THE FLASH TUBE CHAMBER	9
	2.2.1	Construction of the Chamber	9
	2.2.2	The High Voltage Pulsing System	10
	2.2.3	Properties of Flash Tubes	11
	2.3	THE E.A.S. ARRAY EXPERIMENT	12
	2.3.1	Introduction	12
	2.3.2	The Detecting Elements and Fast Timing Techniques of the Array	13
	2.3.3	The E.H.T. Distribution units and the Head Amplifiers	14
	2.3.4	The Linearity of Response of Photo- multiplier Tubes	15
	2.3.5	Calibration of the Detectors	16
	2.3.6	The Data Handling Electronics	16

CHAPTER	3	THE ELECTHON COMPONENT OF E.A.S.	18
	3.1	INTRODUCTION	18
	3.2	THE ELECTRON LATERAL STRUCTURE Function	18
	3.3	METHODS OF CORE LOCATION	21
	3.3.1	Loci Curve Method	21
	3.3.2	Computer Method of Core Location	23
	3.4	CUNCLUSION	24
	3.5	ELECTRON DENSITY FLUCTUATIONS	25
СНАРТЕК	4	THE AGE PARAMETER OF E.A.S. AND ITS DEPENDENCE ON SHOWER SIZE AND ZENITH ANGLE	27
	4.1	1NTRODUCTION	27
	4.1.1 4.1.2 4.1.3	The Electromagnetic Cascade Shower The Age Parameter of E.A.S. Central Density	27 28 30
	4.2	EXPERIMENTAL ARRANGEMENT AND ANALYSIS	30
	4.3	THE RESULTS AND PREVIOUS MEASUREMENTS	33
	4.3.1 4.3.2	The Shower Size and Zenith Angle Dependence The ^A c/N Measurements Dependence	33 35
	4.4	CONCLUSION	37
CHAPTER	5	SIZE SPECTRUM OF E.A.S. AT SEA LEVEL TAKING INTO ACCOUNT THE AGE PARAMETER OF THE SHOWER	39
	5.1	INTRODUCTION	39
	5.2	PREVIOUS MEASUREMENTS OF THE NUMBER SPECTRUM	40
	5.3	PRESENT EXPERIMENT	42
	5.3.1	The Trigger Modes of the E.A.S. Array	42

	5.3.2	The Collecting Area of E.A.S. and the Shower Age	43
	5.3.3	Effect of Zenith Angle on Collecting Area	44
	5.3.4	Analysis of the Data	46
	5.3.5	The Result and Conclusion	49
СНАРТЕК	6	LATERAL DISTRIBUTION OF MUONS IN E.A.S. AT SEA LEVEL	51
	6.1	THE MUON COMPONENT	51
	6.2	THE MUON LATERAL DISTRIBUTION	52
	6.3	PREVIOUS MEASUREMENTS	54
	6.3.1	Allan et al (1968)	54
	6.3.2	Khristiansen et al (1975)	56
	6.3.3	Wdowczyk et al (1973)	57
	6.3.4	Rozhdestvensky et al (1975)	58
	6.3.5	Discussion of Previous Work	59
	6.4	PRESENT WORK	60
	6.4.1	The Muon Detector	60
	б.4.2	Data analysis	62
	6.4.3	The Result of the Present Experiment	63
	6.5	CUNCLUSION	65
CHAPTER	7	SEARCH FOR QUARKS CLOSE TO THE CORE OF E. A .S.	67
	7.1	THE CONCEPT OF QUARKS	67
	7.2	QUARK SEARCH METHODS	71
	7.2.1	Searches at Accelerators	71
	7.2.2	Searches in Stable Matter	72
	7.3	COSMIC RAY SEARCHES	74
	7.3.1	Single Particle Searches	74
	7.3.2	Search in E.A.S.	75

	7.4	PRESENT EXPERIMENT	7 6
	7.4.1	Introduction	7 6
	7.4.2	The basic bata and Analysis	7 8
	7.4.3	lhe Juark Candidates	79
	7.4.4	Conclusion	80
CHAPTER	8	THE ARRIVAL DIRECTIONS OF E.A.S. IN GALACTIC COURDINATES	81
	8.1	INTRODUCTION	81
	8.2	PREVIOUS ANISOTROPY MEASUREMENTS IN THE E.A.S. ENERGY RANGE	81
	8.3	PRESENT WORK	82
	8.3.1	Experimental Arrangement	82
	8.3.2	Conversion of Local Solar Time to Local Sidereal Time	84
	8.3.3	The Sin-Ambiguity	86
	8.3.4	Method of Calculating the Expected Number of Showers in Galactic Co- ordinates Assuming they are Iso- tropically Distributed in Space	89
	8.4	ANALYSIS OF THE DATA AND RESULTS	92
	8.5	CONCLUSION	94
CHAPTER	9	CONCLUSION	95
APPENDI:	Х А	Evaluation of the Fraction of Particles Which Fall Beyond a Distance r From the Shower Axis Direction in Pure Electron Photon Cascades	97
APPENDIX	ХB	A Copy of the Cern MINUIT Program Used to Minimise the N.K.G Function for the Age Parameter and Shower Size	98
APPENDI)	ΧC	The Effect of Sampling Density Fluctua- tions on the Collecting Area for Showers of a Given Size for a Given E.A.S Selection Trigger	100
APPENDI:	X D	The Efficiency of Detecting Single Penetrating Charged Particles Traversing a Shielded Flash Tube Chamber as a Function of Core Distance in Extensive Air Showers	103

APPENDIX E Consistency of the Prescott (1977) 105 and the Clark et al (1958) formulae for determining the right ascension and declination from the measured arrival direction of an E.A.S.

REFERENCES

ABSTRACT

The lateral distribution of muons of energy $E_{\mu} > 500$ MeV in E.A.S. of median size $3 \cdot 10^5$ particles at sea level and their correlation to the electron structure function (shower age parameter) has been investigated using a large flash tube chamber operated in conjunction with the Durham E.A.S. array. The lateral distribution seems to be not dependent on shower size, but for the more inclined and older showers it tends to be flatter. Old showers of a given size are found to contain a greater total number of muons than young showers of the same size.

A measurement of the size spectrum has been performed in which the size and collecting area take into account the age parameter of a single shower. Except at very small and large shower sizes, the spectrum shows a close agreement with the spectrum obtained assuming all showers obey the Greisen average lateral structure function.

A search for charged e/3 particles (quarks) close to the core of E.A.S. has been carried out using the flash tube chamber. In 511.2 hours running time, 2 low efficiency tracks have been observed but none fulfil all the criteria as a genuine quark candidate. A search for any preferred arrival direction of showers in galactic coordinates has been carried out. The results show an overall isotropic primary flux but in the galactic chart two anomalous regions (regions with an excess of events) are observed. Correlation of the regions with the known cosmic ray sources (supernova remnants, pulsars, quasars, X and γ -ray sources) have been studied.

PREFACE

This thesis describes the work performed by the author in the Physics Department of the University of Durham while he was a research student under the supervision of Dr. F. Ashton.

The Durham E.A.S. array, in conjunction with a large flash tube chamber, has been used to study the different components of E.A.S.

The author has shared with his colleagues the collection of the data obtained by the flash tube chamber and has been responsible for the calculations and data interpretation described in the thesis. Air shower information was supplied by Dr. M. G. Thompson, Mr. A.C. Smith, Mr. T. R. Stewart and Mr. M. Treasure.

Some preliminary results, described in this thesis, on electron density fluctuation, muons and the size spectrum, have been reported by Ashton et al (1977).

ii

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Many members of the Cosmic Ray Research group are thanked for helpful discussions and friendly assistance, in particular Dr.H.Nejabat and Dr.I.A.ward, and in the later stages of the work, Mr.M.Abdullah.

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iii

CHAPTER 1

INTRODUCTION

1.1 HISTURICAL REVIEW

In the year 1900, when Elster and Geitel used electroscope techniques to study the electrical conductivity of air, they noticed the existence of a radiation which continuously ionized the air in the electroscope. In the same year. independently, Wilson studied this ionizing radiation using an ionization chamber, where he noticed the penetrability of this radiation, which could pass through a thick layer of earth. Although they did not think it was due to X-rays or radioactive radiation against which the devices were shielded, it was thought that it could be due to some radioactive substances still unknown in the earth's crust. If this was the case as we go high in the altitude, there should be less ionization According to this expectation, Gockel in the apparatus. (1910,1911) performed a balloon experiment at various heights above sea level and their experiment showed the expected effect weakly in their limited range of height of observation.

The continuation of this work was by Hess (1912) who extended the height of observation. He first observed a slight decrease and later a rapid increase up to an altitude of 5 km. The result made it evident that the unknown radiation came from high altitudes. Kolhorstr (1914) performed a balloon experiment and confirmed the Hess result when ionization increased up to an altitude of 9 km. It was argued that it could be due to radioactive gases high in the atmosphere or might be due to thunderstorms. The radiation discovered by



Hess was later investigated in more detail in a series of experiments by Millikan (1923-1926). As an example, he performed the experiments some metres under the surface of two lakes which were thought to be free from radioactive contamination. The result showed in both places a decrease with depth indicating a radiation travelling downwards in the air. He also performed experiments at much higher altitudes, up to 15 km, and his overall result showed that the discovered radiation came from above the atmospheric surface of the earth and was given the name 'cosmic rays'. Since then, they have been the subject of intensive study. At the time, γ radiation was the only known penetrating radiation, so the cosmic rays were assumed to be photons. The next investigations used detectors like the cloud chamber and Geiger-Muller counter to identify and study the charged particles. A great number of different particles were found to be involved in cosmic rays. Positrons were discovered in electron-photon cascades by Blacket and Occhialini in 1932. Muons were discovered by Anderson and Neddermeyer in 1937, and the mass of the muon was found to be about 200 electron masses, it being unstable and decaying into an electron and two neutrinos with a decay constant of 2 µs. Muons are secondary particles produced by $\pi-\mu$ decay, the pions being produced when primary cosmic rays (which are mainly protons) interact in the atmosphere. At sea level there is a considerable flux of muons and they form the major component of radiation able to penetrate 10cm of lead.

1.2 THE NATURE AND ENERGY SPECTRUM OF THE PRIMARY COSMIC RAYS

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The problem in investigating the nature of primary

cosmic ray particles are their low intensity at high energies ($\ge 10^{14}$ eV), and especially their decreasing intensity as the primary energy increases. Primary particles with energy up to 10^{20} eV have been detected and so far no cut-off has been observed.

At low energies (\leq 10¹³ ev) direct measurements are possible by sending balloon and satellites to high altitudes. In the energy region 10^{10} – 10^{13} eV, the composition of the primary flux is given by Juliussen (1975), and is shown in Table 1.1. A comparison between this composition and that of the universe shows that there is a considerable excess of light nuclei (about 10⁶ times more) in the primary radiation. This can be explained by the fragmentation of heavier nuclei in penetrating the amount of matter in space (1 H atom cm⁻³) on their way to the earth. Another point from the table is an increase in the relative abundance of heavy nuclei with increasing primary energy. This is seen especially for iron where at 10^{13} eV, it is as abundant as hydrogen nuclei in primary cosmic rays. Balasubrahmanyan and Ormes (1973) suggest that at high energies ($> 1u^{14}$ eV), the composition of primary particles are dominated by iron nuclei. A considerable work of interest concerning this matter is given by Ulejniczak and Wolfendale (1977). They assumed a linear extrapolation to the higher energy region which was based on the measured low energy spectra of various components of the primary cosmic rays. They obtained the relative flux of iron nuclei to be only 25% for 10^{14} eV and 31_{20} for 10^{15} eV, which does not show firm evidence for much of a change in

Z Elements	Kinetic	energy per	nucleus	(eV)	
	10 ¹⁰	10 ¹¹	1012	10 ¹³	
l Hydrogen	58 <u>+</u> 5	47 <u>+</u> 4	42 <u>+</u> 6	24 <u>+</u> 6	
2 Helium	28 <u>+</u> 3	25 <u>+</u> 3	20 <u>+</u> 3	15 <u>+</u> 5	
3-5 Light nuclei	1.2 <u>+</u> 0.1	1.1 <u>+</u> U.1	0.6 <u>+</u> U.2	-	
6-8 Medium nuclei	7.1 <u>+</u> U.4	12.2 <u>+</u> 0.8	14 <u>+</u> 2	-	
lU-l4 Heavy nuclei	2.8 <u>+</u> 0.2	6 .7 <u>+</u> 0.5	10 <u>+</u> 1	-	
16-24 Very heavy nuclei	1.2 <u>+</u> U.2	3.6 <u>+</u> 0.4	4 <u>+</u> 1	-	
26-28 Iron group nuclei	1.2 <u>+</u> 0.2	4.5 <u>+</u> 0.5	10 <u>+</u> 2	24 <u>+</u> 7	
≽30 very,very heavy nuclei		0.007 <u>+</u> 0.004			

TABLE 1.1 : Composition of cosmic rays at high energies (after Julliussen et al, 1975).

composition. Information on the energy spectrum of primary particles in this energy has been summarized by Kempa et al (1974) and the result is shown in Figure 1.1. The most important aspect of the spectrum is the evidence of a "bump" in the region of $lu^{14} - 10^{15}$ eV. The existence of the bump may be due to the contribution of pulsars to the cosmic ray flux (Karakula et al, 1974).

1.3 ORIGIN OF COSMIC RAYS

Since the discovery of the cosmic radiation, the problem of the origin and the acceleration mechanism of these very high energy particles has been studied. The primary particles can in principle have three origins.

- (a) Solar origin.
- (b) Galactic origin.
- (c) Universal or extra-Lalactic origin.

(a) Solar origin : At first it was believed that the sun is the only producer of observed cosmic rays. The idea started after the observed increase of cosmic ray intensity at the time of solar activity was observed. It indicated that there is an acceleration mechanism available on the sun which can produce particles with energies up to 10 GeV. Later, it was suggested by some workers that particles of higher energies also originate from the sun where their energies are acquired from the interplanetary magnetic field (H) in storage time of $10^3 - 10^8$ years before reaching to the earth.

The objection to this idea could be seen from a calculation (Galbraith, 1958). The comparatively weak interplanetary magnetic fields ($\sim 10^{-5}$ gauss) are not able to confine a proton of 10^{14} ev to the solar system. This



Energy per nucleus, E(ev)

Figure 1.1 : The integral primary cosmic ray spectrum. Combination of data from Figure 2 and Figure 4 of Kempa et al (1974).

would result in an anisotropy of the radiation and it is not observed. Therefore, the sun cannot be the only cosmic ray source. The necessity of other cosmic ray sources and a more powerful mechanism of particle acceleration is required.

(b) Galactic origin : The assumption is that other stars like the sun in the yalaxy (containing 10¹¹ stars) generate cosmic rays. The required total observed flux would not be possible to produce. Therefore we have to look for additional sources in other types of star. Several suggestions have been made, for example, stars such as magnetic variable stars as well as novae and supernovae are considered. However, the energies obtained by particlesaccelerated at their region of origin are not likely to be as great as those observed for the highest energy particles. Therefore an additional acceleration process is necessary, which is possibly the collision of cosmic ray particles with magnetised gas clouds as they stream through the arms of the galaxy.

(c) Extra-Galactic origin : There is a suggestion that very high energy cosmic ray particles producing E.A.S. of great size have extra-galactic origin because their energies are too high to be confined within the galaxy by the galactic magnetic field. Therefore they leak out from one galaxy into space and then enter other galaxies to contribute an extragalactic component to the cosmic ray flux.

1.4 SECUNDARY PARTICLES IN THE ATMOSPHERE

On entering the earth's atmosphere, the primary particles which are now known mainly to be protons and α -particles, interact strongly with the nuclei of the air

molecules. In these interactions a variety of secondary particles are produced. They are mainly of π -mesons (pions) and are partly kaons, hyperons and nucleons. The secondary pions have three charge modes (π^+ , π^- and π^0) which are produced in equal numbers.

The neutral pions decay with life time of 10⁻¹⁶ sec into two photons and further the two photons produce an electron-photon cascade in the atmosphere. The enormous number of electrons and photons forming the electromagnetic cascade of L.A.S. originate from these neutral mesons.

Cosmic ray muons are the result of charged meson decays and because of their relatively long life time (2.10^{-6} sec) a considerable flux of them is observed at sea level. In E.A.S. they form the muon component where the properties of these muons reflect the characteristics of the nuclear interactions from which their parent mesons originate.

At sea level most of the particles in a shower are electons and muons, and the propagation of these and other secondary particles through the atmosphere is shown in Figure 1.2 where a proton primary particle is assumed.

1.5 THE QUARK SEARCH

Since the introduction of quark theory, many experiments have been performed to search for these fractionally charged particles. Naturally the search was first carried out at accelerators where carefully controlled experiments could be done. The negative results of accelerators indicate that the quark mass may be greater than the maximum kinematically possible for production at present accelerator energies. This was the reason that attention was

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Figure 1.2 : Diagram showing the major processes taking place in the atmosphere when an extensive air shower is observed at sea level.

focused on searches in cosmic rays which are sources of much higher energies. The unique importance of cosmic rays comes from the fact that it is the only beam of particles with energy greater than 10^{12} eV that exists in the nature. The present search for quarks is described in Chapter 7, where an investigation close to the core of E.A.S. with medium size 3.10^5 particles is described.

1.6 THE SIGNIFICANCE OF COSMIC RAY STUDIES

It is the broad cosmic ray energy range from about 10^{8} eV to an unknown upper limit (recorded up to 10^{20} eV) which makes it of interest in two different fields of study. These are studies aimed at obtaining new information in the fields of elementary particle physics (e.g. quarks) and astrophysics (sources, acceleration mechanisms, composition etc). It was cosmic ray studies that led to the discovery of many fundamental phenomena such as the observation of very high transverse momentum of secondary particles in some collisions and the change of their multiplicity with energy etc. which is of importance in the investigation of high energy collisions.

Over the years, most of the elementary particles such as muons, mesons and kaons, have also been discovered in cosmic rays where their properties were qualitatively known before using accelerators to study them. Accelerators which produce artificial particle beams can be used up to energies of about 10^{12} eV. To increase the beam energy of accelerators up to 10^{15} eV will take some time and even then this energy is in the relatively low cosmic ray energy range. In spite of this problem, accelerators are still of great importance

since they give good information concerning low energy nuclear interactions which is compared and extended in cosmic ray experiments.

The cosmic rays have also been the source of search for particles theoretically predicted such as quarks, tachyons and magnetic monopoles.

Cosmic rays are also a powerful source of astrophysical information where high energy X and γ rays are the examples of reliable sources of interest.

Also, very high energy cosmic ray particles in the E.A.S. region with $Ep \ge 10^{15}$ eV are of interest because of the reason that they may not be affected greatly by existing magnetic fields on their way to earth and hence show the direction of the source. They are also a probe to investigate the condition of the galaxy and beyond it which is of astronomical interest.

Chapter 8 gives the arrival direction analysis of E.A.S. in galactic coordinates where any preferred arrival direction (e.g. a point source) has been investigated in some detail.

CHAPTER 2

THE DURHAM E.A.S. ARRAY AND THE FLASH TUBE CHAMBER

2.1 INTRODUCTION

The flash tube chamber is a large visual detector and has been used in conjunction with the Durham E.A.S. array to study the characteristics of E.A.S. at sea level. It was originally built to search for quarks and later was modified to look at strongly interacting particles (hadrons), through their burst production in the chamber.

The major aim of the present experiment was to investigate the muon component of E.A.S, but because of the observation of some low efficiency tracks throughout the experimental runs, an effort was also made to identify whether any low ionizing tracks could have been produced by fractionally charged particles (quarks). The array information apart from using it to measure the major shower parameters (i.e. core position and shower size), was also used to study the electron structure function of E.A.S. which is characterised by the age parameter of the shower. Also, from the density information of the array, the fluctuations of the electron density were also studied in some detail.

2.2 THE FLASH TUBE CHAMBER

2.2.1 Construction of the Chamber

The scale diagram of the neon flash tube chamber is shown in Figure 2.1. The chamber has been constructed of about 11000 flash tubes. The tubes are cylindrical and 2 metres in length with mean external diameter 1.78 cm and an internal diameter of 1.58 cm. They are made of soda glass



20cm

Figure 2.1 (a) : Front view of the chamber.





Figure 2.1 (b) : Side view of the Chamber.

filled with neon gas (98%) and helium gas (2%) to a pressure 60 cm of mercury.

The tubes are covered with polythene sleeving to prevent light passing through the neighbouring tubes. The tubes are distributed in 124 layers of 84 or 85 tubes per layer and between every two layers of tubes is an aluminium electrode, 0.122 cms thick and with an area of 2.94 m². The arrangement of different sections of the chamber is shown in Figure 2.1 . From the top to the bottom, it consisted of a layer of 15 cm of lead, 8 layers of flash tubes (Fla.), a layer of 15 cm of iron, three plastic scintillators, each 1.05 m² area designated A plus a further 4 blocks of flash tubes, Flb (6 layers), F2a (46 layers), F2b (48 layers) and F3a (8 layers), three plastic scintillators each of 1.05 m^2 area (B) and the final part is 8 layers of flash tubes (F3b). The scintillators (A and B) were not used in the present work. The shielding materials of the chamber are the 15 cm of lead absorber on the top and at the sides 30 cm barytes concrete walls designed around the chamber to cut out the soft component (electrons and photons) of E.A.S, while allowing penetrating particles (muons) to pass through the chamber. During the time that the experiment is running, the chamber remained in the dark and the photographs are taken by a camera without a shutter. This means that the camera is continuously sensitive to an event and it winds on automatically by one frame after each event.

2.2.2 The High Voltage Pulsing System

A high voltage pulse is applied to the electrodes of the chamber to operate the flash tubes which are affected by

the passage of the particles. It is supplied by a high voltage pulsing system which consists of a thyristor pulsing unit and an air spark gap shown in Figure 2.2. The high voltage pulse is produced after the triggering requirement of the array is established. It is produced by a 5 volt trigger pulse which is used to trigger a thyristor, producing an output pulse of 300 volts. This voltage pulse is applied to the primary of a high voltage transformer and produces an output as the trigger pulse for the spark gap. A voltage of 16Kv is applied across the main spark gap, which causes the gap to break down when the trigger spark is produced. The pulse applied to the electrodes of the chamber has a shape which is approximately rectangular with a height of 8 KV and a length of 10 µs.

2.2.3 Properties of Flash Tubes

When a charged particle passes through a flash tube it ionizes the gas and leaves a trail of positive ions, electrons and excited atoms along its track. After a time delay between the passage of the ionizing particle the high voltage pulse is applied to the electrodes. This causes a breakdown of the neon gas in the tube and avisible discharge results in the tube. The problem of ionization and what causes the discharge has been discussed in detail by Lloyd (1960). The conclusion is that only the electrons which are produced initially are responsible forthe discharge. He concluded that positive ions, metastable neon atoms and produced photons do not contribute to the probability of discharge and can have little or no effect.

Lloyd set up diffusion equations for electrons



Figure 2.2 (a) : High voltage pulsing unit.



Figure 2.2(b) : Spark gap and delay line.

produced in the tube and solved them. The solution gave the probability of a discharge occurring, when a high voltage pulse is applied to the tube in a time $T_{\rm D}$ after passage of a charged particle. This probability is known as the internal efficiency, and he expressed it as a function of $\frac{D \cdot T_D}{2}$ and in terms of a parameter af_1Q_1 , where D is the diffusion coefficient of thermal electrons, a is the internal radius of the tube, f, is the probability that a single electron is capable of producing a flash when a high voltage pulse is applied, and Q₁ is the number of initial electrons produced per unit length in the neon gas. The only parameter dependent on the charge of the particle is Q_1 and is related to the ionization loss of the particle in the gas which is a function of the square of the electric charge. This forms the basis of the use of the flash tube chamber in the search for quarks, since the term af_1Q_1 is 1/9 for a particle of e/3 compared to that of charge e. Using the Lloyd theory, the internal efficiency of the tube as a function of time delay for different values of the af_1Q_1 parameter has been calculated and are shown in Figure 2.3. It is seen from this figure that the efficiency of the tube falls off as the time delay increases. This is due to the fact that the initial number of electrons in the gas will decrease due to diffusion to the glass tube walls where they The longer the time delay the greater is the probstick. ability that no electrons remain in the gas.

2.3 THE E.A.S. ARRAY EXPERIMENT

2.3.1 introduction

The Durham E.A.S. array consists of 14 plastic scintillation counters which are located around the neon



delay for different values of the parameter afQ. afQ = 10 gives a good fit to the measured efficiency versus time delay curve for relativistic muons traversing the chamber.

flash tube chamber inside a cirlce of radius of $\simeq 60$ m. The detectors have areas varying from $2m^2$ to 0.75 m². The location of these detectors are shown in Figure 2.4, which are essentially arranged in a triangular symmetry. All of the detectors are used to obtain the density measurements and seven of them also give the fast timing information. (he density and fast timing detectors are the central detector, C, 0.75 m^2 and six 2 m² detectors, which are also shown in Figure 2.4. These detectors give time markers when the shower front passes through them, which are relayed to the laboratory, where they are converted into time differences relative to the time the shower front passes through the central detector C and stored to determine the arrival direction (Θ and ϕ) of the shower. The operation mechanism of the array will be given later, when the various kinds of detectors are described in the next section.

2.3.2 The Detecting Elements and Fast Timing Technique of the Array

The main detecting elements of the array are plastic scintillation counters. These are the 2 m^2 detectors, 11,13,31,33,51,53, the central 0.75 m^2 detector C, the 1 m^2 detectors 41,52,32 and the 1.6 m^2 detectors 42,12,62,61. The first two sets of detectors are used to select E.A.S. events as well as for density and fast timing measurements, and the rest are used only for particle density measurements. The detectors consist of one or more slabs of plastic scintillator viewed by four photomultiplier tubes to measure the particle densities in a shower. The fast timing detectors have an extra one or two fast timing tubes (Philips 56 AVP), to



Figure 2.4 : Scale diagram of the Durham Extensive Air Shower Array.

generate the fast timing pules.

It is the relationship of the time delays between pulses which is of interest and gives information on the arrival time of the shower front for the determination of the shower axis spatial direction. To do this, 6 time to amplitude converters (T.A.C's) were used, and the procedure was to take a pulse from the central detector C to start each of the six T.A.C's and stop them by the pulses from the relevant detectors. These pulses are already artificially delayed by various timing cables such that the central detector pulse (common pulse) always arrives in the laboratory before any other pulse. Therefore, the produced outputs of the T.A.C's are proportional to the time difference of the central detector pulse and one of the other detector pulses which are required to calculate the arrival direction of the shower (0 and ϕ) where the various delays in the cables are known.

Each detector also contains a head amplifier and E.H.T. distribution unit which are attached to the wall of the detector box. The box of the scintillator is made of wood and is weather-proofed with bitumen paint and aluminium foil, covered and protected also by a weather-proofed hut.

2.3.3 The E.H.T. Distribution units and the Head Amplifiers

The E.H.T. distribution units are used to supply the high voltage needed for the two types of photomultiplier tubes in the array. Each type of tube needs a working voltage which, in the present case, are set to be 2.4 KV and 2.7 KV for the density and fast timing tubes respectively. The high voltage supply to each detector is connected to a resistor chain

through a coaxial cable. Since the voltage of the similar tubes in a detector (i.e. slow tubes) are not exactly the same, the resistor chain is used to adjust and distribute each tube voltage independent of the others. A resistor chain is shown in Figure 2.5 which represents the sections of the E.H.T. distributions at each detector. In each detector there is also a mixer amplifier which is used to add and amplify the output pulses of the four density photomultiplier tubes of each detector, as is shown in Figure 2.6. A +24 volt power supply unit in the laboratory is used to operate all the amplifiers in the array.

2.3.4 The Linearity of Response of Photomultiplier Tubes

In the array there are three types of photomultiplier tubes, (P.M.T), their purpose being to convert the light output of the scintillators into electrical pulses which in turn is a measure of particle number. One of the necessary characteristic of the tubes which should be known is their response to various light input intensities. To examine this, light emitting devices could be used (i.e. light emitting diodes) to give similar light pulses to those obtained from the scintillator. As the intensity of light falling on the tubes could be varied, it was possible to examine the linearity of response of the P.M.T. as a function of light input. The investigation was made for all three different tubes. It was found that the tubes were linear over the range of applied voltages in the present experiment.



Figure 2.5 : A resistor chain (After Smith, (1976))



Figure 2.6 : Four input mixer amplifier (After Smith, 1976).
2.3.5 Calibration of the Detectors

A telescope and a multi-channel analyser (M.C.A) are used to calibrate the individual detectors. The telescope consisted of a 23 x 23 x 3 cm plastic scintillator viewed by two photomultipliers (Philips 53 AVP). It was used for the calibration of the density tubes, where the E.H.T. on the tube was adjusted such that the peak of the particle distribution coincides with the desired calibration value, which could be stored and shown on a M.C.A. in the laboratory. The density tubes were adjusted such that after dividing the sum of the overall pulse heights (from 4 tubes) by 100 mV, the number of particles per square metre at the detector is obtained.

2.3.6 The Data Handling Electronics

When an air shower traverses the array and satisfies the triggering condition, all the density and timing data which are now in analogue forms and are presented to an analogue to digital converter. The data are held for 2 ms and in this period each analogue signal is presented in turn to the analogue to digital converter, and the digitised pulse height is then stored in a buffer memory. Eleven events are stored in this way before the contents of the memory are automatically transferred to the magnetic disc of the on-line computer, later to be analysed.

Another set of information which is obtained by the array called "book-keeping" and is as follows :-

the event number
 the run number
 the triggering mode of the event
 the occurrence time of the event

The necessity for this is in the identification of the event. Figure 2.7 shows a block diagram of the data handling electronics. More detail information of the data handling electronics is given by A.C.Smith (1976).



Figure 2.7 : The data handling electronics (After Smith(1976)).

CHAPTER 3

THE ELECTRON COMPONENT OF E.A.S

3.1 INTRODUCTION

Electrons are the most numerous and convenient particles to measure and study than any other existing particles in E.A.S. (i.e. muons and hadrons). The knowledge of this component is essential to get information about the other shower parameters since it provides the initial parameters required for any further measurement in E.A.S. One of the initial parameters is the correct form of the electron lateral structure function which makes it possible to have an accurate method of core location and a measure of the total number of electrons which are a necessity to interpret the shower data.

3.2 THE ELECTRON LATERAL STRUCTURE FUNCTION (E.L.S.F.)

Since the detailed knowledge and appropriate form of the E.L.S.F. is of initial importance in the investigation of L.A.S, it has therefore been the most often repeated experiment. It has been measured using different techniques and has been found that the form of the structure function is slightly dependent on the type of the detectors used. Experiments performed with Geiger-Mulier counters give a good measure of the actual electron density distribution, where the ones performed with scintillation counters give slightly steeper distributions. This is due to the sensitivity of the scintillator to the photon component of the shower.

An empirical formula for the E.L.S.F. has been

suggested by Greisen (1960) which is based on experimental measurements. This formula has the following form :

$$\Delta(N, \mathbf{r}) = \frac{0.4}{r_1^2} \left\{ \frac{r_1}{r} \right\}^{0.75} \left\{ \frac{r_1}{r_1 + r} \right\}^{3.25} \left\{ 1 + \frac{r}{11.4} \frac{r_1}{r_1} \right\}^{m^{-2}}$$
(3.1)

where N is measured in units of single particles and r is in metres. According to Greisen it is valid for sizes from 2.10^3 to 2.10^9 charged particles, core distances 5 cm to 1500 m from the shower axis, and zenith angles less than 55°, r₁ is the Moliere unit (79 metres at sea level).

Hasegawa et al (1962) measured the E.L.S.F. employing an array of scintillators where the result is presented by the following expression

$$\Delta(N,r) = \frac{N}{2\pi\sqrt{120}} \frac{e}{r^{1.5}} m^{-2}$$
(3.2)

A detailed analysis of measurements by the scintillation counter is given by Catz et al (1975) in the following form :

$$\Delta(N,r) = 0.al5 N - \frac{e}{1.62} m^{-2} (3.3)$$
(r+1)

where the function is valid for the distance range of 2 m to at least 70 m from the shower axis. In both these formulae N is measured in units of single particles and r is in metres. For comparison of the above three mentioned forms of structure function, they are presented in Figure 3.2, the Hasegawa et al (1962) measurements show a steeper density distribution than that of Greisen (1960) where the Catz measurements, apart from

small core distances seems to agree rather well with it. In the present experiment, the showers were recorded by the Durham E.A.S. array (see previous chapter) where an E.A.S. selection of the form $\Delta_{C}(\ge 3.5)$, $\Delta_{13}(\ge 1.5)$, $\Delta_{33}(\ge 1.5)$, $\Delta_{53}(>1.5)$ was used (the figures in brackets are the number of particles per square metre at the corresponding detector). For each E.A.S. event, 10 electron density samples are normally recorded. Four of these densities have been used to locate the position of the shower core using the method of intersecting loci and E.A.S. size has been determined using the Greisen E.L.S.F, (Eqn. 3.1). For each shower, 6 density samples are normally available to check the core position to see whether they are consistent with the assumed E.L.S.F. In order to present average E.L.S.F. of many events on one graph, the measured densities have to be normalized to a fixed size (10⁵ particles in the present work). Normalization means the measured densities in a shower of size N, $\Delta(N,r)$ are converted to densities that would have been measured in a shower of size 10^5 particles, $(10^5, r)$ using

$$^{\Delta}(10^{5},r) = \frac{10^{5}}{N} \cdot ^{\Delta}(N,r)$$
 (3.4)

The normalized densities were obtained for a sample of 98 showers and are plotted as a function of core distance, r in Figure 3.1. From the figure, the average of the densities obtained over small intervals of core distance was calculated and the result is shown in Figure 3.2. It is seen that the average measured densities (representing the average E.L.S.F. of the showers) are consistent with the Greisen structure function, especially in the core distance range of 20<r<60 m.



Figure 3.1 : Test of the consistency of the electron densities measured in detectors not used in core position and shower size determination with the Greisen (1960) and Catz et al (1975) lateral structure functions.





The structure function found by the Hasegawa and Catz E.L.S.F. are also shown in Figure 3.2 for comparison. The Greisen E.L.S.F. has also been checked with the individual showers. The redundant densities of the individual shower were compared to the function. The result obtained showed that 84 showers were consistent with Greisen structure function while 6 and 8 showers showed a flatter and a steeper function respectively.

3.3 METHODS OF CORE LOCATION

The methods available are basically of two types. The loci curve method which was first introduced by Williams (1948) and the other method is using a computer when a minimum χ^2 procedure is performed. For any method of core location, the sampling densities are used to determine the core position while an E.L.S.F. is assumed.

3.3.1 Loci Curve Method

In the loci curve method the ratio of the electron densities from any two detectors is of interest since it determines a line which is the locus of all the possible cores falling on the array producing that ratio. Therefore from a minimum of 3 densities in a shower, two independent density ratios are obtained, which define two loci curves whose corresponding ratios intersect in a point which is the axis of the shower.

In practice, it is not exactly the case, and at least 3 electron density ratios from 4 detectors are used, where the extra ratio defines a checking locus curve which should intersect in the core position located by the other two loci if the E.L.S.F. is correct. The loci curves so produced for

a number of detectors do not generally intersect at a single point due to density fluctuations and the non-uniqueness of the E.L.S.F. However the centre of gravity of the overlapping area provides a good estimate of the core position.

To improve the method and to get a better estimation of core location, the two error limits related to each density ratio was also used to calculate locus curves. Figures 3.3 and 3.4 show examples of the core position located by this method. The loci curves corresponding to the error limits are shown by dotted lines. The errors related to a locus curve with density ratio $y = \frac{\Delta_a}{\Delta_b}$ is

$$\frac{\Delta y}{y} = 1,2 \left(\frac{1}{\Delta_{a} \cdot A} + \frac{1}{\Delta_{b} \cdot B} \right)^{\frac{1}{2}}$$
(3.5)

where Δ_{a} is the electron density measured by detector a of area A, and Δ_{b} is the electron density measured by detector b of area B. The factor 1.2 comes from electron density fluctuation which is found to be 1.2 \sqrt{n} (see section 3.5) where n is the number of detected particles.

To prepare a core locating chart for two detectors with distance ℓ apart one chart is obtained when an E.L.S.F. is assumed. In the present case the Greisen structure function was used which, for a shower falling at core distances of r_a and r_b from the detectors a and b gives a density ratio of $\sqrt{0.75}$ $\sqrt{3.25}$ $\frac{r_b}{11-6}$

$$\frac{\Delta}{\Delta_{b}} = \left(\frac{r_{b}}{r_{a}}\right)^{0.75} \left(\frac{r_{b}+r_{o}}{r_{a}+r_{o}}\right)^{3.25} \left(\frac{\frac{1+r_{o}}{1+r_{o}}}{\frac{1+r_{a}}{1+r_{o}}}\right)$$

22

(3.6)





where Δ_{a} and Δ_{b} are the densities expected in detectors a and b. From Eqn. 3.6, for various values of r, the density ratio, $\frac{\Delta_a}{\Delta_i}$ is plotted as a function of r_b which are shown in Figure 3.5. From the figure, for each density ratio, various values (r_a, r_b) are obtained and, the locus curve of that ratio is drawn for any two detectors. An example of a core locating chart for loci curves of various density ratios is shown in Figure 3.6, where detectors C and 62 were chosen. the loci method is sufficiently accurate provided the shower core has fallen within or near the array boundary. For core distances less than 72 metres from the centre of the array. simulation work was performed where in simulating the shower the fluctuation on the number electrons n at a detector expected by the Greisen E.L.S.F. is assumed to be Poissonian of standard deviation (S.D) 1.2 \sqrt{n} (see section 3.5). With this assumption, the S.D. of the difference in true core distance from the centre of the array, C and the core distance located by the method of intersecting loci for a sample of simulated showers was found to be (5.88 + 0.44)m.

3.3.2 Computer Method of Core Location

For a given set of measured electron densities the problem is to determine the core position and shower size assuming the electron lateral structure function is known. In practice a search is made over a lattice of points and a minimum χ^2 procedure is used to determine the best core position and shower size

$$\chi^{2} = \sum_{i}^{i} k_{i} (\Delta_{i}(0) - \Delta_{i}(P))^{2}$$
(3.7)

where K_i is a weight function given by σ_i^{-2} and σ_i is the standard deviation of the density measurement (see next section).







 $\Delta_{i}(0)$ is the observed density and $\Delta_{i}(P)$ is the predicted density from Eqn. 3.3. The χ^2 minimizing procedure normally starts from a point chosen near the highest density detector in the array which gives a good estimation of the core position. By assuming this starting point (X_s, Y_s) the value of N that gives minimum χ^2 is obtained. The χ^2 calculation is repeated over either a lattice of points that cover the array or various random points chosen uniformly around the starting point (X_s, Y_s) where a step size (Δ_x, Δ_y) is taken on any point (X,Y) to shift it to a new position. The χ^2 values of the data are compared to get the real core position and shower size by its corresponding minimum χ^2 . The method has been described by Clark et al (1958) and more recently by Evans (1971) and Smith (1976). The present core location analysis was performed by a versatile minimizing package known as MINUIT (James and Hoos, 1975). The system has basically the same performance of minimization but with much greater accuracy when the processing time of each event is 2 to 3 seconds to be analysed.

For comparison of the method of loci curves and computer analysis to determine core position, a sample of 189 shower was used where the difference in core distance from C (the centre of the array) located by the two methods was calculated. The difference was found to be Gaussian with S.D. of 3 metres.

3.4 CONCLUSION

For showers of size in the range 10⁵-10⁶ particles and core distance less than 72m from the centre of the array the error in core position as determined by the method of inter-

secting loci is (5.88 + 0.44)m.

3.5 ELECTRON DENSITY FLUCTUATION

The loci curves method was applied for an array of 10 electron density sampling detectors where 4 measured densities were used to locate the core position and determine shower size assuming the E.L.S.F. is known. The remaining detectors that give normally 6 measured densities can be taken both to check whether the assumed form of E.L.S.F. is correct and also to give information on the magnitude of density sampling fluctuations. In section 3.2 it was found that the Greisen formula, Eqn. 3.1, is quite consistent with the experimental density measurement. To get information on sampling density fluctuation, the observed number of particles n_ at the detectors of area 0.75 to $2m^2$ were plotted versus the expected number n assuming the Greisen formula to be the correct E.L.S.F. of all showers. Figure 3.7 shows a plot of n_{p} versus n_{p} for density samples in which $n_{p} \leq 20$ particles. The data is taken from a sample of 98 E.A.S. of median size 3.10⁵ particles whose cores fell at distances < 70m from the centre of the array. The upper and lower standard deviation limits are shown in Figure 3.7 assuming Poisson fluctuations. For $n_e > 10$ these are $n_e + \sqrt{n_e}$ and $n_e - \sqrt{n_e}$ respectively but for smaller values of n the limits given by Regener (1951) are shown. If the fluctuations are Poisson then 68% of the observed events should lie in the range $n_e - \sigma_1$ to $n_e + \sigma_2$ where σ_1 and σ_2 are the S.D. limits. Breaking the data down into 2 ranges of shower size, and considering observations with n_< 20 particles and n_> 20 particles separately, the observed percentage of events lying in the range $n_e - \sigma_1$ to $n_e + \sigma_2$ is compared with expectation in Table 3.1. It is seen that



Figure 3.7 : Scatter plot of observed number of detected particles versus the expected number. The full lines are the upper and lower standard deviation limits of a Poisson distribution on the expected numbers which have been calculated using the Greisen lateral structure function.

Expected no. of detected particles	Shower size range	No.of density samples	Expected percentage in range ⁿ e ± σ assuming Poisson statistics	Ubserved percent- age in range ⁿ e ± σ
n _e ≼ 20	7.4.10 ⁴ <n<3.3.10<sup>5</n<3.3.10<sup>	342	68%	(73 <u>+</u> 5)%
	3.3.10 ⁵ < N×2.7.10 ⁶	281	68%	(55 <u>+</u> 4)%
n _e > 20	7.4.10 ⁴ < N×3.3.10 ⁵	32	68%	(54 <u>+</u> 4)%
	3.3.10 ⁵ < N<2.7.10 ⁶	145	68%	(47 <u>+</u> 6)%

TABLE 3.1 :Comparison of the percentage of observed
events lying in the range n_e with expectation
for different ranges of the expected number
of particles n_e and shower size.

there is a suggestion that the observed fluctuations are broader than expected, assuming a Poisson distribution but not considerably so. If one assumes that the standard deviation limits are given by $n_e - k \sigma_1$ to $n_e + k \sigma_2$ such that 68% of all events lie in this range exactly, then grouping all the data together gives k = 1.2.

Brennan et al (1958)and Clark et al (1958,1961) have made a similar study to the present one using showers of size $\sim 10^5$ particles and $\sim 10^5 \sim 10^8$ particles respectively at sea level. clark et al (1961) found K = 1.15 at distances > 50m from the core for showers in the range 5.10^5 <N < 10^8 particles. Kitajima et al (1979) studied density fluctuation of near vertical showers ($0 < 30^{\circ}$) at distances of 30m from the core for showers in the range $10^6 < N_p < 4.10^7$ particles. They found the value of K = $(0.25 + 0.0225 \text{ n}_{\text{s}})^{\frac{1}{2}}$ which indicates the fluctuation gets broader than Poissonian for n_e> 33 particles and increases slightly with n_e. However, if consideration is taken of errors in core location, shower size determination, fluctuation in the shape of the structure function and also in the actual density recording process (e.g. low energy hadron interactions in the scintillators, etc.) then it would seem likely that both in the present work and previous work the true fluctuations in electron numbers sampled by a detector are closely represented by the Poisson distribution.

CHAPTER 4

THE AGE PARAMETER OF E.A.S. AND ITS DEPENDENCE

ON SHOWER SIZE AND ZENITH ANGLE

4.1 INTRODUCTION

4.1.1 The Electromagnetic Cascade Shower

So far, a lot of work has been done on the theory of the electromagnetic cascade. An example is the summary of Cocconi (1961) which discusses the one dimensional development of an electron-photon shower in the air. The calculations used are from Snyder (1949) where the total number of electrons of energy $E \ge 0$ initiated by a primary photon of energy W_0 is given as a function of air thickness. The results for various values of W_0 are shown in Figure 4.1, where they can be represented by the following equation due to Greisen (1956).

$$N(W_{0},t) = \frac{0.31}{\beta_{0}^{\frac{1}{2}}} \exp \left[t \left(1 - \frac{3}{2} \log S \right) \right]$$
(4.1)

 $t = \frac{X}{X_0}$ is the air thickness in radiation units, $X_0 (X_0 = 37.7 \text{ gr cm}^{-2} \text{ in air}), \beta_0 = \log \frac{W_0}{\epsilon_c}, \epsilon_c$ is the electron critical energy in air (84.2 MeV) and $S = \frac{3t}{t + 2\beta_0}$. The parameter S is known as the age of the shower and is related to the development of shower properties. From Equation 4.1 and Figure 4.1, the shower reaches its maximum development when S = 1 at the thickness of

$$t_{\max} = \beta_0 = \log \frac{W_0}{\varepsilon}$$
(4.2)



Figure 4.1: The total number of electrons, as a function of the thickness $(g \text{ cm}^{-2})$ of air crossed, produced by photons of various energies, W_0 , in eV. The parameter s is the age of the shower at different stages of its development, (after Cocconi, 1961).

where before and after its maximum S is less and bigger than one respectively. The relation of age parameter to the number of particles in the shower at any level and the energy of the primary particle is also given by Equation 4.1 as

$$\frac{d \log N}{d \log W_0} = S - \frac{1}{2\beta_0} \gtrsim S$$
 (4.3)

(the approximation is for high energy primary particles, i.e. $u_0^{>>} \varepsilon_0$).

4.1.2 The Age Parameter of E.A.S

The behaviour of the electron and photon cascade is well described in terms of cascade shower theory by Nishimura and Kamata (1958). According to this theory, the definition of the age parameter S in shower development is given by

$$5 \sqrt[3]{t} (t + 2 \ln (\frac{E_o}{c}) + 2 \ln \frac{r}{c}) \qquad (4.4)$$

where E_0 is the electron primary energy in c_c units, c_c is the electron critical energy in air, t the atmospheric depth, and r the radial distance from the core (Greisen, 1956). The parameter S represents the age of a shower which increases as it develops, and reaches its maximum when S is equal to one. For S less than one it shows the early stage of development (young shower), and for S greater than one it shows the declining stage of a shower (old shower). Equation (4.4) shows the decrease of S as the distance from the shower axis increases. This corresponds physically to the fact that the maximum of a shower is reached later for the high energy particles near the axis than for the low energy particles far from the axis. Also in 1952 and 1958, Nishimura and Kamata derived the lateral structure function of E.A.S. particles, which was based on a pure electromagnetic cascade considering the multiple Coulomb scattering of electrons. This function can be simplified by an expression due to Greisen known as the Nishimura-Kamata-Greisen, (N.K.G), function, which is given as

$$F(r_0) = C(s) (r/r_0)^{S-2} (\frac{r}{r_0} + 1)^{S-4.5}$$
 (4.5)

where r_0 is 79 metres for air at sea level, and C(s) is a normalization factor such that

$$\int_{0}^{\infty} 2 \pi F(x) X dx = 1 \text{ where } X = \frac{r}{r_{0}}$$
(4.6)

and can be approximated by (Greisen, 1956)

$$C(s) = 0.443 S^2 (1.09 - S) \text{ for } S^{<} 1.6$$

or $C(s) = 0.366 S^2 (2.07 - S)^{5/4} \text{ for } S^{<} 1.8$

Exact values of C(s) according to Wdowczyk (1973) are given in Table 4.1, which are consistent with the last formula

S	0.6	0.8	1	1.2	1.4	1.6	1.8
C(s)	0.22	0.31	0.4	0.44	0.43	0.36	0.25

TABLE 4.1

as shown in Figure 4.2. These values of C(s) were used in the data analysis. Assuming the lateral distribution function



Figure 4.2 : Consistency of the values of normalization factor as a function of age parameter.

is independent of shower size, for a shower with a total of N particles, the electron density at distance r from the core is given by

$$\Delta(\mathbf{r}) = \frac{N}{r_0^2} F(\mathbf{r}/r_0)$$
 (4.7)

Figure 4.3 shows a plot of $\Delta(\mathbf{r})$ versus \mathbf{r} for $\mathbf{N} = \mathbf{l}$ and shows how S determines how peaked or flat the structure function of the shower is. Also, the fraction of particles in a shower that fall at a distance greater than \mathbf{r} from the core was calculated and the results are given in Appendix A.A₁.

4.1.3 Central Density

By assuming the N.K.G. function for the lateral distribution of electrons in different development stages of E.A.S. and measuring the age parameter of individual showers, one may get some information on the shower central density. Central density is a useful parameter due to the fact that it is roughly proportional to the energy per nucleon of the primary particles, whereas the total number of particles represents energy per nucleus (Bray et al, 1964, Thielheim and Beiersdorf, 1970). It was suggested by the Sydney group (Bray et al, 1964) that the distribution of $^{\Delta}c/N$ values of showers ($^{\Delta}_{c}$ - central density in a shower of size N) might contain some information on the chemical composition of the primary particles. For a given size the mean value and fluctuation of this quantity are expected to be smaller for heavy primary particles than for primary protons.

4.2 EXPERIMENTAL ARRANGEMENT AND ANALYSIS

The Durham E.A.S array was previously described in Chapter two and a scale diagram of it is shown in Figure (2.1).



of the shower.

Air showers were selected by an outer ring Trigger ; a 2 particles m^{-2} coincidence in detectors 13,33,53 with a 4 particles m^{-2} in the central detector C, where the area of the detectors varies from 2 m² to 0.75 m². For each event the sampled electron densities were used to measure the age parameter of the shower (S was determined by assuming the core position found using the Greisen structure function was correct and the best S and N that fitted the measured electron densities in E.A.S detectors was then found. This was achieved by computer using the CERN MINUIT program which is a package for minimizing a function of n parameters. The program for two parameters, age and shower size, is given in Appendix A.A. In deriving the age parameter distribution, we have to consider the fact that the efficiency of triggering depends on age for a given shower size. The requirement for an E.A.S trigger is that the density of particles in each triggering detector exceeds a certain level. Since the density given in Equation 4.7 depends on S, the distance from the axis r is a function of N and S for a given Δ . Hence the effective collecting area depends on S as πr^2 (N,S) for a given triggering level of \triangle . For the present triggering level, the minimum shower size to produce an outer ring trigger as a function of age is given in Figure 4.4. Figure 4.4 shows the minimum size to be triggered by a shower of all ages to be 2.3.10⁵ particles which is why it was chosen to be the minimum analysable shower size. An example of collecting area for different ages S = 0.6 and S = 1.8 of fixed sizes 5.10⁵ and 5.10⁶ particles are shown in Figure 4.5a and Figure 4.5b which gives a bigger collecting area for flatter



Figure 4.4 : Variation of minimum shower size to produce an outer ring trigger as a function of age parameter.



6



Figure 4.5a ; Collecting areas for showers with s = 0.6and N = 5.10⁵ and 5.10⁶ particles capable of producing an outer ring trigger.



outer ring trigger.

showers (5 = 1.8) than steep ones (5 = 0.6). The curves of collecting area as a function of size were calculated for different age and are shown in Figure 4.6, which will be used in the data analysis.

656 events were grouped into three ranges of shower size, $2.3.10^5 - 5.10^5$, $5.10^5 - 5.10^6$ and $5.10^6 - 5.10^7$ particles which are shown in Table 4.2, where in each size range the measured distribution of age for showers having orthogonal core distance of less than 105 metres from C was obtained. The resulting data was further sub-divided into two ranges of zenith angle ($0 < 22^{\circ}$ and $0 \ge 22^{\circ}$) the results being shown in Figure 4.7 to Figure 4.12b, the distribution (full lines) are for the showers triggered by the array. The measured age distributions were corrected for the variation of collecting area with shower age as shown by the dashed lines in Figures 4.7, 4.9 and 4.12a, where the orthogonal core distance cut-off was taken to be 105 metres. This was done by using the curves of Figure 4.6, which for any shower of fixed size shows the variation of its collecting area with age which makes it possible for a given area to obtain the relative collecting probabilities of a shower of various ages. Practically, to obtain corrected distribution from the measured distribution for every interval of age its average age, \overline{S} and size \overline{N}_{a} were calculated and by using Figure 4.6 the corresponding collecting areas A (\bar{S}, \bar{N}_{a}) were obtained. These areas were used to get the relative collecting probabilities for all intervals which were the ratio of their collecting area to a given area, i.e. area $(\pi r_c^2 : r_c = 105 \text{ m}) = 3.4.10^4 \text{ m}^2$. These ratios, or collecting probability factors, have been multiplied by their corresponding



Figure 4.6: Collecting area as a function of shower size for showers with different age parameter detected by an outer fing trigger, $\Delta_{c} (\geq 4m^{-2}) \cdot \Delta_{13} (\geq 2m^{-2}) \cdot \Delta_{33} (\geq 2m^{-2}) \cdot \Delta_{53} (\geq 2m^{-2}) \cdot$

Size range	2.3.10 ⁵ -5.10 ⁵	5.10 ⁵ -5.10 ⁶	5.10 ⁶ -5.10 ⁷	Total
Total number of events for 0 < 22 ⁰	134	186	21	341
Total number of events for 0 ≥ 22 ⁰	123	182	10	315
Total	257	368	31	656

<u>TABLE 4.2</u> : The total number of analysed events detected by the outer ring trigger for two ranges of zenith angle ($0 < 22^{\circ}$ and $0 \ge 22^{\circ}$) and for three different ranges of shower size. r_{c} , the core distance from central detector was taken to be less than 105 metres.




















and two zenith angle ranges of $(\Theta \ge 0$ and $\Theta \le 22^{\circ})$.

frequency of measured age intervals to obtain the corrected frequency of every interval which are shown by the dashed lines. These dashed lines form the corrected distribution of age parameter for the three mentioned ranges of shower size where, in each range, an example of showers with various age parameter are given in Figures 4.13a, 4.13b and 4.13c. 4.3 THE RESULTS AND PREVIOUS MEASUREMENTS

4.3.1 The Shower Size and Zenith Angle Dependence

Theoretical predictions of the age parameter dependence on shower size and zenith angle of E.A.S were given by Karakula (1968), where the standard model of E.A.S. development was used. The results are given in Figure 4.15, after Wdowczyk (1973), which shows a small decrease of age parameter with increasing shower size, where the decrease is more pronounced for less inclined showers. The simulation work of Acharya et al (1979) on the size-age dependence of E.A.S is also shown in the figure where a greater average age parameter for primary iron showers than primary proton showers is found. For comparison they presented their experimental results for small showers ($(1-4)10^4$ particles) at an atmospheric depth of 920 grms/cm² which are consistent with primary protons.

Experimentally it is of interest to note that while most of the measurements do not give any size age dependence (Greisen, 1960) there is some evidence which suggests that not only does the age parameter depend on shower size but also for higher shower size the average age parameter increases with shower size. The experimental points of Vernov et al (1970) at sea level and Miyake et al (1973) at mountain altitude,



Figure 4.13a : Examples of the lateral structure of typical E.A.S. events in the size range of 2.3.10⁵-5.10⁵ particles.



Figure 4.13b : Examples of the lateral structure of typical E.A.S. events in the size range of 5.10⁵- 5.10⁶ particles.



Figure 4.13c : Examples of the lateral structure of typical E.A.S. events in the size range of 5.10 6 - 5.10 7 particles.

present this dependence which is shown in Figure 4.14. It shows that the average age parameter at sea level and mountain altitude shows an increase at an equivalent primary energy of about 3.10¹⁶ eV. Miyake et al (1973) suggested that the increase of age in this energy region could be due to a change in the composition of the primary cosmic rays or in the properties of high energy nucleon-nucleon collisions. Since then efforts have been made to clarify the difference. One approach is the central density measurements which are sensitive to the mass composition of primary particles (Peters, 1961 ; Tramper et al, 1971 ; Samorski et al, 1979). This will be discussed in the next section.

A more detailed age parameter study is the work of Chudako et al, 1979, in which they studied the correlation of age parameter with core distance. In two core distance ranges of (1-15)m and (6-45)m for $N_e \ge 2.10^5$ particles on the average they found no significant increase of age with core distance, where the mean lateral distribution function is well approximated by a single N.K.G. function.

The present result of the shower size-age parameter dependence is shown in figure 4.15 and is for three ranges of shower size with means, $3.5.10^5$, $1.6.10^6$ and 8.10^6 particles. The average age parameter for the first two size ranges decrease from 1.17 to 1.15 as predicted by the cascade shower theory, since at the level of observation, the maximum development of a shower comes down with primary energy. In the third size range an increase of age parameter was observed which is in the same primary energy region as obtained by Vernov et al,(1970) and Miyake et al, (1973).











Figure 4.15b : Similar to Figure 4.15a except that the preliminary results obtained using the Japanese Akano EAS array (atmospheric depth 927 g cm⁻²) are also shown.

The dependence of age parameter on zenith angle was also considered by dividing the showers into two ranges of less and bigger than 22° for three ranges of shower size as shown in Figures 4.7, 4.9 and 4.12a. The result shows that the average age parameter is independent of Θ in the limit of statistical error. It is of interest to mention that at a different altitude and different range of shower size the consistency of zenith angle-age has also been observed. Aguirre et al (1973) at 5200 m.a.s.l, found no correlation for showers bigger than 3.10^7 particles in the zenith angle ranges of $0 < 20^{\circ}$, $20^{\circ} \le 0 \le 40^{\circ}$ and $40^{\circ} \le 0 \le 60^{\circ}$.

4.3.2 The ^Ac/N Measurements

Measurements concerning central density to get information about the chemical composition of cosmic rays started after Peters (1961) proposed the possibility of a greater number of heavy primaries at an energy $> 3.10^{15}$ eV. The Sydney group (McCusker et al, 1968, 1969) measured the $\frac{1}{N}$ distribution ($^{\Delta}$ central density, N shower size) and compared it with the result of Monte Carlo calculations which indicated the primary cosmic ray beam has a mixed chemical composition at around 10¹⁵ eV which becomes richer in heavy nuclei above 3.10^{15} eV up to 10^{17} eV. However, the Sydney result was not confirmed by other measurements (Trumper, 1969) in the same energy region. The Keil group (Trumper et al, 1971) using $_{
m e}$ 32 m 2 hedoscope, have also performed the same comparison of the $\Delta c/N$ distribution. They concluded that the chemical composition at corresponding energies can not be much different from a pure proton or mixed composition. More recent work of the Kiel yroup (Samorski et al, 1979) on the central electron

densities also shows a significant proportion of protons for the primaries in the shower size range of $2.10^5 \le N \le 2.10^6$ particles. In the present work to obtain the central density. N.K.G functions (Equation 4.7) were used, where the number of particles in an area of $F = 0.215 \text{ m}^2$ centred on the core was defined as the central particle number n_c. Values of n_c corresponding to different age parameter were calculated and the results are shown in Table 4.3 which, for any shower of size Ne, makes it possible to calculate its central density when its age parameter is known. The integral distribution of the normalized central density $\Delta_{c} = \left(\frac{n_{c}}{E} - \frac{10^{5}}{N_{B}}\right)$ was found from the measured age parameter of individual showers and the result obtained is shown in Figure 4.15 for all Θ and Figure 4.17 for $0 < 22^{\circ}$. This was done for the size range of previous work (Samorski et al, 1971) 3.10⁵- 10⁶ pts as well as for the three ranges of shower size chosen for the present study, and particularly the higher size range of 5.10^6 -5.10⁷ pts which the increase of average S have been observed. The calculated distribution of the central density for a pure primary composition A = 1 (proton) and A = 56 (iron) is given by the Sydney group (McCusker et al, 1968, 1969) and the Kiel group (Thielheim and Beiersdorf, 1970; Samorski et al, 1971) which are also shown in the figure. Figures 4.16 and 4.17 show the present results which give a broader distribution of central density than previous work. The flattening can be understood from the recent measurements of central density by the Kiel group (Samorski et al, 1979) where a very large neon hodoscope was used to measure the electron density from 10 up to 0.1 metre to the core centre. They found that the distri-

1.8	3.105	
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9.1	1.5.10	re regio
1.5	3.1.10 ⁴	ntral co
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1.3	1.2.10 ³	number i nd age p
1.2	2.4.10 ³	lectron h size a
1.1	4.4.10 ³	is the e .5 m ² wit
г	8.2.10 ³	here n _c irea 0.21
6.0	1.4.10 ²	c,S)dr v
8. O	2.4.10 ²	;,16 ¹ 2тг F(r
0.7	4.2.102	
0.6	7.10 ²	
S, Age Parameter	р сур ц	TABLE 4.3 : n e



Figure 4.16 :

Comparison of the distribution of the normalized cantral density $\Delta_c = \left(\frac{n_c}{F}, \frac{10^5}{Ne}\right)$ for different ranges of shower size and the expected distributions assuming pure protons and pure iron (Samorski et al, 1971). n_c is the number of charged particles observed in an area of $F = 0.215 \text{ m}^2$ around the centre of the shower core. Previous measurements of the Kiel group are also shown.



Figure 4.17 :

Comparison of the distribution of the normalized central density $\Delta_{c} = \left(\frac{n_{c}}{F} - \frac{10^{5}}{Ne}\right)$ for different ranges of shower size and the expected distributions assuming pure protons and pure iron. Present work is for $\theta < 22^{0}$.

bution of E.A.S electrons becomes on average progressively flatter than an N.K.G. function when approaching the shower core centre (see Figure 4.18). Therefore, determining the central density using N.K.G functions (i.e. age parameter) gives a greater percentage of young showers or on the otherhand a bigger percentage of higher central density than previous work which implies the flatter observed distributions. The interesting feature of the present results is its size dependence. For the size range of $5.10^6 - 5.10^7$ particles, the central density distribution is relatively flatter than the other size ranges (see Figure 4.17). Therefore, knowing that lower central density is produced by a shower of large S (flat shower) the results indicate a bigger percentage of flat showers in the higher energy range..

4.4 CONCLUSION

For a given shower size at sea level both the mean age parameter and the standard deviation of the age parameter distribution are independent of zenith angle. The result obtained for the mean age parameter \overline{S} is consistent with previous work, but the standard deviation is larger than the result quoted by Wdowczyk (1973), $\frac{\overline{S}S}{S} = 0.09$. In the next stage of analysis, an age parameter-shower size dependence was found, particularly the surprising change and increase of age parameter at large size is noticed, which is in the same primary energy region as previous work, (Vernov et al, (1970) and Miyake et al, (1973)). The increase indicates that the position of the maximum development of E.A.S does not move down in the atmosphere as the primary energy increases as is expected from cascade shower theory assuming the chemical



Figure 4.18: The lateral distribution of electrons for core distance range of $0.1 \le r \le 10$ metre, (after Samorski, 1979). composition of the primaries does not change throughout the energy range studied. Since heavy primaries are expected to produce a greater average age parameter than primary protons, it is possible that the chemical composition of the primary radiation changes at a primary energy of $\sim 5.10^{16}$ eV such that the primary radiation contains a greater percentage of heavy nuclei. However, as measurements of the primary energy spectrum show no significant change in slope in this energy range, it is thought that a more likely explanation is a change in the characteristics of the nucleon-nucleon interaction at an energy of $\sim 5.10^{16}$ eV.

CHAPTER 5

SIZE SPECTRUM OF E.A.S. AT SEA LEVEL TAKING INTO ACCOUNT THE AGE PARAMETER OF THE SHOWER

5.1 INTHODUCTION

The interest in investigating the size spectrum is the information it contains about the energy spectrum of the primary high energy cosmic rays, while a comparison of spectra measured at different altitudes above sea level with other information on E.A.S. may also produce a picture of their evolution in the atmosphere.

The method used to obtain the size spectrum of vertical showers is by using the measured size distribution of the showers at different ranges of zenith angle taking the zenith-angle dependence of the showers as

$$I(0) = I(o)\cos\theta \tag{5.1}$$

The size distribution and the electron lateral distribution are closely connected.

The determination of the size and collecting area of a shower is dependent on the structure function, and the precise location of the core. Too steep a structure function causes an overestimation in the size of the shower and an underestimation in the collecting area of the shower. Many electron lateral distribution functions for different types of detector have been used. The most popular form that fits the experimental data is defined by Nishimura-Kamata-Greisen (N.K.G) which is dependent on s, the age parameter of the shower. The function is

$$\triangle (N,s,r) = C(s) \frac{N}{r_1^2} (1 + \frac{r}{r_1})^{s-4.5} (\frac{r}{r_1})^{s-2} (1 + \frac{r}{11.4 r_1})$$
(5.2)

where r₁ is the Moliere unit, 79 m at sea level (see Chapter 4). Although the measurement of the size spectrum is commonly obtained by assuming the same electron lateral structure function for all the showers (e.g. Catz et al, 1975, Ashton et al, 1979a, Crouch et al, 1980), to determine the size spectrum accurately, the age parameter of individual showers should be taken into account in order to get an accurate determination of size and collecting area.

Only Vernov et al, 1968, have carried out the latter approach and concluded that the spectrum had the same shape but lower intensity by an average factor of 0.77 than the spectrum determined using an average electron lateral structure function. The present experiment is a check and continuation of this work.

5.2 PREVIOUS MEASUREMENTS OF THE NUMBER SPECTRUM

The two ways that have been used to determine the number or size spectrum of E.A.S. are (a) the more reliable one which is derived from measuring the frequency, size and angular distribution of showers (direct method), (b) from density spectrum measurements (indirect method). The determination of the density spectrum is the frequency of showers, $P(\Delta) d\Delta$ which give densities within the range Δ to $\Delta + d\Delta$ particles per unit area at a particular point and is known to have the form $H(>\Delta) = K \Delta^{-\beta}$. In both cases, apart from

knowing the location of the shower axis and its arrival direction, the electron structure function and its size dependence is necessary.

Over many years, the number spectrum has been measured by many workers with different types of detector. Hillas (1970) calculated the best estimate number spectrum from the available data of all reliable experiments. His summary of the number spectrum at sea level is formulated as follows :

 $R(\ge N) = 52 \ N^{-1.5} \ m^{-2} \ s^{-1} \ st^{-1} \ for \ N \le 5.10^{5}$ $R(\ge N) = 36920 \ N^{-2} \ m^{-2} \ s^{-1} \ st^{-1} \ for \ 5.10^{5} \ N \ \le 3.10^{7}$ $R(\ge N) = 6.76 \ N^{-1.5} \ m^{-2} \ s^{-1} \ st^{-1} \ for \ N \ge 3.10^{7}$

where $R(\ge N)$ is the integral rate of showers of size more than N particles. It is plotted in Figure 5.22 (Curve a). Some more recent experiments are summarised by the Australian group, Crouch et al (1980), see Figure 5.23. The size spectrum is characterised as ;

(i) having a sharp break or "knee" around size 5.10^5 particles at sea level and 2.10^6 particles at mountain altitude. (ii) an increase of the exponent of the slope above the "knee". A determination of the size spectrum from the measured density spectrum has been described by Parvaresh (1975). The experiment consisted of a proportional counter and three large area liquid scintillators. The former was employed to measure the density spectrum of E.A.S, and the latter to select E.A.S. The number spectrum was derived from the density spectrum measured over the density range of 40 m⁻² < Δ < 5000 m⁻², where the kink was at $\Delta \sim 1000$ m⁻². The best estimation of the

- 41 -

integral number spectrum at sea level was derived as,

$R(>N) = 3. N^{-1.3}$	m ⁻² s ⁻¹ st ⁻¹	N ≤7.10 ⁵
$R(>N) = 36920 N^{-2}$	m ⁻² s ⁻¹ st ⁻¹	7.10 ⁵ & N < 3.10 ⁷
$R(>N) = 6.76 N^{-1.5}$	$m^{-2} s^{-1} st^{-1}$	N> 3.10 ⁷

The spectrum has approximately the same form as that given by Hillas except for $N_p < 7.10^5$ where a smaller rate is predicted (Figure 5.22 (Curve b)). In spite of a suggestion of slope flattening of the integral number spectrum for $N_p \ge 10^7$ by Khristiansen et al (1974), it has not been clearly investigated. A change in the slope of the density or number spectrum reflects a sharper change in the form of the primary energy spectrum, that is in the energy interval $E \sim 10^{15}$ -10¹⁶ eV. Around the break the exponent of the slope changes from -1.7 to -2.3, two possible interpretations of the sharp break in the energy spectrum may be (a) the break of energy spectrum of primary cosmic rays itself (a genuine change) or (b) a sudden change of nature of nuclear interaction at an energy around 5.10¹⁵ eV. Generally, the form of the primary energy spectrum is of particular interest from the point of view of the theory of the origin of the cosmic radiation.

5.3 PRESENT EXPERIMENT

5.3.1 The Trigger Modes of the E.A.S.Array

The Durham E.A.S. array consists of 14 plastic scintillators, and E.A.S. are recorded by two types of selection system each triggered by C, the Central detector, and either detectors 11, 31, 51 that are close to the centre

- 42 -

of the array (inner ring) or 13, 33, 53 the outer ring detectors. The triggering condition of the array is satisfied by a density of \geq 4 particles per m² at C and \geq 2 particles per m² at the other three mentioned detectors. On changing the trigger mode from the inner ring to the outer ring the detection sensitivity of the array changes from a small to a larger shower size range. Overall it is from size 2.10⁴ to 3.10⁷ particles (present experiment).

n, the power of the assumed zenith angle distribution of the shower (Eqn. 5.1) has been calculated to be $n = 8.0 \pm 0.3$ and $n = 8.5 \pm 0.2$ for the inner and outer ring trigger modes respectively was shown in Figure 5.4.

5.3.2 The Collecting Area of E.A.S. and the Shower Age

Une of the important parameters required to determine the size spectrum is the collecting area of showers of a given size. This is the area within which the shower axes have to fall to be detected. The requirement for detecting an E.A.S. is that the density of particles in the selection detectors should exceed the respective triggering levels. Since the density is given by $\Delta = N F(r, s)$, the maximum allowed distance of the axis from a given trigger detector is a function of N, Δ and s. Hence the collecting area depends on s, as $\pi r^2(N,s)$ for a given triggering detector. In the present work the collecting areas have been calculated for three equi-number groups of showers having age parameter ranges of 0.6< s<1.1, 1.1<s<1.3, 1.3<s<1.8 with means 0.95, 1.2 and 1.45. The result is shown for the three zenith angle ranges of $0-10^{\circ}$, $10-20^{\circ}$, $20-30^{\circ}$ with means 5°, 15° and 25° respectively, in Figures 5.16 to 5.18 for both the inner and outer ring triggers.

- 43 -

The dependence of age on collecting area can be explained with the help of Figure 4.3. It shows that the density at small core distances (r< 20m) in a shower of small age is larger than for showers with a bigger value of s, whereas at larger core distances the reverse is true. This is reflected in the variation of the collecting area of the shower with the age parameter. For fixed large shower sizes the collecting area of the shower increases with its age, as shown in Figure 5.13. However, for smaller shower sizes concerning smaller core distances this may not be the case. The example in Figure 5.14 shows that as the age parameter of E.A.S. increases, the collecting areas for a fixed size first increases and then decreases as s increases. The variation of collecting area with size for the three mean age parameter ranges of 0.95, 1.2 and 1.45 are shown in Figure 5.15 where showers were assumed to be vertical.

5.3.3 Effect of Zenith Angle on Collecting Area

Each scintillator in the array is calibrated by determining the average pulse height $m{v}$ produced by relativistic muons traversing it at normal incidence. If a pulse height V is produced by a shower of particles traversing a scintillator of area s at normal incidence, the particle density Δ is given by

$$\Delta = \frac{V}{vs} m^{-2}$$
 (5.3)

Consider the same particle density traversing the scintillator at zenith angle 0. The actual number of particles that traverse the scintillator is A.s cos0 but each particle will produce a larger pulse height v/cos0 because of its longer

- 44 -

track length in the phospor. The pulse height produced is thus, $\Delta \cdot s \cos \Theta \cdot \frac{v}{\cos \Theta} = \Delta \cdot sv = V$ from Equation 5.3. Thus if a pulse height V is observed from any detector and v is the average pulse height produced by normally incident muons, the particle density at the detector is correctly given by $\frac{V}{v}$ for any incident zenith angle.

Consider a detector of area s situated at 0 as shown in Figure 5.1a and initially assume showers can only fall anywhere along the line 0X. If an electronic requirement of >n particles m^{-2} is required for triggering then vertical showers of size N will only trigger the detector if they fall at distance $\leq r$ from 0 in the direction of 0X where r is found from solving the equation N F(r) = n, where F(r) is the electron lateral distribution function. For showers of size N incident at A at zenith angle 0 their orthogonal core distance from 0 is not r but the smaller value r cos 0. only at the larger distance r/cos 0 from 0 is their orthogonal core distance from 0 equal to r as illustrated in figure 5.1b. Thus the maximum distance from 0 along the line 0X at which showers of size N can trigger the detector at 0 increases as their zenith angle increases.

In the case of three triggering detectors situated in a plane, they will be simultaneously triggered by a shower of size N, only if it falls in an area (collecting area) which is approximately given by ;

 $A \simeq \pi (r-d)^2 \quad \text{for vertical showers} \quad (5.4a)$ $B \simeq \pi (r/\cos 0 - d)^2 \quad \text{for inclined showers} \quad (5.4b)$ d is the distance of an outer detector from C (assumed to be The same for all three triggering detectors) and r is the maximum core distance that a shower of size N incident vertically can fall from a triggering detector to satisfy the electron density triggering requirement (see Figure 5.2). Taking the present outer ring trigger detectors with $d\sim 58m$ and various collecting areas, say A = 1, 10^2 and 10^3 m² (corresponding to three increasing shower sizes each incident vertically) r is found by solving equation (5.2a) to be r = 58.56, 63.6 and 75.8m for each collecting area. To see the effect of zenith angle $_{\Theta}$ on collecting area we consider showers of the same size (i.e. they have collecting areas 1 1, 10^2 and 10^3 m² when incident vertically) but with zenith angle 0. The maximum distance that their cores can fall in the horizontal plane to satisfy the selection criteria is increased from r to $r_1 = r/\cos\theta$, for $\theta = 15^{0}$, $r_1 = r/\cos\theta$ 1.035 r or $r_1 = 60.62$, 65.42 and 78.47m which from equation (5.2b) gives collecting areas of 21.5, $1.72.10^2$ and $1.31.10^3$ m². This shows that the collecting area of showers with collecting areas 1, 10^2 and 10^3 m² when incident vertically increases by factors of 21.5, 1.72 and 1.31 when incident with $\theta = 15^{\circ}$. It is seen that the importance of this effect is very large close to the triggering threshold but becomes less important as the collecting area (shower size) increases. The variation of collecting area with shower size for different zenith angles are shown in Figures 5.16 to 5.18 for the inner and outer ring triggers of the E.A.S. array.

5.3.4 Analysis of the Data

A total number of 4814 triggers in a running time of 511.27 hours were analysed and the shower information : shower size N_e, core distance r_c and zenith angle 0 and also age

- 46 -



Figure 5.1 : To be detected by a given local density detector situated at 0 the maximum distance from 0 along 0X at which showers of a given size can fall is r as shown in Fig.(5.1a) if the showers are incident vertically. For showers incident at zenith angle 0 the maximum distance is r/cos0 as shown in Fig.(5.1b).





Figure 5.2 : The dependence of collecting area on zenith angle for showers of a given size. A is the collecting area for a vertical shower and B is the collecting area for the same shower incident at zenith angle Θ .

parameter s and shower size $N_e(s)$ were obtained. N_p and $N_{\rm p}(s)$ are sizes obtained using the Catz and N.K.G. (i.e.age parameter) structure functions respectively. Figure 5.3 shows the minimum shower size that showers of given age must have to produce a trigger. It is seen that the minimum size of a shower to trigger the array is 7.10^4 and 2.10^5 particles for the inner and outer ring triggers respectively. Table 5.1 shows the basic data used in the determination of the size spectrum for both the inner and outer ring triggers used in the present work. In this table the quoted shower sizes are $N_{\alpha}(s)$. The observed and expected zenith angle distributions of recorded E.A.S. are shown in Figure 5.4, where the exponent n (see equation 5.1) for best to the data was calculated to be n = 8.0 + 0.3 and 8.5 ± 0.2 for the inner and outer ring triggers respectively. The age parameter and shower size distributions are given in Figures 5.5 to 5.7. A comparison of N_D with N_D(s) for showers with $0 < 30^{\circ}$ are given in Figures 5.8 to 5.10 where the average percentage difference $\frac{N_{e}(s) - N_{e}}{N_{e}(s)} = is + (36.1 \pm 1.8)\% \text{ for } 10^{4} < N_{e} < 4.10^{4} - (0.6 \pm 1.0)\%$ for $4.10^6 < N_e(s) < 10^6$ and $+(15.1 \pm 6.7)\%$ for $N_{e(s)} > 4.10^6$ particles. Overall. it is seen that for very small and large shower sizes there is a significant difference between the correct size $N_{\rm p}(s)$ and the value obtained if a unique electron structure function is assumed for all showers. The distribution of orthogonal core distance from the central detector C is given with a comparison with (X,Y) plane core distances in Figures 5.11 and 5.12. For showers with $0 < 30^{\circ}$ the average $\frac{r_{xy} - r_{orth}}{r_{yy}}$ is $(3.9 \pm 0.02)\%$. percentage difference

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$ \begin{array}{c c} E.A.S. \ Selection \\ Inter ring \ Trigger \ int \ $							
Inner ring Trigger ; $\Delta_{c}^{(\geq 4m^{-2})}$ $\Delta_{l1}^{(\geq 2\overline{m}^{2})}, \Delta_{31}^{(\geq 2\overline{m}^{2})}, \Delta_{51}^{(\geq 2\overline{m}^{2})}$ $\Delta_{l1}^{(\geq 2\overline{m}^{2})}, \Delta_{31}^{(\geq 2\overline{m}^{2})}, \Delta_{51}^{(\geq 2\overline{m}^{2})}$ Outer ring Trigger; $\Delta_{c}^{(\geq 4\overline{m}^{2})}$ $\Delta_{13}^{(\geq 2\overline{m}^{2})}, \Delta_{33}^{(\geq 2\overline{m}^{2})}, \Delta_{53}^{(\geq 2\overline{m}^{2})}$ $\Delta_{13}^{(\geq 2\overline{m}^{2})}, \Delta_{33}^{(\geq 2\overline{m}^{2})}, \Delta_{53}^{(\geq 2\overline{m}^{2})}$	E.A.S. Selection	Run time (hrs)	Total No. of Triggers	Trigger rate (hr ⁻¹)	Total No.of Analyzable Showers	No. of Triggers with 0<30 ⁰ ,r _c <75m N<4.10 ⁶	No. of Triggers with 0<30 ⁰ ,r _c <105 N<4.10 ⁶
Outer ring Trigger; Δ _c (≥4π ²) a83.27 2131 5.56 ± 0.12 2042 1 Δ ₁₃ (≥2π ²),Δ ₃₃ (≥2π ²),Δ ₅₃ (≥2π ²)	ner ring Trigger ;∆ _c (≥4m ⁻²) (≥2m ²),∆ ₃₁ (≥2m ²),∆ ₅₁ (≥2m ²)	128	2683	20.96 <u>+</u> 0.40	2608	1802	б
	ter ring Trigger; ∆ _c (≥4m ⁻²) ;(≥2m ²),∆ ₃₃ (≥2m ²),∆ ₅₃ (≥2m ²)	383.27	2131	5.56 ± 0.12	2042	1149	33

TABLE 5.1 : Summary of experimental data used in the analysis.



Figure 5.3: The dependence of minimum shower size on the shower age parameter for showers to satisfy the inner ring trigger and the outer ring trigger of the Durham E.A.S. array, Values calculated assuming all showers obey the Greisen average electron structure function are indicated by the solid circles.





to the data according to $I(\Theta) = I(o) \cos^{n} \Theta$.







Figure 5.6 : The size distributions of all showers and those with $\Theta < 30^{\circ}$ used in the data analysis.


Figure 5.7 : The size distributions of all showers and those with $0 < 30^{\circ}$ used in the data analysis.



<u>Figure 5.8</u>: A comparison of the measured distributions of shower size N_e and N_e (s) for showers with zenith angles of less than 30° used in the determination of the size spectrum. Two events (not plotted in the histogram) have $N_e(s) = 7.10^3$ and 9.10^3 particles.



Figure 5.9 : The fractional difference between the correct shower size, $N_e(s)$ taking the age parameter of individual showers into account and the shower size N_e determined assuming all showers obey the Catz average electron structure function for showers in different size ranges.



Figure 5.10: The fractional difference between $N_e(s)$ and N_e for showers in the size range of less than 10^6 particles.



Figure 5.11: A comparison between orthogonal and (x, y) plane core distances from the central

detector C.



Figure 5.12: The fractional difference between the orthogonal and (x,y) plane core distances from the central detector C for all the showers and those with zenith angle less than 30° .

In determining the size spectrum the dependence of collecting area on shower age is of importance. For showers with zenith angle less than 30°, the data was grouped into approximately three equinumber ranges of age parameter with mean ages of s = 0.95, 1.2 and 1.45, where each age range was subgrouped into three zenith angle ranges of $0-10^{\circ}$. $10-20^{\circ}$ and $20-30^{\circ}$ with mean zenith angles 5°, 15°, 25°. An example of collecting areas for vertical showers with different values of age are shown in Figures 5.13 and 5.14. The dependence of collecting area on shower size for vertically incident showers with different age parameter is shown in Figure 5.15 for the inner and outer ring triggers. The dependence on zenith angle Θ is shown in Figures 5.16 to 5.18. Figure 5.19 shows that for vertical showers, on average, variation of collecting area with size does not depend strongly on the assumed electron lateral structure function. The structure functions considered are the structure function relevant to the age parameter of individual showers, the Catz and the Greisen structure function.

To obtain the vertical differential size spectrum R(N,0) from the experimental data it was assumed that the differential size spectrum at zenith angle $_{\Theta}$ is given by ;

$$R(N,\Theta) = R(N,O) \cos^{n}\Theta m^{-2} s^{-1} st^{-1}/unit N$$

The number of showers X of size N/unit N traversing a collectting area $A(\Theta)$ in the horizontal plane in time t that have

- 48 -



An example of the variation of acceptance area of showers with size 3.10⁵ particles for different values of the shower age parameter. Figure 5.13 :

4



Ne=2.10⁵ particles Vertical shower

33



53 іа. 3

Figure 5.14 : An example of the variation of acceptance area of showers with size 2.10⁵ particles for different values of the shower age parameter.

13



Figure 5.15 : Dependence of collecting area on shower size for vertically incident showers with different age parameter for the inner and outer ring triggers. The curve for showers which obey the Greisen average electron structure function has s = 1.25 and is close to the curve labelled s = 1.20 in the figure.



Figure 5.16 : The dependence of collecting area on shower size for showers with age parameter s = 0.95and different values of zenith angle.



Figure 5.17 : The dependence of collecting area on shower size
 for showers with age parameter s = 1.2 and
 different values of zenith angle.



re 5.18 : The dependence of collecting area on shower size for showers with age parameter s = 1.45 and different values of zenith angle.



Figure 5.19 : Collecting area-shower size dependence for vertically incident showers with different average electron lateral structure functions.

zenith angle 0 is given by

$$X = \int_{0}^{0} R(N, 0) \cdot R(0) \cos \theta + 2 \pi \sin \theta d\theta$$

from which
$$R(N,0) = \frac{\chi}{t.2\pi \int_{0}^{\Theta} A(\Theta) \cos^{n+1}\Theta \sin\Theta d\Theta}$$
 (5.5)

Using the shower size and age dependence of $A(\Theta)$ obtained from the curves of Figures 5.16 to 5.18 and using n = 8.0 and 8.5 for the inner and outer ring triggers, equation 5.5 was evaluated for showers in the three stated age parameter ranges. Adding the three resulting rates together gives the total differential rates of showers of N/unit N incident vertically at sea level. This was done when $N_e(s)$ and N_e were used for showers with zenith angle less than 30° . For near vertical showers, when $A(\Theta) = A = a$ constant, equation 5.5 becomes

$$R(N,0) = \frac{X}{t + 2\pi \cdot A} \left\{ \frac{1 - \cos^{n+2} \theta}{n + 2} \right\}$$

5.3.5 The Results and Conclusion

The size spectrum determined assuming all showers obey the same Catz electron structure function and using the resulting N_e sizes is given in Table 5.2a. To be more precise, in determining the size spectrum, the age parameter of the individual showers has been taken into account and the resulting size spectrum using N_e(s) for three stated ranges of age parameter has been found. The result for each range of age and the total result as a final size spectrum are

- 49 -

given in Tables 5.2b to 5.2f. The results are plotted in Figures 5.20 and 5.21 where the work of Hillas (1970), Curve a and Parvaresh (1975), Curve b, are also plotted for comparison. From these figures it is seen that apart from very small and large sizes the size spectrum obtained using $N_{s}(s)$ is consistent with the previous work of Parvaresh and also with the spectra obtained using N.. The result for the integral size spectrum is shown in Figures 5.22 and 5.23 where it is compared with some recent measurements (Catz et al. 1975. Ashton et al, 1979a, Crouch et al, 1980). The significant rate difference at small sizes (<4.10⁴) shown in Figure 5.22, is due to a loss of showers with large age parameter since the minimum size of a shower of all ages to trigger the inner ring trigger is > 7.10⁴ particles (see Figure 5.3). The difference at large sizes > 10^7 particles is due to an increase of age parameter with shower size which results in a larger average size when individual shower ages are taken into account than when an average electron structure function is assumed.

- 50 -

tz average electron	obey the Ca	l showers	uming al) <30 ⁰ assi	howers with (trum of s tion.	size spec ture func	erential ral struc	: Diff. late:	TABLE 5.2a
					2968	1186	1782			
(1.06 <u>+</u> 0.27)10 ⁻¹⁶	9.92.10 ¹⁷	1.25.10 ¹⁶	3.46.10	3.46.10	15	1	4	1.1.10	<105m	,01 (2- <i>1</i> .0)
(5.16 <u>+</u> 0.95) 10 ⁻¹⁶	4.68.1 0 ¹⁶	9.39.10 ¹⁶	3.46.10	3.46.10	29	26	m	5.5.10	<105m	(4-7) 10 ⁰
$(1.54 \pm 0.44) 10^{-15}$	1.7.10 ⁻¹⁵	1.06.10 ¹⁵	1.76.10	1.76.10	12	6	m	3.5.10	<75m	(3-4) 10
(3.58 <u>+</u> 0.65) 10 ⁻¹⁵	2.6.10 ⁻¹⁵	4.7.10 ⁻¹⁵	1.76.10	1.76.10	30	16	14	2.5.10		(2-3) 10 ⁰
$(1.96 \pm 0.14) 10^{-14}$	2.06.10 ¹⁴	1.69.10 ¹⁴	1.76.10	1.76.10	182	134	48	1.5.10		(1-2) 10 ⁶
	5.3.10 ⁻¹⁴	6.11.10 ¹⁴	1.76.10	1.76.10 ⁴	53	35	18	9.5.10 ⁵		(9-10) 10 ₂
(6 8 ± 0 5010-14	7.5.10 ⁻¹⁴	9.06.10 ¹⁴	1.7.10 ⁴	1.76.10	77	20	27	8.5.10 ⁵		(8-9) 10 ⁵
	7.1.10 ⁻¹⁴	9.9.10 ⁻¹⁴	1.45.104	1.76.104	74	46	28	7.5.105		(7-8) 10 ⁵
14 01 12 01 12 01	1.15.10 ¹³	1.21.10 ¹³	1.17.104	1.76.10 ⁴	111	75	36	6.5.10 ⁵		(6–7) 10 ⁵
(1.58 + 0.13) 10 ⁻¹³	1.65.10 ¹³	1.42.10 ¹³	9.1.10 ³	1.76.104	149	107	42	5.5.10 ⁵		(2-6) 10 ⁵
(3.98 <u>+</u> 0.26) 10 ⁻¹³	4.7.10 ¹³	2.50.10 ¹³	6.6.10 ³	1.65.104	233	158	74	4.5.10 ⁵	-	(4-5) 10 ⁵
(6.20 ± 0.36) 10 ¹³	7.10 ¹³	5.10 ⁻¹³	4.3.10 ³	1.3.10 ⁴	294	176	118	3.5.10 ⁵		(3-4)10 ⁵
(1.56 ± 0.08) 10 ¹²	1.43.10 ¹²	1.67.10 ¹²	2.2.10 ³	7.6.10 ³	413	175	237	2.5.10 ⁵		(2-3):10 ⁵
(5.16 ± 0.22)10 ¹²	4.4.10 ¹²	5.48.10 ¹²	5.4.10 ²	3.9.10 ³	576	168	408	1.5.10 ⁵		(1-2) 10 ⁵
0T (/T 0 - 50.7)		1.75.10 ¹¹		1.95.10 ³	65		65	9.5.104		(9-10) 10 ⁴
		2.31.10 ¹¹		1.6.10 ³	77		77	8.5.10 ⁴		(8-9).10 ⁴
(2.83 <u>+</u> 0.31) 10 ⁻¹¹		2.83.10 ¹¹		1.3.10 ³	81		81	7.5.10 ⁴		(7-8) 10 ⁴
or (ac.) - (a. ;)		4.24.10 ¹¹		1.02.10 ³	94		94	6.5.10 ⁴		(6-7)10 ⁴
		5.47.10 ¹¹		7.10 ²	84		84	5.5.104		(5-6) 10 ⁴
-		1.07.10 ¹⁰		3.8.10 ²	97		67	4.5.10 ⁴		(4-5) 10 ⁴
$(3.45 + 0.19) I \overline{0}^{10}$		2.73.10 ¹⁰		2.10 ²	131		131	3.5.10 ⁴		(3-4)10 ⁴
_		6.56.10 ¹⁰		4.4.10 ¹	92		92	2.5.10 ⁴	<75m	(2-3) 10 ⁴
	ring	ring	ring	ring	triggers	ring	ring	12	range distb Core	Range
ring triggers	Outer	Inner N	Outer	Inner	outer ring	Outer	Inner		a but	ž

				N.1	K.G. No	. of Sh	owers i	n S Rano	ge	
Size Bange	distance ange	Ň	Catz No.of	0.6<5<	1.1	1.1<5	<1.3	1.3<5<	1.8	Inner & Outer
	r Core Core		with Θ <30	Inner ring	Outer ring	Inner ring	Outer ring	Inner ring	Outer ring	for all S
(2-3)104		2.5.104	92	25		9		1		35
(3-4)104	<75	3.5.104	131	36		14		4		54
(4-5)104	ĺ	4.5.104	97	38		23		17		78
(5-6)104		5.5.104	84	39		24		1.8		81
(6-7)104		6.5.10 ⁴	94	50		23		23		96
(7-8)104		7.5.104	81	41		18		19		78
(8-9)104		8.5.104	77	38		27		26		91
(9-10) 104		9.5.104	65	34		29		13		76
(1-2)105		1.5.10	576	185	54	155	73	168	36	671
$(2-3)10^{5}$		2.5.10	413	97	50	88	85	94	44	458
(3-4)10 ⁵		3.5.10	294	46	38	33	80	30	45	272
(4-5)105		4.5.10	233	33	33	35	78	27	37	243
(5-6)10 ⁵		5.5.105	149	20	29	23	53	11	30	166
(6-7)10 ⁵		6.5.10	111	12	20	17	33	8	27	117
(7-8)105		7.5.105	74	9	13	11	31	6	17	87
(8-9)105		8.5.105	77	9	8	11	22	9	8	67
(9-10)105		9.5.105	53	4	7	8	20	2	9	50
(1-2)106		1.5.10	182	12	39	23	58	13	39	184
(2-3)10 ⁶		2.5.10	30	2	9	3	9	6	6	35
(3-4) 10 ⁶	<75	3.5.10	12 ·	o	4	2	3	1	2	12
(4-7)10 ⁶	<105	5.8.10	29	2	6	1	5	1	8	23
(0.7-2)10	<105	1.01.10	15	1	4	1	2	3	8	19
										2993

TABLE 5.2b : The number of showers in different ranges of shower size assuming

(2) taking the age parameter of individual showers into account.

⁽¹⁾ all showers obey the Catz electron structure function and

kange	core dista apnar		Inner ring	Outer ring	Total	Inner ring	Outer ring	Inner ring	Outer ring	outer 1109 triggers m ⁻² sec ⁻¹ st ⁻¹ unit N ⁻¹
2-3) 10 ⁴		2.5.104	25		25	2.2.10 ²		4.4.10 ⁻¹¹		(4.4 + 0.88) 10 ⁻¹¹
3-4) 10 ⁴	< 75	3.5.104	36		36	5.4.10 ²		2.92.10 ¹¹		$(2.92 \pm 0.48) 10^{-111}$
4-5) 10 ⁴		4.5.10 ⁴	38		38	8.9.10 ²		2.02.10 ¹¹		$(2.02 \pm 0.32) 10^{-11}$
5-6) 10 ⁴		5.5.104	39		39	1.27.10 ³		1.62.10 ⁻¹¹		(1.62 + 0.26) 10 ⁻¹¹
6-7) 10 ⁴		6.5.10 ⁴	20		ß	1.65.10 ³		1.62.10 ⁻¹¹		$(1.63 \pm 0.23) 10^{-11}$
7-8) 10 ⁴		7.5.104	41		41	2.07.10 ³		9.4.10 ⁻¹²		$(9.40 \pm 1.46) 10^{-12}$
8-9) 10 ⁴		8.5.104	38		38	2.45.10 ³		8.12.10 ⁻¹²		$(8.12 \pm 1.31) 10^{-12}$
9-10) 10 ⁴		9.5.104	34		34	2.85.10 ³		6.39.10		$(6.39 + 1.09) 10^{-12}$
1-2) 10 ⁵		1.5.105	185	54	239	5.10 ³	8.10 ¹	2.04.10 ⁻¹²	7.10 ⁻¹²	$(3.1 \pm 0.2) 10^{-12}$
2-3) 10 ⁵		2.5.10 ⁵	97	ß	147	8.3.10 ³	IO3	6.13.10 ⁻¹³	9.6.10 ⁻¹³	(7.31 + 0.60) 10 ⁻¹³
3-4) IC ⁵		3.5.10	46	38	84	1.1.104	2.35.13	2.27.10 ⁻¹³	3.2.10 ⁻¹³	(2.69 ± 0.29) 10 ⁻¹³
4-5) 10 ⁵		4.5.10 ⁵	33	33	66	1.35.104	3.8.10 ³	1.38.10 ⁻¹³	1.92.10 ⁻¹³	(1.65 + 0.2) 10 ⁻¹³
5-6) 10 ⁵		5.5.10 ⁵	20	29	49	1.6.10 ⁴	5.4.10 ³	6.77.10 ⁻¹⁴	1.15.10 ⁻¹³	$(9.57 \pm 1.37) 10^{-14}$
6-7) 10 ⁵		6.5.10 ⁵	12	20	32	1.76.10 ⁴	7.103	4.53.10 ⁻¹⁴	5.98.10 ⁻¹⁴	$(5.43 \pm 0.96) \log^{-14}$
7-8) 10 ⁵		7.5.10 ⁵	6	13	22	1.76.10 ⁴	8.6.10 ³	3.20.10 ⁻¹⁴	3.11.10 ⁻¹⁴	$(3.14 \pm 0.67) 10^{-14}$
8-9) 10 ⁵		8.5.105	<u>б</u>	80	17	1.76.10 ⁴	1.05.10	⁴ 3.15.10 ⁻¹⁴	1.57.10 ⁻¹⁴	$(2.41 \pm 0.58) 10^{-14}$
9-10) 10 ⁵		9.5.10 ⁵	4	7	11	1.76.10 ⁴	1.25.10	⁴ 1.25.10 ⁻¹⁴	1.41.10 ⁻¹⁴	$(1.35 \pm 0.41) 10^{-14}$
1-2)106		1.5.106	12	39	51	1.76.10 ⁴	1.76.10	⁴ 4.14.10 ⁻¹⁵	5.7.10-15	$(5.33 \pm 0.74) 10^{-15}$
2-3) 10 ⁶		2.5.106	' 72	6	11	1.76.10 ⁴	1.76.10	⁴ 7.56.10 ⁻¹⁶	1.22.10 ⁻¹⁵	(1.13 + 0.34) 10 ⁻¹⁵
3-4) 10 ⁶	< 75	3.5.106	0	4	4	1.76.104	1.76.10	0	5.92.10 ⁻¹⁶	(5.92 + 2.96)10 ⁻¹⁶
4-7) 10 ⁶	<105	6.2.10 ⁶	2	9	8	1.76.10 ⁴	3.46.10	⁴ 10 ⁻¹⁶	1.22.10 ⁻¹⁶	(1.16 ± 0.41)10 ⁻¹⁶
0.7-2)10 ⁷	<105	1.1.10 ⁷	7	4	S	1.76,10 ⁴	3.46.10	¹ .75.10 ⁻¹⁷	2.9.10 ⁻¹⁷	$(2.67 \pm 1.19) 10^{-17}$
ABLE 5.2C	: Dif	ferential	size spe	sctrum of '	showers wi	th 0< 30° a	nd 0.6	<pre></pre>		

•

	.																							
m-2sec-1st-1 unit N ⁻¹	(4.36 + 1.45)10 ⁻¹¹	(2.32 + 0.62) 10 ⁻¹¹	(2.24 + 0.49) 10 ⁻¹¹	(1.34 + 0.27) 10 ⁻¹¹	$(9.8 \pm 2.04) 10^{-12}$	$(6.04 \pm 1.42) 10^{-12}$	$(6.91 \pm 1.32) 10^{-12}$	$(7.14 \pm 1.31) 10^{-12}$	$(1.84 + 0.12)10^{-12}$	$(6.1 \pm 0.47) 10^{-13}$	$(2.81 + 0.26)10^{-13}$	$(1.88 + 0.17) 10^{-13}$	$(1.02 + 0.12) 10^{-13}$	$(5.69 + 0.81) 10^{-14}$	$(4.57 + 0.71) 10^{-14}$	(3.35 + 0.58) 10 ⁻¹⁴	$(2.86 + 0.54) 10^{-14}$	(7.19 + 0.80) lo ⁻¹⁵	(1.21 + 0.35) lo ⁻¹⁵	$(5.21 \pm 2.32) 10^{-16}$	$(5.50 + 2.24) 10^{-17}$	(2.98 <u>+</u> 1.72) 10 ⁻¹⁷		
Outer ring									73.10 ⁻¹²	6.62.10 ⁻¹³	3.4.10 ⁻¹³	2.2.10 ⁻¹³	1.13.10 ¹³	5.82.10 ¹⁴	4.93.10 ¹⁴	3.32.10 ¹⁴	2.96.10 ¹⁴	7.05.10 ¹⁵	1.27.10 ¹⁵	4.56.10 ¹⁶	5.6.10 ⁻¹⁷	2.6.10 ⁻¹⁷		
Inner ring	4.36.10 ¹¹	2.32.10 ¹¹	2.24.10 ¹¹	1.34.10 ¹¹	9.8.10 ⁻¹²	6.04.10 ¹²	6.91.10 ¹²	7.14.10 ¹²	1.90.10 ¹²	5.6.10 ⁻¹³	1.38.10 ¹³	1.18.10 ¹³	7.8.10 ⁻¹⁴	5.44.10 ¹⁴	3.56.10 ¹⁴	3.43.10 ¹⁴	2.62.10 ¹⁴	7.57.10 ¹⁵	1.05.10 ¹⁵	6.2.10 ⁻¹⁶	5.10 ⁻¹⁷	3.75.10 ¹⁷	< S < 1.3	
Outer ring									5.4.10 ²	2.35.10 ³	4.6.10 ³	7.10 ³	9.7.10 ³	1.24.104	1.5.104	1.7.104	1.7.10 ⁴	1.7.104	1.7.10 ⁴	1.7.104	3.46.104	3.46.104	nd 1.1	
Inner ring	4.3.10 ¹	1.8.10 ²	3.8.10 ²	7.10 ²	1.02.10 ³	1.3.10 ³	1.6.10 ³	1.95.10 ³	3 9.10 ³	7.6.10 ³	1.3.104	1.65.104	1.76.10 ⁴	1.76.104	1.76.104	1.76.104	1.76.104	1.76.104	1.76.10 ⁴	1.76.104	3.46.10 ⁴	3.46.10 ⁴	0 < 30 ⁰ a	
Total ring	6	14	23	24	23	18	27	29	227	173	113	113	76	So	42	33	28	81	12	ŝ	9	m	owers with	
Outer ring			_						73	85	8	78	53	33	31	22	20	58	6	m	Ś	5	rum of sh	
Inner ring	6	14	23	24	23	18	27	29	154	88	33	35	23	17	#	11	8	23	m	2	н		size spect	
	2.5.10 ⁴	3.5.10 ⁴	4.5.104	5.5.104	6.5.10 ⁴	7.5.104	8.5.104	9.5.10 ⁴	1.5.105	2.5.10 ⁵	3.5.10 ⁵	4.5.10 ⁵	5.5.10 ⁵	6.5.10 ⁵	7.5.10 ⁵	8.5.10 ⁵	9.5.10 ⁵	1.5.106	2.5.106	3.5.10 ⁶	5.5.10 ⁶	8.5.106	erential	
cc dtat 52		< 75																		< 75	<105	<105	Diffe	
Range	(2-3) 10 ⁴	(3-4) 10 ⁴	(4-5) 10 ⁴	(5-6) 10 ⁴	(6-7) 10 ⁴	(7-8) 10 ⁴	(8-9) 10 ⁴	(9-10) 10 4	(1-2) 10 ⁵	(2-3) 10 ⁵	(3-4) 10 ⁵	(4-5) 10 ⁵	(5-6) 10 ⁵	(6-7) 10 ⁵	(7-8) 10 ⁵	(8–9) 10 ⁵	(9-10) 10 ⁵	(1-2) 10 ⁶	(2-3) 10 ⁶	(3-4) 10 ⁶	(4-7) 10 ⁶	(0.7-2) 10 ⁷	TABLE 5.2d :	



(1.86 ± 0.13) 10 ⁻¹³ (4.53 ± 0.15) 10 ⁻¹³ (1.31 ± 0.15) 10 ⁻¹³ (8.32 ± 1.04) 10 ⁻¹⁴ (8.32 ± 0.02) 10 ⁻¹⁴ (3.67 ± 0.62) 10 ⁻¹⁴ (2.36 ± 0.49) 10 ⁻¹⁴ (2.13 ± 0.52) 10 ⁻¹⁴ (1.11 ± 0.33) 10 ⁻¹⁴ (1.36 ± 0.39) 10 ⁻¹⁵ (1.36 ± 0.39) 10 ⁻¹⁵ (2.85 ± 1.64) 10 ⁻¹⁶	2.54.10 3.37.1513 1.48.10 ⁻¹³ 7.93.10 ¹⁴ 5.10 ⁻¹⁴ 3.95.10 ⁻¹⁴ 1.23.10 ⁻¹⁴ 1.23.10 ⁻¹⁴ 1.22.10 ⁻¹⁵ 8.63.10 ¹⁶ 8.63.10 ¹⁶	1.72.10 5.05.1013 1.06.1013 8.86.1014 8.86.1014 3.68.1014 1.87.1014 1.87.1015 6.24.1015 6.24.1015 4.18.1015 1.87.1015 1.87.1015 1.87.1015	2.4.10 ⁻ 2.15.10 ³ 6.25.10 ³ 10 ⁴ 1.75.10 ⁴ 1.75.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴	5.10 9.7.10 ³ 1.4.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴	204 138 25111233515457538 251112335154575		1 6 3 2 6 8 1 2 4 8 1 6 3 7 6 8 1 7 7 9 4 8	1.5.10 ⁵ 2.5.10 ⁵ 3.5.10 ⁵ 4.5.10 ⁵ 5.5.10 ⁵ 6.5.10 ⁵ 7.5.10 ⁵ 7.5.10 ⁵ 9.5.10 ⁶ 1.5.10 ⁶ 2.5.10 ⁶ 2.5.10 ⁶	< 75	(1-2) 10 ⁻ (2-3) 10 ⁵ (1-4) 10 ⁵ (4-5) 10 ⁵ (5-6) 10 ⁵ (7-8) 10 ⁵ (9-10) 10 ⁵ (1-2) 10 ⁶ (1-2) 10 ⁶ (2-3) 10 ⁶ (2-3) 10 ⁶
$(2.13 \pm 0.52) 10^{-14}$ $(1.11 \pm 0.3) 10^{-15}$ $(5.37 \pm 0.74) 10^{-15}$ $(1.36 \pm 0.39) 10^{-15}$ $(1.36 \pm 1.64) 10^{-16}$ $(1.4 \pm 0.4) 10^{-16}$ $(9.35 \pm 2.81) 10^{-1}$	1.23.10 1.22.10 ⁻¹⁴ 5.77.10 ⁻¹⁵ 8.63.10 ¹⁶ 2.72.10 ⁻¹⁶ 1.5.10 ¹⁶ 9.4.10 ⁻¹⁷	2.93.10 6.24.1015 4.18.1015 1.87.1015 1.87.1016 6.8.10 ⁻¹⁷ 6.8.10 ⁻¹⁷ 9.22.10 ¹⁷	1.76.10 1.76.10 1.76.10 1.76.10 1.76.10 3.46.10 3.46.10 and of 1	1.76.10 1.76.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴ 3.46.10 ⁴ 3.46.10 ⁴ 3.46.10 ⁴	17 11 52 12 3 3 11 11 showers with	ectru 0 f 0 f 0 f 0 f 0 f 0 f 0 f 0 f	9 132 132 15 15 15 15 15 15 15 15 15 15 15 15 15	8. 5.10 9.5.10 ⁵ 1.5.10 ⁶ 2.5.10 ⁶ 3.5.10 ⁶ 5.7.10 ⁶ 5.7.10 ⁷ 1.7.10 ⁷	 < 75 < 105 < 105 < 105 	(8-9)10 (9-10)10 ⁵ (1-2)10 ⁶ (2-3)10 ⁶ (3-4)10 ⁶ (4-7)10 ⁶ (0.7-2)10 ⁷ (0.7-2)10 ⁷
$(1.31 \pm 0.15) 10^{-13}$ $(8.32 \pm 1.04) 10^{-14}$ $(4.64 \pm 0.72) 10^{-14}$	1.48.10 ⁻¹³ 7.93.10 ¹⁴ 5.10 ⁻¹⁴	1.06.10 ¹³ 8.86.10 ¹⁴ 3.68.10 ¹⁴	6.25.10 ³ 10 ⁴ 1.41.10 ⁴	1.4.10 ⁴ 1.76.10 ⁴ 1.76.10 ⁴	75 64 41	45 37 30	, 30 27 11	3.5.10 ⁵ 4.5.10 ⁵ 5.5.10 ⁵		(3-4)10 ⁵ (4-5)10 ⁵ (5-6)10 ⁵
$(2.50 \pm 0.69) 10^{-12}$ $(1.86 \pm 0.13) 10^{-12}$ $(4.53 \pm 0.38) 10^{-13}$	2.54.10 ⁻¹² 3.37.1c ¹³	2.50.10 ¹² 1.72.10 ¹² 5.05.10 ¹³	2.4.10 ² 2.15.10 ³	2.4.10 ⁷ 5.10 ³ 9.7.10 ³	13 204 138	36	13 168 94	9.5.10 ⁵ 1.5.10 ⁵ 2.5.10 ⁵		(9-10) 10 ⁵ (1-2) 10 ⁵ (2-3) 10 ⁵
$(8.17 \pm 1.7)10^{-12}$ $(5.73 \pm 1.35)10^{-12}$ $(6.87 \pm 1.35)10^{-12}$		8.17.10 ¹² 5.73.10 ¹² 6.87.10 ¹²		10 ⁻ 1.4.10 ³ 1.8.10 ³	23 19 26		23 19 26	6.5.10 ⁴ 7.5.10 ⁴ 8.5.10 ⁴		(6-7) 10 ⁴ (7-8) 10 ⁴ (8-9) 10 ⁴
$(4.53 \pm 4.53) \text{ IO}^{-11}$ $(1.53 \pm 0.76) \text{ IO}^{-11}$ $(2.04 \pm 0.49) \text{ IO}^{-11}$ $(1.19 \pm 0.28) \text{ IO}^{-11}$		$\begin{array}{c} 4.53.10^{-11} \\ 1.53.10^{-11} \\ 2.04.10^{-11} \\ 2.04.10^{-11} \\ 1.19.10^{-11} \\ 1.20^{-11} \end{array}$		8 1.3.10 ² 3.5.10 ² 6.4.10 ²	1 17 18		1 4 17 18	2.5.10 ⁴ 3.5.10 ⁴ 4.5.10 ⁴ 5.5.10 ⁴	<75	(2-3) 10 ⁴ (3-4) 10 ⁴ (4-5) 10 ⁴ (5-6) 10 ⁴
outer ring cityyers m ⁻² sec ⁻¹ st ⁻¹ unit N ⁻¹	Outer ring	Inner ring	Outer ring	Inner ring	Total ring	Outer ring	Inner ring		tang dista Ore	Aange

all S m ² sc ⁻¹ s ⁻¹ unit N ⁻¹		(9.78 ± 0.68) 10 ⁻¹¹		$(3.78 + 0.28) 10^{-11}$		(2.11 <u>+</u> 0.23) 10 ⁻¹¹	$(1.90 + 0.15) 10^{-11}$		(6.80 ± 0.26) 10 ⁻¹²	(1.79 <u>+</u> 0.08) 10 ⁻¹²	(6.81 ± 0.41) 10 ⁻¹³	(4.36 <u>+</u> 0.28) 10 ⁻¹³	$(2.44 \pm 0.19) 10^{-13}$	$(1.24 + 0.09) 10^{-13}$		$(6.60 + 0.61) 10^{-14}$		(1.79 ± 0.13) 10 ⁻¹⁴	(3.70 ± 0.62) 10 ⁻¹⁵	(1.40 <u>+</u> 0.40) lo ⁻¹⁵	$(3.11 \pm 0.64) 10^{-16}$	(1.50 <u>+</u> 0.34) 10 ⁻¹⁶	
	$(4.53 \pm 4.53)10^{-11}$	$(1.53 \pm 0.76)10^{-11}$	(2.04 ± 0.49)10 ⁻¹¹	(1.19 ± 0.28)10 ⁻¹¹	(8.17 ± 1.7) 10 ⁻¹²	$(5.73 \pm 1.35) 10^{-12}$	$(6.87 \pm 1.35) 10^{-12}$	(2.50 <u>+</u> 0.69) 10 ⁻¹²	(1.86 ± 0.13) 10 ⁻¹²	(4.53 ± 0.38) 10 ⁻¹³	$(1.31 \pm 0.15) 10^{-13}$	$(8.32 \pm 1.04) 10^{-14}$	$(4.64 \pm 0.72) 10^{-14}$	(3.67 ± 0.62) 10 ⁻¹⁴	(2.36 <u>+</u> 0.49)10 ⁻¹⁴	$(2.13 \pm 0.52) 10^{-14}$	$(1.11 \pm 0.33) 10^{-14}$	$(5.37 \pm 0.74) 10^{-15}$	(1.36 ± 0.39) 10 ⁻¹⁵	$(2.85 \pm 1.64) 10^{-16}$	$(1.4 \pm 0.4) 10^{-16}$	(9.35 <u>+</u> 2.81) 10 ⁻¹⁷	
2	(4.36 <u>+</u> 1.45) 10 ⁻¹¹	(2.32 <u>+</u> 0.62) 10 ⁻¹¹	$(2.24 \pm 0.49) 10^{-11}$	$(1.34 \pm 0.27) 10^{-11}$	$(9.80 \pm 2.04) 10^{-12}$	$(6.04 \pm 1.42) 10^{-12}$	$(6.91 \pm 1.32) 10^{-12}$	$(7.14 \pm 1.31)10^{-12}$	(1.84 ± 0.12)10 ⁻¹²	(6.1 <u>+</u> 0.47) 10 ⁻¹³	(2.81 <u>+</u> 0.26) 10 ⁻¹³	(1.88 ± 0.18) 10 ⁻¹³	(1.02 ± 0.12)10 ⁻¹³	(5.69 <u>+</u> 0.81) 10 ⁻¹⁴	$(4.57 \pm 0.71)10^{-14}$	(3.35 ± 0.58) 10 ⁻¹⁴	(2.86 <u>+</u> 0.54) 10 ⁻¹⁴	(7.19 ± 0.80) 10 ⁻¹⁵	$(1.21 \pm 0.35) 10^{-15}$	$(5.21 \pm 2.32) 10^{-16}$	(5.50 <u>+</u> 2.24) 10 ⁻¹⁷	$(2.98 \pm 1.72) 10^{-17}$	
1.1.1	(4.4. <u>+</u> 0.88) 10 ⁻¹¹	$(2.92 \pm 0.48) 10^{-11}$	(2.02 ± 0.32)10 ⁻¹¹	(1.62 ± 0.26) 10 ⁻¹¹	(1.63 ± 0.23) 10 ⁻¹¹	$(9.40 \pm 1.46) 10^{-12}$	$(8.12 \pm 1.31) 10^{-12}$	(6.39 <u>+</u> 1.09) 10 ⁻¹²	(3.1 <u>+</u> 0.2) 10 ⁻¹²	(7.31 ± 0.60) 10 ⁻¹³	(2.69 <u>+</u> 0.29) 10 ⁻¹³	(1.65 ± 0.2) 10 ⁻¹³	(9.57 ± 1.37) 10 ⁻¹⁴	(5.43 <u>+</u> 0.96) l0 ⁻¹⁴	$(3.14 \pm 0.67) 10^{-14}$	(2.41 <u>+</u> 0.58) 10 ⁻¹⁴	$(1.35 \pm 0.41) 10^{-14}$	(5.33 <u>+</u> 0.74) 10 ⁻¹⁵	$(1.13 \pm 0.34) 10^{-15}$	(5.92 ± 2.96) 10 ⁻¹⁶	(1.16 ± 0.41)10 ⁻¹⁶	(2.67 <u>+</u> 1.19) 10 ⁻¹⁷	
2	2.5.10 ⁴	3.5.104	4.5.104	5.5.104	6.5.10 ⁴	7.5.104	8.5.104	9.5.104	1.5.10 ⁵	2.5.10 ⁵	3.5.105	. 4.5.10 ⁵	5.5.10 ⁵	6.5.10 ⁵	7.5.105	8.5.10 ⁵	9.5.10 ⁵	1.5.106	2.5.10 ⁶	3.5.106	5.8.106	1.4.107	
Cor Istaib Istange		< 75								.		•								< 75	<105	<105	
Range	(2-3) 10 ⁴	(3-4) 10 ⁴	(1-5) 10 ⁴	(5-6) 10 ⁴	(6-7) 10 ⁴	(7+8) 10 ⁴	(8-9) 10 ⁴	(9-10) 10 ⁴	(1-2) 10 ⁵	(2-3) 10 ⁵	(3-4) 10 ⁵	(4-5) 10 ⁵	(5-6) 10 ⁵	(6-7) 10 ⁵	(7-8) 10 ⁵	(8–9) 10 ⁵	(9-10) 10 ⁵	(1-2) 10 ⁶	(2-3) 10 ⁶	(3-4) 10 ⁶	(4-7) 10 ⁶	(0.7-2) 10 ⁷	

TABLE 5.2f : Final differential size spectrum of showers with $\theta < 30^{\circ}$ for all values of the age parameter S.



Figure 5.20 : The vertical differential size spectrum of E.A.S. at sea level for showers with different values of the age parameters. The total rate for showers of all age parameter is also shown. The work of Hillas (1970) and Parvaresh (1975) are also plotted for comparison.



Figure 5.21 :

Comparison of the vertical differential size spectrum of E.A.S. at sea level assuming that all showers obey the Catz average electron lateral structure function (open circles), with the more accurate evaluation taking the age parameter of individual showers into account (solid points). The full lines are the previous work of Hillas (1970) and Parvaresh (1975).



Figure 5.22 : Comparison of the vertical integral size spectrum of E.A.S. at sea level assuming that all showers obey the Catz average electron lateral structure function (open circles) with the more accurate evaluation taking the age parameter of individual showers into account (solid points). The full lines are the previous work of Hillas (1970) and parvaresh ·1975)



Figure 5.23 : Comparison of the vertical integral size spectrum of E.A.S. at sea level taking into account the age parameter of individual showers with other recent measurements.

CHAPTER 6

LATERAL DISTRIBUTION UF MUONS

IN E.A.S. AT SEA LEVEL

6.1 THE MUON COMPUNENT

The muon component of extensive air showers (E.A.S.) has been investigated by numerous workers because of its close link to the nuclear cascade and nuclear interactions. From a practical viewpoint, this component is easier to study than the more fundamental particles of the nuclear cascade, because it can be isolated with relative certainty from the other components of the shower. Also, muons are of interest because of their weak interaction with matter. As penetrating particles they carry information about the early stages of E.A.S. development, and about the primary particles and their mechanism of interaction. The average muon energy in a typical shower is much more than that of the electron component. At sea level, they carry much more total energy than the electrons, therefore this energy is a good measure of the primary energy.

An important parameter of the muon component is its lateral distribution, which is of great importance since it provides information about the transverse momenta of the parent pions and the height of origin of the muons in the atmosphere. The height of origin is dependent on the rate of development of the nuclear cascade in the atmosphere which is related to the multiplicity of secondary particle production in high energy interactions.

- 51 -

In practice, measuring the lateral distributions of muons is difficult because of the low number of muons relative to the number of electrons present in the shower. It is necessary to construct a large and well-shielded muon detector to obtain accurate measurements. The muon detector is usually operated in conjunction with an E.M.S. array to provide information about the other shower parameters. The total number of muons with energy greater than E_{μ} in a shower, N_{μ} (> E_{μ}), is obtained by integrating average $2\pi rdr \times$ the average density distribution function over all core distances, where E_{μ} is the muon threshold energy defined by the detector absorber thickness.

In a shower, the total number of muons is not proportional to the number of electrons, N_e , but $N_\mu = A N_e^{\alpha}$ where α is a constant less than one. A measured variation of the exponent, α in the shower size range $10^5 - 10^6$ particles could be associated with a possible increase of heavy nuclei in the primary cosmic radiation in the region 10^{15} eV (N.v. Kabonov, et al, 1973).

6.2 THE MUON LATERAL DISTRIBUTION

As muons represent the emission direction of their parent pions rather well, the lateral spread of muons in E.A.S. is mainly due to the acquired transverse momentum of mesons at their generation. A small additional contribution to the lateral spread is produced by a combination of Coulomb scattering and geomagnetic deflection. These are not important except for highly inclined showers, because the path lengths of muons are large in this case. The measurement of the lateral distribution of muons is performed above a

- 52 -

particular energy threshold for various radial distances from the shower core. The early experimental result on the form of distribution was given by Clark et al (1958). Muons of energy greater than one GeV for showers in the size range of $2.10^5 - 2.10^8$ particles were studied. Their results were reduced by Greisen (1960) to the following empirical form :

$$\Lambda_{\mu} (N_{e}, r) = 18 \left(\frac{Ne}{10^{6}} \right)^{0.75} .r^{-0.75} .\left(1 + \frac{r}{320} \right)^{-2.5} (6.1)$$

where $\Delta_{\mu}(N_{e},r)$ is the muon density (m^{-2}) at a core distance of r(m) in a shower of size N_{e} .

A more complete form of the lateral distribution of muons for various threshold energies E in the size range of 10^3-10^7 particles was proposed by Bennett and Greisen (1962). The empirical formula is : 0.37

$$\Delta_{\mu}(N_{0}, r, z \in L) = 14.4 \left(\frac{N}{10^{6}}\right)^{0.75} r^{-0.75} \left(1 + \frac{r}{320}\right) \left(\frac{51}{E_{\mu} + 50}\right) \left(\frac{3}{E_{\mu} + 2}\right)^{0.14r}$$
(6.2)

where E_{μ} is in GeV and the formula is valid for muons of energies of 1-10 GeV. No serious deviation of experimental results from the above formula has been observed up to the present time. Figure (6.1) shows the prediction of formula (6.2) for muons with energies, $E_{\mu} > 1$ GeV, compared with the results of various experiments. It is seen that the measured muon densities at small core distances are lower than expected. This was interpreted to bedue to errors in core location and to the effect of normalizing the measured results to a fixed shower size of 2.10⁷ particles. The previous result for the



Figure 6.1 : The muon lateral distribution for 1 GeV energy threshold. All data are normalized to a shower size $N = 2.10^7$ particles. The continuous curve was calculated according to Greisen's formula (After Wdowczyk, 1973).

lateral distribution of muons of different threshold energy, shower size, zenith angle and core distance ranges and also its correlation with the electron component (represented by the age parameters of the shower) are considered in the next section, where a comparison is made between the theoretical standard cascade model and the experimental data observed by several workers.

6.3 PREVIOUS MEASUREMENTS

6.3.1 Allan et al (1968).

The muon detector consisted of four scintillation detectors, of total area 10 m^2 , shielded by a sheet of lead 20 cm thick. The detector was located at the central position of the Haverah Park E.A.S. array so that it could be operated in conjunction with all three sub arrays of radius 50 m, 150 m and 500 m respectively. The shower sizes to which these arrays were sensitive were 2 x 10^5 to $4 \cdot 10^6$, 10^6 to 10^7 and $5 \cdot 10^6$ to 10^8 particles respectively. In this work the lateral distribution of the muon component and the variations of the total number of muons with shower size have been studied. The variation of the number of muons was found to be governed by the relationship

$$N_{\rm H} \propto N$$
 (6.3)

where the exponent 0.75 is constant over the whole range of shower sizes $N_e = 3.10^5$ to 10^8 particles with zenith angles of less than 27 degrees. In particular, there was no evidence for a discontinuity in the exponent with changing N, which could arise from a change in composition of the primary cosmic radiation. The observed muon densities were normalized to $N_o = 2.10^7$ particles with the aid of equation (6.3), to estimate the lateral distribution of muons with energy greater than 0.3 GeV. From the 50 m and 150 m arrays the variation of muon density with shower size, N_e and core distance, r was found to be

$$\Delta_{\mu} = \kappa_{1} \left(\frac{N}{2 \times 10^{7}} \right)^{\beta_{1}} \frac{\exp(-r/320)}{(r/320)^{\alpha_{1}}}$$
(6.4)
$$\kappa_{1} = 2.5 \text{ m}^{-2} \qquad 3 \times 10^{5} < N < 4.10^{6}$$

with

 $\kappa_{1} = 2.5 \text{ m}^{-2} \qquad 3 \times 10^{3} < N < 4.10^{3}$ $\alpha_{1} = 0.8 \pm 0.01 \qquad 10 \text{ m} < r < 80 \text{ m}$ $\beta_{1} = 0.73 \pm 0.05 \qquad E_{u} > 0.3 \text{ GeV}$

The choice of N = 2.10^7 as normalization size was made to facilitate comparisons with showers recorded by the 500 m array. The lateral distribution of muons for large sizes ($N_{c} > 4.10^6$ particles) was also performed with the 500 m array. Overall, the measured lateral distribution was found to be in essential agreement with Greisen's formula (196U) where the densities were about 15% larger. The dependence of the distribution on r for r > 250 m was a power law of the form r⁻ⁿ. The exponent, n, was observed to decrease with increasing Θ , implying a greater lateral spreading of the muons under a greater thickness of air. The evidence that n changes with 0 suggests that a similar dependence should be observed for changes in N, since both N and O control the age of the shower (i.e. its distance from maximum development) at the level of observation. In this experiment, the statistical evidence was too weak to demonstrate this dependence.

6.3.2 Khristiansen et al (1975)

An underground muon detector, consisting of hodoscoped Geiger-Müller counters with a total area of 37 m² was used in conjunction with an E.A.S. array to investigate the muon component and its correlation with s, the age parameter of the shower. In their early work, Khristiansen et al (1968) studied the correlation between the lateral distribution of muons with energy greater than 10 GeV and the form of the electron lateral distribution, i.e. the parameter s. This result showed that within a core distance range of 10 to 50 m, a muon flux in old showers ($S \ge 1.3$) was 1.64 <u>+</u> 0.2 times a muon flux in young showers.

With the improved statistics of the present work and also their division into two groups of data with $s \le 1$ and $s \ge 1.3$, respectively, the muon lateral distribution was obtained for shower sizes in the range 2.10^5 to 10^6 particles. Figure (6.2) represents the experimental results which are normalized to $N_e = 10^6$ particles with the aid of the relation $\Delta_{\mu} = A N^{0.78}$. The result in the figure can be approximated by a function of the form :

$$\Delta_{\mu} = B r^{-n} exp \left(-\frac{r}{80}\right)$$

where $n = 0.7 \pm 0.07$ for $s \le 1$ $n = 0.5 \pm 0.07$ for $s \ge 1.3$

which shows its correlation up to a distance of 50 m from the shower axis. For large showers, with sizes $N_e = 10^7 - 7 \cdot 10^7$ particles, the correlation between the lateral distribution of muons and the age parameter, s was studied up to 100 m

- 56 -

from the shower core. In this range, two groups of data with $s \le 1.2$ and $s \ge 1.4$ were selected and each yroup was normalized to $N_e = 2.10^7$ particles. These are shown in Figure (6.3). It was found that lateral structure functions with different values of s are of the same form and the relation

$$\Delta_{\mu} (5 \ge 1.4)$$
$$\Delta_{\mu} (5 \le 1.2)$$

has a value of 3.0 <u>+</u> 0.2 averaged over all core distances. Figures (6.2) and (6.3) show that the total number of muons is clearly lower in young showers and that their lateral distribution is steeper. The distributions for larger showers are also clearly steeper.

6.3.3 Wdowczyk et al (1973)

Some theoretical considerations of experimental observations were carried out for muons of energy greater than 5 GeV. The experiment was performed at sea level with a large underground muon detector consisting of G-M counters in conjunction with an E.A.S. array. The parameters investigated here were the muon lateral distribution, muon to electron ratio in E.A.S. and fluctuations of the ratio. To obtain the lateral distribution, muon densities in individual detectors of area, about 12 m^2 , were measured and plotted as a function of the distance between the shower core and the centre of the detector.

The measured lateral distribution of muons for shower sizes of about 10^5 particles resulted in a much wider distribution than expected on the basis of the E.A.S. standard model (multiplicity $\alpha E^{\frac{1}{4}}$) calculated by de Beer et al, (1966). The

- 57 -



Figure 6.2 : Sea level muon lateral distribution for showers with two different age parameters and a fixed size of 10^6 particles (After Khristiansen et al (1975)).



widening of the distribution was interpreted to be more likely due to a high multiplicity of secondary particle production in extremely high energy interactions. The possibility that it could be due to an increase in the mean transverse momentum was not favoured since at those muon energies, the transverse momenta of their parent pions should be normal.

This effect was also reported by a Moscow group, Khristiansen et al (1971). The high multiplicity indicates the fact that a high level of muon production should be due to rapid decrease of the mean energy of secondary hadrons with penetration through the atmosphere. The consistency of the observed fluctuations of the ratio of muon to electron densities versus muon shower size with the theoretical predictions of De Beer et al (1968) for showers of primary mixed composition and of pure proton primary composition indicates that the increase of multiplicity is not caused by a rapid increase of the mean primary mass.

6.3.4 Rozhdestvensky et al (1975)

A magnetic spectrometer was used to study relatively high energy muons in the range (10-90) GeV. The apparatus consisted of the magnetized iron body placed between arrays of wide-gap spark chambers of area 1 m². In order to obtain the density and energy of muons from this experiment, photographs of the spark chambers were scanned and the trajectories of muons before and after the magnet were digitised and fed into a computer. The spectrometer was located at a depth of 40 meters water equivalent (m.w.e) underground at the centre of the E.A.S array of Moscow University in order to investigate muons in the core distance range of 6 to 100 m and the shower
size range of N_e = 3.10^4 - 10^6 particles. Using the data on muon energy spectra at various distances from the shower core and the absolute muon density measured in the previous work for all muons registered underground (i.e. $E_u > 10$ GeV, see Kulikov et al, 1974). The lateral distribution of muons of energies 20, 50 and 90 GeV respectively as shown in Figure (6.4) were obtained. These distributions are compared with theoretical predictions from a standard model which are shown by the full lines in Figure (6.4). It is seen that the experimental lateral distributions are clearly wider than those predicted as was the case in the previous experiment. The widening of the distribution could be due either to a higher transverse momentum than assumed or to a higher level of muon origin in the atmosphere. An alternative explanation is to assume that the energy of the particles in the initial stages of the shower development are degraded at a faster rate. For example, a higher multiplicity law with $n_s \propto E^{\frac{1}{2}}$ may be assumed in contrast with the standard law, $n_{s} \propto E^{\frac{2}{4}}$.

6.3.5 Discussion of Previous Work

The experimental work on the muon component of E.A.S. at sea level can be summarised as follows :

> (i) The lateral distribution of muons depends on zenith angle, especially for large distances (r > 200m) from the shower axis. The function tends to be a power law of the form, r^{-n} , where the exponent n decreases with increasing zenith angle, 0. This indicates a greater spread of muons about the shower axis for showers traversing a greater thickness of the atmosphere. (ii) No significant change in the shape of the lateral



Figure 6.4 : The muon lateral distributions of Rozhdesivensky et al, 1975.

distribution of muons with increase of shower size in the range $10^4 - 10^8$ particles has been observed. (iii) There is a clear correlation between the lateral distribution of muons and the age parameter of the electron photon component. Young showers give a steeper lateral distribution and a greater number of muons than old showers.

(iv) When measured muon lateral distributions are compared with theoretical predictions of a standard model the measured distributions are found to be flatter than expected. This result is interpreted as being caused by a higher multiplicity of secondary particles than the assumed relationship, $n_s \alpha E^{\frac{1}{4}}$.

(v) The Greisen formula of equation (6.2) is the best function that fits the experimental results obtained for muon energies.in the range (1-10)GeV. This formula has been used in the present experiment for comparison purposes.

6.4 PRESENT WORK

6.4.1 The Muon Detector

The muon detector used in the present experiment was a flash tube chamber of sensitive area 2.95 m² which was triggered by the Durham E.A.S array. It was shielded above by a 15 cm lead absorber and also a 15 cm iron absorber. The lead absorber was designed to cut out the soft component (electrons and photons) whereas the iron absorber was placed to separate the muons from the nuclear active particles. The chamber is situated in a tunnel of rectangular cross-section with 30 cm thick barytes concrete walls. This also acts as a filter by absorbing the soft component.

The detailed description of the chamber and the array are given in Chapter 2, and a scale diagram of the front view of the chamber is shown in Figure (6.5).

Events occurring in the chamber were recorded photographically by an automatic camera. For each event triggered, the timing and density information of the air shower were recorded by the array. The array information was used to determine, shower size, core location, arrival direction (zenith angle, Θ , and azimuth angle ϕ), and the age parameter of the shower. Where the chamber data made it possible to investigate the muon component, the procedure of chamber event analysis consisted of projecting the negative of the film onto a scanning sheet of a size reduced in the ratio of 1:13 of the actual size. An example of this is presented in Figure (6.5) showing the passage of muons through the middle of the chamber (AB), which was defined as a reference level to measure acceptable muon tracks. For each event, the number of acceptable muon tracks was counted and the muon density obtained. An acceptable event was defined as one which satisfied the following criteria ;

> (i) the muons passed through the reference level taken as the middle of the chamber. (ii) the muons were parallel to each other to within $\pm 5^{\circ}$ in the projected plane. (iii) the muons had a track length of \ge 60 cm in real space.

These criteria ensured that the tracks counted were due to muons and it excluded any bias due to background muons and

- 61 -

LEAD



Figure 6.5 : A scale diagram showing the passage of muons through the middle AB of the chamber.

any other unreal tracks (i.e. small tracks due to diffused electrons). Events, for which the whole or part of the chamber was obscured by bursts so that measurement was impossible or inaccurate, have been rejected in the analysis of the data.

6.4.2 <u>Data Analysis</u>

Evidence for a change in slope of the size spectrum in the shower size range of 10^5 -10⁶ particles has been described in Chapter 5. It is of interest to investigate if there is any observed effect of this change of slope on the lateral distribution of muons. A total of 3387 triggers with both chamber and array information available were analysed, and are shown with the basic data in Table (6.1). The electron structure function was initially assumed to be the same for all the events. With this assumption, the core location and the size (N_{a}) of each shower was obtained. In the second step of the analysis, the sampling densities of each shower were re-analysed by computer, to find the best N.K.G.function and hence age parameter s as well as the best shower size $N_p(s)$ that fitted the measurements. Ihe average difference of the two sizes (N_e and N_e(s) was found to be about 10 per cent. Measurement of the average lateral distribution of muons raises the problem of the normalisation of the muon densities, $\Delta_{_{\rm II}}(N,r)$ in a shower of size, N at core distance, r. Generally, the relationship $\Delta_{\Pi}(N,r) = F(N) F(r)$ is anticipated, where F(N) is of the form $F(N) = A N^{\alpha}$ as found in previous work. If it is further assumed that F(r) is the same for all N, α can be found from a scatter plot of the number of muons including zeros detected in the chamber as a function of shower size for showers whose cores fall within a given distance of

- 62 -

No.of analysable shower triggers with $\Theta < 50^{\circ}$, orthog- onal core distance from flash tube chamber <70m and chamber operational	2060	1327	3387
No.of analysable shower triggers with 0<50 ⁰ when flash tube chamber operational and no cut on core distance	2263	1798	4061
No. of analysable shower triggers with 0<50 ⁰ and no cut on core distance	2572	2014	4586
Total No. of Shower Triggers	2683	2131	4814
E.A.S.Selection	<pre>Inner ring trigger ; Δ_c(≥4m⁻²),Δ₁₁(≥2m⁻²) Δ₃₁(≥2m⁻²),Δ₅₁(≥2m⁻²)</pre>	Outer ring trigger; ∆ _c (≥4m ⁻²),∆ ₁₃ (≥2m ⁻²) ∆ ₃₃ (≥2m ⁻²),∆ ₅₃ (≥2m ⁻²)	Total

Summary of experimental data used in the analysis. The cut in core distance used was r< 70m from the centre of the flash tube chamber. TABLE 6.1 :

the chamber. Using the value of α found in this way by Nejabat (1980) $\alpha = 0.69 \pm 0.08$, all measured muon densities have been normalised to a standard shower size of 3.10^5 using the relation

$$\Lambda_{\mu} (3.10^5, r) = \Lambda_{\mu} (N, r) \left(\frac{3.10^5}{N}\right)^{\alpha}$$
 (6.5)

6.4.3 The Results of the Present Experiment

The lateral distribution of muons for a sample of 3,387 events was measured for two different zenith angle ranges, $0^{<0\le25}$ and $25^{0<}0\le50^{0}$, respectively. The results are shown in Figures (6.6) and (6.7), where a comparison is also made with the analytical expression given by Greisen (1962), (Equation 6.2), which is evaluated for muon energies of more than 500 MeV in showers of size 3.10^{5} particles.

The distribution for nearly vertical showers, $0 < 0 \le 25^{\circ}$, shows reasonable agreement with Greisen's prediction. For the other zenith angle range, $25 < 0 \le 50^{\circ}$, the distribution is significantly flatter. The previous experimental results of Nejabat (1980) are also shown on the same plots and they are consistent with the present result. The consistency is also valid when the shower size, $N_e(s)$ is used instead of N_e . The age parameter distributions, shower size, and zenith angle distributions, of the total number of events analysed, are shown in Figures (6.8a), (6.8b) and (6.9); only showers with zenith angle of less than 50° being used in the analysis. In the next step, the dependence of the lateral muon distribution on shower size was investigated for the size range intervals of $10^4 - 3.10^5$ and $3.10^5 - 4.10^6$ particles respectively. This was



Figure 6.6 & 6.7 : The lateral distribution of muons for 500 MeV energy threshold and different ranges of zenith angle. All data are normalized to a shower size $N = 3.10^5$ particles. The solid curve was calculated according to Greisen's formula (eqn. 6.2).



Figure 6.8a : Age parameter distributions of the data for different ranges of zenith angle. The percentage of showers that could not be fitted with a value of S in the range 0.6 - 1.8 is $0<0<25^{\circ}$, 3% ; $25<0<50^{\circ}$, 4% ; $0<0<50^{\circ}$, 3.3%.



Figure 6.8b : Shower size distribution of the showers used in the present analysis.



Figure 6.9 : Zenith angle distribution of the showers used in the present analysis.

carried out for different ranges of zenith angle, 0, and age parameter, and comparison was made with the predictions of Greisen's formula. The results are shown in Figures (6.10), (6.11), (6.12) and (6.13). They show no significant dependence of the lateral distribution of muons on shower size in the size range 10^4 - 4.10⁶ particles. This is also true for zenith angle and age parameter ranges of $0 \le 0 \le 50^{\circ}$ and 0.6 <s ≤ 1.8 respectively.

The correlation of the lateral distribution of muons with the age parameter was investigated for nearly vertical showers and a large zenith angle range where the age parameter ranges of less than, and greater than, the average age value s = 1.2 were considered. The results are shown in Figures (6.14) and (6.15). It seems that for showers with a larger age parameter (old showers), the distribution is flatter than for young showers with smaller age values. The muon density at small distances from the core of old showers seems to be smaller than for young showers, where for relatively larger core distances (greater than 20 m) the case is the inverse. This gives the overall result that there are more muons in old showers than young showers of the same size, which will be discussed later in this section. Besides, it should be mentioned that the shape of the lateral distribution of muons apart from the sample for young and nearly vertical showers (the results for which are in very good agreement with the predictions of Greisen), is flatter than predicted, especially for the case of inclined, old showers ($25^{\circ} < \theta < 50^{\circ}$ and S ,1.2) see Figure (6.1).

- 64 -



Figure 6.10 & 6.11 : The dependence of the lateral distribution of muons on shower size for different ranges of zenith angle and age parameter.



Figure 6.12 & 6.13 : The dependence of the lateral distribution of muons on shower size for different ranges of zenith angle and age parameter.



Figure 6.14 & 6.15 : The dependence of the lateral distribution of muons on age parameter for different ranges of zenith angle.

To obtain the value of the exponent, α in the relation $\bar{N}_{_{\rm H}} \sim N_{e}^{\alpha}$ where $\bar{N}_{_{\rm H}}$ is the observed mean number of muons including zeros, in the chamber a scatter plot of \mathbb{N}_{μ} -versus N_{e} was made. Finding \overline{N}_{u} for a given range of N_{p} , the exponent, α was measured from the slope of the line fitted to the experimental points of the $\bar{N}_{\rm c}$ -N relation, which in turn was measured for different ranges of core distance and age parameter as is shown in Figures (6.16) and (6.17). The values obtained for α are tabulated in Table (6.2) for core distance ranges of less than 40 m. As deduced from the table, two points are of considerable importance. The first is the smooth decrease of the exponent α with increase of core distance for old and young showers respectively. The mean shower size for every range of core distance happened to be nearly the same for old and young shower intervals (S $_{\leq}$ 1.2 and 5 > 1.2). The second point is that the average exponent over the core distance range 10-40m is greater for old showers than for young showers provided that the mean shower size is the same. This indicates that the number of muons in old showers is greater than in young showers.

6.5 CONCLUSION

From the results of the previous section, it is concluded that there is no evidence for a significant change of the muon lateral structure function with shower size over the size range of 10^4 -4.10⁶ particles at sea level. The measured lateral distribution of muons in showers with zenith angle $\ge 25^{\circ}$ and age parameter $\ge \ge 1.2$ is significantly flatter than suggested by the empirical analytic expression of Greisen (1962), whereas for near vertical and young showers

- 65 -



Figure 6.16 & 6.17 : Size dependence of the average number of muons observed in the chamber for different ranges of core distance and age parameter.

		< 1.2			> 1.2	
(10-20)		(20-30)	(30-40)	(10-20)	(20-30)	(30-40)
(1.84 <u>+0</u> .06	3) 10 ⁵	(2.18 <u>-</u> 0.1)10 ⁵	(3.71 <u>+</u> 0.15)10 ⁵	(1.87 <u>+0</u> .12)10 ⁵	(2.91 <u>+0</u> .17)10 ⁵	(4.13 <u>+</u> 0.23)10 ⁵
0.74+0.0	4	0.56 <u>+0</u> .03	0.43 <u>+</u> 0.02	0.7 <u>+</u> 0.02	0.65 <u>+</u> 0.05	0.63 <u>+</u> 0.03
	(2	.58 <u>+</u> 0.11)10 ⁵)	(2.97 <u>+</u> 0.17)10 ⁵	
	0	•59 <u>+</u> 0.03			0.66 ± 0.03	

N is the average shower size for showers falling in the given range of r. and \bar{N}_{e} the overall The values of α in Δ (r) = A N^{α} for different ranges of core distance and age parameter. average. TABLE 6.2:

 $(S \le 1.2)$ it is consistent with the formula. The total number of muons in old showers seems to be greater than for young showers, which was also observed in previous work, Khristiansen, et al (1975).

CHAPTER 7

SEARCH FOR QUARKS CLOSE ID THE CORE OF. E.A.S

7.1 THE CONCEPT OF QUARKS

Since the discovery of pions (1947) and many other so-called elementary particles, attempts have been made to understand them in terms of elementary sub-units. Historically, Fermi and Yang (1949) proposed the hypothesis that the π -meson may not be elementary but composite formed by the association of a nucleon and anti-nucleon assuming the existence of a strong binding force between them. However, this hypothesis could not account for all strongly interacting particles as another sub-unit carrying a strangeness quantum number was needed. Sakata (1956) proposed the triplet of proton, neutron, lambda zero and their antiparticles, as sub-units to fill up this gap. By then, the model was able to describe the structure of the octet and singlet meson multiplets but it failed to be consistent with the observed octet and decuplet multiplets of baryons when their properties became firmly established experimentally.

The next development in the theory was by Gell-Mann and Zweig (1964), independently. They noticed that although from the group theory viewpoint, the Sakata model gives the wrong multiplet structure of baryons 3 & 3 & 3 = 15 @ 6 @ 3 @ 3. Eut instead the form 3 & 3 & 3 = 10 @ 8 @ 8 @ 1 agrees with the experimental observations. (& means direct product and @ means direct sum). They also pointed out that all the

hadronic particles (baryons and mesons), could be built up from three types of fundamental entity called quarks (q). They are named as p,n, λ , (or u,d,s) each having spin $1/2\hbar$. They are also characterized by quantum numbers ; isospin (I) and strangeness (S) which are conserved in strong interactions. The isospin, I, is defined by the (2I + 1) charge substates (labelled ${\rm I}_3)$ of a particle, in analogy with angular momentum. As it has already been hinted, the hadrons are of two types : baryons with baryon number B = 1, and mesons with B = 0. However any of their states, (I, S), may be built up from combinations of p, n, λ quarks and their antiparticles. The hadronic charge, isospin and strangeness quantum numbers are related to each other by : $Q = I_3 + \frac{B+S}{2} = I_3 + Y/2$ (7.1) which is called the Gell-Mann/Nishijima formula. Here, Y is the hypercharge quantum number. These quantum numbers are tabulated in Table 7.1.

riplet particles	I ₃	В	S	Y	Q	Spin(ħ)
р] 2	<u> </u> 3	0	13	2/3	1 2
n	- 2	C.ir.	0	<u>]</u> 3	-3	$\frac{1}{2}$
λ	0	3	-1	-2/3	- ±	1 <u>2</u>

TABLE 7.1

It is seen in this table that the baryon number assigned to each quark is fractional. A consequence of this is that the expected electric charge of quarks is also fractional.

The above theory of quarks predicts that all the hadronic states are made up either by combining a single quark (q) with a single antiquark (\overline{q}), i.e. (q. \overline{q}) or by making combinations of three quarks (qqq). In the simplest quark model, therefore, the particle states of the baryons and mesons could be grouped into multiplets. For instance, the baryon multiplets consist of octets and decuplets of states with a particular spin (j) and parity (p), i.e. j^p . Fig.7.1 below shows octet states of baryons of spin parity $j^p = \frac{1}{2}^+$. Here the quark combination (e.g. ppn) of each state in the Gell Mann/Zweing model is also indicated.



Fig.7.1 : Baryon octet, spin parity $j^p = \frac{1}{2}$

The quark model can account for all known strongly particle states. However, on the ground of previous experimental observation of the so known "elementary" particles such as electron, nucleon, pion, we could expect that the proposed quarks ought to be detectable if they exist as free particles. So far the result of experimentation in this direction has led to the following expected properties of them.

(a) Mass of quark

Comparing the known masses of elementary particles and their corresponding combination of quarks, it is found that $M_p \simeq M_n = M$ and $M_\lambda = M + M_\pi$. But if mesons are quarkantiquark systems, then a crude estimation of quark or antiquark mass could be in the range of 5 GeV/C² to several tens of GeV/C².

(b) Decay scheme

A possible decay scheme of quark is shown in Table 7.2 below and it seems that only the p type quark is stable.

Quark	Decay Scheme	Lifetime
p	stable	infinite
n	$n \rightarrow p + \bar{e} + \bar{\nu}_{e}$	∿ sec
λ	$\lambda \xrightarrow{\gamma} \overset{\rho}{\longrightarrow} \overset{+}{\pi} \overset{\pi}{\longrightarrow} \overset{\sigma}{\longrightarrow} \overset{\sigma}{\longrightarrow} \overset{\tau}{\longrightarrow} \overset{\tau}{\to} \overset{\tau}{$	∿10 ⁻¹⁰ sec

TABLE 7.2

(c) Some possible reactions producing quarks If quarks exist as elementary particles, then they will be produced in the interaction of high energy nucleon-nucleon collisions (Ashton et al, 1973a) as follows :

(1) N + N
$$\longrightarrow$$
 N + N + q + \overline{q}
(2) N + N \longrightarrow N + 3q
(3) N + N \longrightarrow 3q + 3q
(7.2)

The interaction will produce either a quark and its antiparticle or the three constituent quarks of the nucleon. Therefore, it should be possible to detect stable quarks experimentally.

7.2 QUARK SEARCH METHUDS

7.2.1 Searches at Accelerators

Accelerators have been applied to investigate quarks that could be produced by some of reaction of eqn.(7.2). In this method, a target is bombarded by the high energy accelerated particle beam. A secondary beam is selected according to the momentum in a given angle with respect to the primary beam. This method is considered to measure the mass and the charge of quarks or any other new particles. To identify the secondary particles a set of electronic and visual detectors is used as the detection system. To measure the charge, a scintillation counter or bubble chamber is used. In the case of employing scintillation counters, a set of them is needed to reduce the fluctuation in determination of the charge. Also, time of flight measurements are used independently of the charge to determine the mass of particles as well

as Cerenkov counters to measure the velocity at fixed momentum. So far, particle accelerators show no positive evidence for the existence of fractionally charge particles but two sensitive experiments that have been reported are now described. D. Antreasyan (1977), searched for noninteger charged particles produced with large transverse momentum in 400 GeV P-Cu collision. The motivation was that a quark might physically be knocked out of a nucleon in a high p, collision. They gave an upper limit for the invariant production cross-section per nucleon for charge $-\frac{1}{3}$ and charge 2/3 as 8.8.10⁻³⁹ and 1.3.10⁻³⁹ cm² GeV⁻² respectively. Also, a search for tungsten ions having an additional charge of $-\frac{1}{3}$ e has been performed by R.N.Boyd (1977). An ultra-sensitive mass spectrometer was used to investigate the mass range of 182-192 a.m.u. No tungsten ions having fractional electron charge were found above a level of 1 part in 1 x 10^{12} of the tungsten sample over the mass range covered.

7.2.2 Searches in Stable Matter

If quarks were produced by cosmic rays, they would be absorbed in some depth x the earth's crust or the oceans. Over the age of the earth, $T = 4.10^9$ years, there should be an accumulated density of quarks in the stable matter of the earth, which is proportional to the cosmic ray flux, j, $(cm^{-2} s^{-1} st^{-1})$. Then, the quark density of the matter is given by the formula,

$$A(quarks/nucleon) = \frac{\pi j T}{N x}$$
 (7.3)

where N is Avogadro's number and π comes from integrating over the flux. Taking eqn.(7.3) gives an estimation of the quark

density as 48 quarks per gram in the water of the oceans. where x = 3 km and $j \sim 5.10^{-11} \text{ cm}^{-2} \text{ s}^{-1} \text{ st}^{-1}$. Some methods of searching for quarks in stable matter are now described. One method is the modified Millikan (1910) oil drop experiment. The purpose is to measure the charge on a droplet of oil which is determined by its motion under the influence of gravity and electric fields in the presence of viscous drag. In the Millikan experiment, the electric and the gravitational forces on the droplet should be comparable in order to measure the precise charge. That is why for a heavier sample an improved technique is required. which is the levitation method. In this method, the test body is placed in a magnetic potential well and the charge on the body is measured by the body's motion under the influence of an electric field. Using the levitation method, Larue et al (1977) reported observing fractional charges in a total of eight heat treated niobium balls. Two balls showed a charge of (0.377 + 0.09)e and (-0.331 + 0.07)e, where the mass of each ball was 90 µy, (Table 7.3). However, to be more confident of these results, confirmation by other workers is required. A recent summary of quark searches in stable matter by the method of oil drops and the levitometer is given by L.Jones (1977) shown in Table 7.3 . Notice that the upper limits of the quark flux shown in the table using different techniques varies widely.

^aSample "rubbed" on spheres of polyethylene to transfer quarks to spheres.

 $\mathbf{b}_{\mathbf{A}\mathbf{h}}$ enrichment factor is included in this figure.

^CValues given are upper limits except last three entries.

 d Flux values given assuming Eq.(5.2) ($y = 5 \times 10^{7} \text{ g cm}^{-2}$) as well as a smaller value of y, smaller than that corresponding to the existing oceans ($y = 5 \times 10^{1} \text{ g cm}^{-2}$).

^eOne pellet of q = 1/3 e reported, although systematic uncertainties precluded quark claim.

= 1/3 e, although systematic uncertainties precluded quark claim. f_{MOSt} pellets appeared to show residual q ^eTwo pellets of residual charge q = (+ 0.337 + 0.009)e and q = (-0.331 + 0.070)e reported. Positive evidence for existence of fractional charge on matter claimed.

TABLE 7.3 : Stable matter quark searches. Oil drops, levitometer (After Jones, (1977)).

Reference	Technique	Source material	Sample mas s(gm)	No. of samples	Quarks per nucleon p	Corresponding quark flux upper limitsd \$ (cm ² sr sec) ⁻¹
Millikan, 1910 Arear	Oil drop	Water Sea water a	10-11 6x10 ⁻¹¹	∼ 100 1000	<10 ⁻¹³ <10 ⁻¹⁴ b	
Stephens, 1966	do to	air air	6-01		-18	
Gallinaro and Murpurgo,1900 Stower Woran and Mrischka	levitometer Ferromannetic	d aplit ce	9 - 0 - 1	5 0	~10 ~10	8-u
1967	levitometer		-10	1	-20 b	
Rank , 1 968	Oil drop	Mineral oil, soy bean oil, cod liver oil, peanut oil	0	46 45 20	012	10 -10
Braginskii et al, 1968	Diamagnetic levitometer	Graphite and sample mixed	10-8	36	<10-17	10 ⁻³ -10 ⁻⁶
Johnston,1969	Superconduct- ing levitometer	Niobium	9x10 ⁻⁶	2	<10-19	10-5-10-8
Morpurgo,Gallinaro, and Palmieri, 1970	Diamagnetic levitometer	Graphite	5×10 ⁻⁷	75	<5×10 ⁻¹⁹	5x10 ⁻⁵ -5x10 ⁻⁸
Hebard and Fairbank,1971	Superconduct- ing levitometer	Niobium	7×10 ⁻⁵	N	2x10 ⁻ 20 e	2x10 ⁻⁶ -2x10 ⁻⁹
Garris and Ziock,1974	Ferromagnetic levitometer	Iron	3x10 ⁻⁵	12	5×10 ^{-20 f}	5×10 ⁻⁶ -5×10 ⁻⁹
LaRue,Fairbank, and Hebard, 1977	Superconduct- ing levitometer	Niobium	9x10 ⁻⁵	ω	2x10 ⁻²⁰ 9	2x10 ⁻⁶ -2x10 ⁻⁹
Gallinaro, 1977	Ferromagnetic levitometer	Iron	2×10 ⁻⁴	e	<3x10 ⁻²¹	3x10 ⁻⁷ -3x10 ⁻¹⁰

7.3 CUSMIC RAY SEARCHES

Since the proposal of quarks by Lell-Mann (1964), searches in cosmic rays have been of interest as they contain a much higher range of particle energy than is produced by the accelerators. Experiments have been performed at different depths in the atmosphere and underground using different techniques. A summary of the progress in the subject is given by L. Jones (1977).

7.3.1 Single Particle Searches

One of the most numerous types of quark searches is by using a vertically arranged set of detectors in coincidence. It has been done by using scintillation counters in such a way that the recorded pulse height of the detectors is sensitive to the fractional charge ionization of single particles. Searches have been done at mountain altitudes, e.g.Krider(1970) and underground, e.g. Briatore (1968), respectively. The problem with these experiments is to distinguish the recorded spurious events that are produced, for instance, by a low energy electron shower, hitting the side of the detectors and giving small relevant pulses and also statistical fluctuations. This problem could be reduced by increasing the number of the detectors or by using track detectors such as a flash tube chamber (Ashton et al, 1968) or spark chambers (Chin, 1971), to ensure that the events are indeed single and specified.

The combination of the independent single particle experiments, assuming they are all equivalent gives the overall flux limits of quarks as $j \leq 1.1.10^{-11}$ (cm⁻² sec⁻¹ st⁻¹) for e/3, and $j \leq 2.4.10^{-11}$ (cm⁻² sec⁻¹ st⁻¹) for 2e/3 with 90% confidence level (see L. Jones, 1977).

7.3.2 Search in E.A.S.

Since extensive air showers are produced by the interaction of energetic primary particles (E₀ > 10¹⁴ eV) with air nuclei, it is likely that quarks may exist as secondary particles of the shower. Many searches have been made for quarks in E.A.S, especially near the core of the shower using different techniques, often visual detectors. One exciting result was reported by McCusker et al (1969) which claimed to have observed quarks. They used a cloud chamber and found five possible quark events which gave a flux of 5.5.10⁻¹⁰ cm⁻² sec⁻¹ st⁻¹ with charges 2e/3. After their claim for the events to be genuine, questions were raised by a number of workers (Rahm et al. (1970); Kiraly et al (1970); Frauenfelder (1970). The criticism concerned whether the droplet count along the tracks was anomalously low due to technical problems associated with the cloud chamber technique. McCusker et al continued to repeat the experiment with somewhat improved technique. However, for a longer running time, no confirmation of the detected quarks was obtained.

The other positive result was reported by Chu et al, (1970) using film obtained from a heavy shielded liquid bubble chamber. They identified two tracks as quarks corresponding to a flux of 10^{-7} cm⁻² sec⁻¹ st⁻¹, which was sharply criticised by Allison et al (1970), and the Michigan group which designed and built the chamber (Sinclair, 1970). Their flux was quite high and in disagreement with many convincing negative results. However, the rest of the experiments searching for quarks give negative results and so far there is no strong evidence that shows quarks exist.

7.4 PRESENT EXPERIMENT

7.4.1 Introduction

In this experiment the flash tube chamber was used as the quark detector in conjunction with the E.A.S. Array which has been described in Chapter 2. Some relevant properties of the chamber are now described. The efficiencytime delay variation of the flash tubes is theoretically given in terms of the parameter afQ (Lloyd, 1960), where a is the tube radius, f is the average probability that a single electron produces a flash and G is the average number of initial electrons produced per unit length in the neon gas. The Lloyd parameter (af4) was empirically measured (Ashton et al, 1973) to have the value 9 + 1 for the best fitted curve to the points (Fig.7.2) and also the curve for the particles of charge e/3 corresponding to afQ = $\left(\frac{1}{3}\right)^2$.9 = 1 is presented. It is apparent from Figure 7.2 that the difference between the efficiency for e and e/3 particles increases as $T_{\rm D}$ increases but for finding the optimum $T_{\rm D}$ for the experiment a limit is set when an e/3 track has so few flashes that it is not distinguished from random background flashes. Therefore, the time delay was chosen to be T_{fi} = 20 µsec as it gives a reasonable separation in the distribution of the number of flashes along the particle tracks between charges e and e/3.

The chamber does give a good resolution to particles of charge e/3 but does not to particles of charge 2e/3 as will be shown in the following section. It is assumed that the median momentum of the muons measured in the chamber is 2.1 Gev/c, which was calculated from the muon spectrum of Hayman and Wolfendale (1962). Further, it is assumed that



Figure 7.2 : The variation of the internal efficiency of the flash tubes as a function of time delay, T_D . The full curve represents the theoretical prediction with afQ = 9 as a best fit to the experimental points. The curve with afQ = 1.0 corresponds to a particle of charge $e/_3$. The curves — indicate the latitude of uncertainty, (after Ashton et al, 1973).

the curve given by Crispin and Fouler (1970), describes the variation of the most probable ionization loss in neon as a function of muon momentum. This makes it possible to obtain $\frac{1}{I_{-}}$ and $\frac{1}{P}$ ratios which are 1.14 and 0.69 respectively, where I_m and I_m are minimum and plateau ionization losses. Taking these ratios, the values of afU for $I_{\rm m}$ and $I_{\rm p}$ are calculated to be $\frac{9^{\pm}1}{1.14} = 7.9 \pm 0.9$ and $\frac{9^{\pm}1}{0.69} = 11.3 \pm 1.3$ respectively when $T_{\hat{D}}$ is 20 $\,\mu\,sec\,$. However, these af4 values are for particles of charge e, and for charge e/3 and 2e/3 they are expected to be 1/9 and 4/9th of its value as shown in Table 7. 4 . Knowing afQ values makes it possible to obtain the internal efficiency at fixed $T_{\rm m}$ which is related to the expected number flashes in (F2a and F2b) which contains 96 layers of tubes as shown in Table 7.4 considering particles of charge e, e/3 and 2e/3 and also the minimum and plateau ionization regions. In column 7 the expected standard deviation (S.D.) of the expected number of flashes about the mean taking various T_D is shown (Saleh, 1975). However, considering the last two columns of the table gives the e/3 quark track efficiency to be in the range F2a and F2b = 28-50 flashes and the corresponding ranges for particles of charge 2e/3 and e are (60-70) and (70-82) flashes. Therefore, it can be seen that the chamber could not resolve 2e/3 quarks because it cannot distinguish them from particles of charge e, but it is possible to resolve e/3 quarks, if any.

e I	harge	Ionisation Loss	aflQl	Internal efficiency (%) η _I (for T _D = 20 μ s)	Layer efficiency (%) n_L = 0.873 n _I	Expected No. of flashes in F2a + F2b (96 layers)	Expected standard dwiation of the distribution of number of flashes about mean = 96 n _I
$ \begin{bmatrix} I \\ m \\ m \end{bmatrix} = \begin{bmatrix} 7.9 \pm 0.9 \\ 1 \end{bmatrix} = \begin{bmatrix} 89 \pm 1 \\ 1.26 \pm 0.9 \end{bmatrix} = \begin{bmatrix} 77.6 \pm 0.9 \\ 43.5 \pm 2.6 \end{bmatrix} = \begin{bmatrix} 74.5 \pm 0.9 \\ 43.5 \pm 2.6 \end{bmatrix} = \begin{bmatrix} 74.5 \pm 0.9 \\ 43.5 \pm 2.6 \end{bmatrix} = \begin{bmatrix} 73.5 \pm 2.6 \\ 34.4 \pm 2.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.6 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix} 73.7 \pm 1.5 \\ 70.9 \pm 1.5 \end{bmatrix} = \begin{bmatrix}$		ца	11.3 ± 1.3	92 + 1	80.0 + 0.9	77.1 <u>+</u> 0.9	+ 4.5
$ \begin{bmatrix} 2/3 \\ P \\ P \\ m \end{bmatrix} \begin{bmatrix} 1, 26 \pm 0.15 \\ P \\ m \end{bmatrix} \begin{bmatrix} 52 \pm 3 \\ 41 \pm 3 \\ 5.04 \pm 0.1 \end{bmatrix} \begin{bmatrix} 32.5 \pm 3 \\ 41 \pm 3 \\ 73.7 \pm 1.6 \\ 73.7 \pm 1.6 \\ 73.7 \pm 1.6 \\ 70.9 \pm 1.5 \\ 70.9 \pm 1.5 \\ 70.9 \pm 1.5 \\ 70.9 \pm 1.6 \\ 70.9 \pm 1.5 \\ 70.9 \pm 1.6 \\ 70.9 \\$	0	, 1 ₆	7.9 <u>+</u> 0.9	89 + 1	77.6 ± 0.9	74.5 ± 0.9	+ 4.7
a/3 I _m 0.88± 0.1 41 ± 3 35.8 ± 2.6 34.4 ± 2.5 a/3 I _p 5.04± 0.6 84.5± 1.8 73.7 ± 1.6 70.9 ± 1.5 a/3 I _m 3.52± 0.4 78 ± 2 68.0 ± 1.7 65.2 ± 1.6	e/3	ц	1.26+ 0.15	52 + 3	45.4 <u>+</u> 2.6	43.5 <u>+</u> 2.6	6°3 +1
a/3 I P 5.04± 0.6 84.5± 1.8 73.7 ± 1.6 70.9 ± 1.5 a/3 I P 3.52± 0.4 78 ± 2 68.0 ± 1.7 65.2 ± 1.6	e/3	ц	0.88+ 0.1	41 <u>+</u> 3	35 . 8 <u>+</u> 2.6	34.4 + 2.5	2°8 1+
a/ ₃ I _m 3.52±0.4 78±2 68.0±1.7 65.2±1.6	e/3	ᆈᅆ	5.04 <u>+</u> 0.6	84.5 <u>+</u> 1.8	73.7 ± 1.6	70.9 <u>+</u> 1.5	+ 4.9
	e/3	н ^е	3.52 <u>+</u> 0.4	78 ± 2	68.0 + 1.7	65.2 <u>+</u> 1.6	د ۲ +۱

The expected number of flashes produced by plateau and minimum ionising (I and I) e particles, e/3 and 2e/₃ quarks in F2a and F2b layers for time delay T $_D^2$ 20 μs^m •• TABLE 7.4

(after Saleh, 1975).

7.4.2 The Basic Data and Analysis

The basic data of the flash tube (F/T) chamber for all E.A.S. triggers are 4547 events which, with the details concerning running time and the number of charge e/3 guark candidates, are presented in Table 7.5. The flash tube film events were scanned and copied on a special skeleton diagram of the chamber. The number of flashes were counted along the track of every event showing a measurable track. A measurable track is one that passes through the regions F2a (48 layers of tubes) and F2b (48 layers of tubes) with the added requirement that at least one flashed tube must occur on the track in each of the defining layers Fla(8 layers of tubes), F1b (6 layers), F3a (8 layers) and F3b(8 layers) -see Figure 6.5 . The number of triggers with 0,1,2 etc. measurable tracks for the two E.A.S. selection triggers are shown in Table 7.6, and the distribution of their number of flashes in the defined (F2a & F2b) layers of the flash tube chamber is shown in Figure 7. 3. In the tail of the distributions, in the e/3 quark region (less than fifty flashed tubes) two quark-like tracks are observed which are presented in Figure 7.4a and 7.4b, where the full details of the two events are also given in Table 7.7. The above measurements are again performed for all analysable shower where the shower information of every event N_p, r_{H} , Θ and ϕ are known (Table 7.6 and Figure 7.5). The shower size and core distance distributions for these events are shown for the two E.A.S. selection triggers in Figure 7.6a and 7.6b. The next step in the analysis of the data was by dividing it in two different core distance ranges of less or bigger
r r,N,Θ,φ, known known known l 2299 l	i r.N.Θ.φ. known known known known l 2299 l 1826 0
r,N, θ, φ, known 2	r,Ν,Θ,φ, known 2 0
2552	2552 1995
20.96±0.40	20.96 <u>+</u> 0.40 5.56 <u>+</u> 0.12
128	128 383.27
2683	2683 2131
Inner Ring Trigger	Inner Ring Trigger Outer Ring Trigger
	Outer Ring Trigger 2131 383.27 5.56±0.12 1995 0 1826 0

Summary of the basic data.

TABLE 7.5

by the inner ring and outer ring trigger respectively. The figures refer to all E.A.S. triggers and those in brackets to E.A.S. in which the core position, shower The frequency distribution of observing n measurable tracks for E.L.S. selected size, and arrival direction are known.

Outer ring trigger	Frequency xn	(0) 0	271 (254)	172 (166)	60 (60)	28 (28)	15 (15)	6 (6)	7 (7)	(o) o	Total No. of tracks = 559 (536)
	Frequency	1606 (1457)	271 (254)	86 (83)	20 (20)	(2) (2)	3 (3)	1 (1)	T (T)	(0) 0	Total No. of triggers = 1995 (1826)
g trigger	Frequency xn	(O) O	354 (321)	154 (142)	48 (45)	16 (16)	5 (5)	(o) o	(0) 0	(0) 0	Total Nc. of tracks = 577 (529)
Inner ring	Frequency	2100 (1887)	354 (321)	77 (71)	16 (15)	4 (4)	1 (1)	(0) 0	(o) o	(0) 0	Total No. of triggers = 2552 (2299)
	No. of triggers with n measurable tracks in Chamber	0	-1	2	m	4	S	Q	7	ω	

TABLE 7.6 :



Figure 7.3 : Frequency distribution of the observed number of flashed tubes in $F2_a + F2_b$. The arrows indicate the expected number of flashes for minimum ionising and plateau ionising charge e, 2e/3 and e/3 pts. The small bars indicate the uncertainty in the position of the arrow and the large bars, the expected standard deviation of the distribution.

Figure 7.4a : Event M53 -	- 11E419 (inne	er ring trigger)
A low effic	ciency tra	ck	
N (F∠a & F2	2b)	Ξ	17
	г _Н	Ξ	27 m
.:	Ne	=	1.4.10 ⁵ pts
	Θ	E	8.5 ⁰
	φ	=	263 ⁰
Measured projected zenith	angle, ¤ _m	=	-16.5 ⁰
Predicted projected zenit	h angle,α p	=	+1.040
,			



Figure 7.40Event M57 - 11Ex90 (inner ring trigger)A quark candidateN (F2a & F2b)= 26

r_H = 4.6 m N_e = 1.5.10⁴ pts

Measured projected zenith angle, $\alpha_m = +7^{\circ}$

no timing data



No. of flashes on quark candidate track	17	26
Measured projected zenith angle of other tracks	l	-10
No. of other tracks in photo	0	Ч
Z	1.4.10 ⁵	1.5.10 ⁴
÷	263 ⁰	I
Ū	ى ھ	I
г ^г н (п)	27	4°6
α expected	+ 1.04 ⁰	No timing data
α measured	-16°50	° +
Quark Candidate	Event 1	Event 2

arrival direction determined from the E.A.S. array fast timing measurements. r_H is the distance of the E.A.S. core from the centre of the flash tube chamber. $\theta, \phi,$ N are the zenith angle, azimuth angle and shower size of the projected zenith angle of the quark candidate track in the front view of angle assuming that real quark tracks are closely parallel to the E.A.S. $\alpha\,(\text{measured})\,\,\text{is the measured}$ the flash tube chamber and $\alpha(\text{expected})$ is the expected projected zenith Details of the two quark candidate events. E.A.S. TABLE 7.7 :

-



Figure 7.5 : Frequency distribution of the observed number of flashes in $F_a^2 + F_b^2$ where all shower information r_H, N_e, θ and ϕ are known. The arrows indicate the expected number of flashes for minimum ionising and plateau ionising charge e, 2e/3 and e/3 pts. The small bars indicate the uncertainty in the position of the arrow and the large bars, the expected standard deviation of the distribution.









than 75 meters as shown in Table 7.8 and Figure 7.7 to 7.8b. From Figure 7.7 and Table 7.7, it is seen that the two quark candidates are in the small core distance range and both are observed in E.A.S. selected by the inner ring selection system but only one has all shower information.

7.4.3 The Quark Candidates

To decide whether the two observed quark-like events are genuine guarks, it is first necessary to consider the expected number of background muons. Background muons may simulate low efficiency tracks in the expected e/3 quark region of (17-50) flashes in (F2a & F2b) if they traverse the sensitive volume of the chamber in the time domain 100 to 161 us before the chamber trigger (see Figure 7.2). Knowing the calculated flux of muons (31.5 sec^{-1}) through the chamber acceptance volume, the expected number of background muons simulating e/3 guarks in a sample of 4,547 triggers is $4547 \times 61.10^{-6} \times 31.5 = 8.7$. This is larger than the observed number of 2 and the lack of background muon events can only be accounted for as a statistical fluctuation. Therefore, there is a high possibility that the two observed events are background muons that simulate e/3 quark-like tracks. Examining the quark candidates individually shows that for the first event, there is evidence of knock on electron flashes on the quark-like track. Also, the measured projected zenith angle of the quark-like track is -16.5° compared with an expected value of $+1.0^{\circ}$ assuming that a genuine guark track would be close in direction with the E.A.S. arrival direction. This evidence strongly suggests that the first event is a background muon.

e tracks	
measurable	
of	
no.	•
f observing	ore distance
o V:	ਂ ਯੂ
quenc	ges o
Fre	ran

Frequency X	o	575	308	105	44	20	6	7	0	1065
Frequency of n tracks in chamber r _H > O	3344	575	154	35	11	4	1	4	0	4125
۲ م ۲ م ۲	0	103	66	39	24	15	0	0	0	247
Frequency of η tracks in chamber r _H \$75 m	481	103	33	13	و	£	ο	ο	0	639
Frequency X n	0	472	242	66	20	S	و	7	0	818
Frequency of n tracks in chamber $r_{ m H}^{-75}$ m	2863	472	121	22	S	l	ı	1	0	3486
No. of n measurable tracks in chamber	0	-1	2	£	4	S	ę	7	8	Totals

in chamber for different **TABLE 7.8**:

r

Ų







Figure 7.8a : Shower size distribution of events with > 1
measurable track in chamber for different ranges
of core distance.





The second event also shows evidence for a low efficiency knock on electron track having a total of 4 flashed tubes occurring just below the middle of F2a. For a genuine quark track producing a knock on electron the number of flashed tubes on this track should be larger. Also, it is seen from Figure 7.4b that the quark-like track makes a large angle with the high efficiency track in the chamber which is almost certainly related to the E.A.S. producing the trigger. Unfortunately, no fast timing measurement was available from the E.A.S array to determine the shower arrival direction for this event but the evidence presented above is sufficient to rule out it being a genuine quark.

7.4.4 Conclusion

From a sample of 4547 E.A.S. triggers covering the size range $10^4 - 10^7$ particles and the core distance range 0-100 m from the flash tube chamber, no evidence for a finite flux of charge e/3 quarks has been found. In all 1,136 tracks of penetrating charge e particles were measured. Thus the ratio of penetrating charge e/3 particles to penetrating charge e particles is $< \frac{1}{1,136}$ for E.A.S. in the size range and core distance range detailed in the text.

CHAPTER 8

THE ARRIVAL DIRECTIONS OF E.A.S IN GALACTIC COORDINATES

8.1 INTRODUCTION

As the earth spins around its axis, different parts of the sky will be scanned by an instrument on the earth. Thus, if point sources of high energy cosmic rays exist or there is anisotropy in their arrival directions, then a variation in detection rate with sidereal time is expected. Time variations of E.A.S may also be produced by changes in atmospheric temperature and pressure but these effects should average themselves out over a long observation time.

8.2 PREVIOUS ANISOTROPY MEASUREMENTS IN THE E.A.S ENERGY_RANGE

Since the discovery of cosmic rays in (1912), efforts have been made by many workers to find any significant anisotropy of the primary flux in sidereal time. No positive result has been obtained or if it has, it has not been confirmed by other similar experiments. In recent years (after 1975) more precise experiments have been carried out. The first strong evidence of an anisotropy in the primary energy range of $(10^{13}-10^{14})$ eV, was given by Gombosi et al (1975) and Nagashina et al (1977).

In the higher energy range, between 10¹⁴ and 10¹⁷ eV, a review paper by Linsley and Watson (1977) also gave positive evidence for an anisotropy which was supported by the positive experimental result of Pollack et al (1978) where the shower primary energy range of 6.10¹⁶-10²⁰ eV, was investigated. In these experiments the anisotropy was specified by the amplitude of the first harmonic which was fitted to the observed sidereal variation. Amplitudes of previous work were examined and summarized by Wolfendale et al (1977,1978) and Kiraly et al (1979) and are shown in Figure (8.1). Two features of this analysis are of particular interest in understanding the nature and origin of cosmic rays. As is shown in the figure, the first feature is the increase of anisotropy with energy. Second, is the change of slope of anisotropy versus energy at around $3 \cdot 10^{15}$ eV where the primary energy spectrum also has a change of slope.

8.3 PRESENT WORK

8.3.1 Experimental Arrangement

The Durham E.A.S. array was described in Chapter two and has been used in the present experiment to detect E.A.S using both the inner and outer ring triggering modes. The outer ring trigger was also used independently, where the record of the events with relatively greater shower size range was desired.

The advantage of this array is its sensitivity to the shower size range of (10^5-10^6) particles which covers particle energies around 3.10^{15} ev which is of particular significance in measurements of anisotropy as this is the energy region in which the primary energy spectrum changes slope.

Apart from the shower size, the required parameters from the array were the occurrence time of the events and also the arrival direction, (the zenith angle, 0, and azimuth



Figure 8.1 : Amplitude of harmonic analysis versus primary energy (after Wolfendale, et al 1977,1978)

angle, ϕ , of individual showers which is obtained from the timing information of the shower front). From knowing the arrival direction (Θ , ϕ) of the primary particles, it is possible to calculate its corresponding arrival direction in celestial coordinates (right ascension, RA, and declination, β), where the conversion was performed by the equations given by Prescott (1977) which are as follows :

(a) $\sin \delta = \sin \delta \cos \theta + \cos \delta \sin \theta \cos \phi$

(b)
$$\sin H = \frac{\sin \theta \sin \phi}{\cos \delta}$$
 (8.1)
(c) $RA = \gamma + H$
(d) $\cos H = \frac{\cos \theta - \sin \delta_{0} \sin \delta}{\cos \delta \cos \delta}$

where $\delta_0 = 1$ atitude of the array (54.75⁰) $\gamma = 1$ ocal sidereal time H = Hour angle

A more meaningful picture of these parameters and their relationship is given in Figure (8.2).

The measured right ascension and declination of individual showers have been converted into galactic coordinates (latitude and longitude) and the following



Figure 8.2 : Presentation of the arrival direction of an event ^e in celestial coordinates where o is the projection of the array

formulae given by Lang (1974) were used :

(a)
$$\sin b'' = \sin \delta \cos 62.6^{\circ} - \cos \delta \sin(RA - 282.25^{\circ}) \sin 62.6^{\circ}$$

(b)
$$\sin(\ell'' - 33) = \frac{\cos \delta \sin(\alpha - 282.25^{\circ}) \cos 62.6^{\circ} + \sin \delta \sin 62.6^{\circ}}{\cos b'}$$

(c) $\cos(\ell'' - 33) = \frac{\cos \delta \cos(\alpha - 282.25^{\circ})}{\cos b''}$
(8.2)

To obtain the right ascension, it is seen from equation (8.1c) that a knowledge of the sidereal time of each individual shower is required. The sidereal time is obtained from the solar occurrence time of the event which is discussed in the next section.

8.3.2 <u>Conversion of Local Solar Time to Local</u> <u>Sidereal Time</u>

The E.A.S used in the present analysis were recorded during the period March to July 1977. For each event the local time of its occurrence was recorded. During the period March 21st to October 23rd 1977 local time was British summer time which is one hour ahead of Greenwich mean time. Having established the Greenwich mean time (which is also called Universal time) of each event the local sidereal time of its occurrence was found using the Astronomical Ephemeris for 1977. The Procedure is best illustrated by an example.

Example What is the local mean sidereal time of an EAS observed on March 28th 1977 at 18 hr 26 min 43 sec local time. 18hr 26min 43sec local time = 17 hr 26min 43sec Greenwich mean time (GMT) Zero hours GMT on March 28th 1977 = 12hr 21min 10.889sec sidereal time at Greenwich (see p 13 of 1977 Astronomical Ephemeris) 17hr 26min 43sec Add 17hr. 26min 43sec 29hr 47min 53.889sec Add 2min 51.946sec for gain of sidereal time on GMT in 2min 51.946sec 17hr 26min 43sec. See p 515 29hr 50min 45.835sec of 1977 Astronomical Ephemeris Subtract 24hr to give the local 24hr mean sidereal time at Greenwich 5hr 50min 45.835sec Subtract 6min 17.2sec to give the

local mean sidereal time at Durham which is at a longitude 1⁰ 34.3 west of Greenwich

Local mean sidereal time of the EAS 6min 17.200sec

5hr 44min 28.635sec

8.3.3 The Sin-Ambiguity

To calculate the celestial and galactic coordinates, the first three equations of (8.1) and the first two equations of (8.2), seem to be sufficient to obtain these coordinates. This is true for obtaining declination (δ) and galactic latitude (b'') as their range variation is from 0 to \pm 90 degrees. Therefore if their sin-values from equations (8.1a) and (8.2a) is between 0 and \pm 1 the angle derived would be 0 to \pm 90 which satisfy the required values. But for obtaining the hour angle (H) and galactic longitude (ℓ '') their range variation is from 0 to 360° equations (8.1b) and (8.2b) are not sufficient, since from the following table ;

Anyle Degree	U-90	90-180	180-270	270-360
sin	+	+	-	-
cos	+	-	-	+

Table 8,1

If the sin-value is between 0 to 1 or positive the angle could be in the range of (0-90) or (90-180) degree. Also if the sin-value is between 0 to -1 or negative then the angle could be in the range of (180-270) or (270-360) degree. To remove this sin-ambiguity another equation for 'cos' was independently used to find the relevant angle. The equations for obtaining hour angle (H) and galactic longitude (& '') are equation (8.1d) and (8.2c) respectively. To show the sin-

ambiguity more clearly an example of obtaining galactic coordinates through the equations (8.1 and (8.2) is now given.

starting data
information
$$\begin{cases}
\Theta = 35^{\circ} \\
\phi = 162^{\circ} \\
\delta_{\circ} = 54.75^{\circ} \\
\gamma = 11.5 \text{ hr}
\end{cases}$$

To obtain the celestial coordinates equations (8.1) are used :

 $\sin \delta = \sin \delta \cos \theta + \cos \delta \sin \theta \cos \phi \rightarrow \delta (\text{declination}) = 20.8^{\circ}$

$$\sin H = \frac{\sin \theta \sin \phi}{\cos \delta} \rightarrow \sin H = 0.19 > 0 \rightarrow H = \arcsin (0.19)$$

According to Table 8.1 the hour angle (H) could have two values : (H = 10.93

H:
$$\begin{cases} n' = 10.95 \\ or \\ H' = \pi - H' = 169.07^{0} \end{cases}$$
 (1)

To choose the relevant H value the following formulae is used :

$$\cos H = \frac{\cos \theta - \sin \theta_0 \sin \theta}{\cos \theta_0 \cos \theta} = 0.98 > 0$$

Since the sin and cosin values of H are both positive then from T_a ble 8.1 the hour angle (H) is in the range of (0-90) degree. It is thus concluded from (1) that

 $H - H' = 10.93^{\circ}$

To obtain the right ascension

$$AA = \gamma + H$$

$$\begin{cases}
H = 10.93^{\circ} = 0.73 \text{ hr} \\
\gamma = 11.5 \text{ hr}
\end{cases}$$
So the celestial coordinates are RA= 12.23 \text{ hr} and A= 20.81^{\circ}
which are converted to corresponding galactic coordinates

$$(b'', k'') \text{ by equations (8.2) as follows:}$$

$$sin b'' = sin \delta cos62.6 - cos6 sin (RA-2B2.25) sin 62.6$$
and
having $\begin{cases}
AA = 12.23 \text{ hr} \\
\delta = 20.61^{\circ}
\end{cases}$
Now to evaluate galactic longitude (k'') , where its equation
is

$$sin (k''-33) = -0.61 < 0$$

$$apparent arc sin $(k''-33) = -37.8^{\circ} = a$
According to Table 8.1 the angle $(k''-33)$ could have two values :

$$\begin{cases}
k''-33 = 2\pi - |a| \longrightarrow k'' = 335.2 \\
\circ r & (2) \\
k''-33 = \pi + |a| \longrightarrow k'' = 250.8^{\circ}
\end{cases}$$$$

88

•

To choose the relevant galactic longitude (& '') the following formula is used

$$\cos\left(\ell''-33\right) = \frac{\cos\left(\cos\left(-282.25^{\circ}\right)\right)}{\cos b'}$$

 $\cos \left(\frac{1}{2} - 33 \right) = -0.79 \le 0$

Since the sin and cosin of the angle $(\ell''-33)$ are both negative, then from Table 8.1, $(\ell''-33)$ is in the range (180-270) degree. It is thus concluded from (2) that ;

 $\ell'' - 33 = \pi + |a| \rightarrow \ell'' = 250.8^{\circ}$

Thus the galactic coordinates are $\frac{l'=250.8}{b'}$ and $\frac{b''=79.57^{\circ}}{b''=79.57^{\circ}}$

8.3.4 <u>Method of Calculating the Expected Number of</u> <u>Showers in Galactic Coordinates Assuming they</u> <u>are Isotropically Distributed in Space</u>

Having obtained the measured number of showers arriving from different cells of galactic coordinates, it is required to calculate the expected numbers assuming that the occurrence of an EAS is uniformly probable in sidereal time. To obtain such expected numbers the following procedures were performed; (a) The probability of a shower arriving with zenith angle 0 and azimuthal angle 4 $p(0, \phi)$ was calculated as follows; Assume $I(0) = I(0)\cos^{n}0 \text{ m}^{-2} \text{ s}^{-1} \text{ st}^{-1}$ for a horizontal collecting area A in time t. No. of events with $0 \rightarrow 0 + d = I(0)A\cos^{0}0.A\cos^{0}.2\pi\sin0.d0.t$ $= I(0).A.2\pi t \cos^{0}+\frac{1}{0}\sin0.d0.t$

= const $\cos^{n+1}\theta$ $\sin^{\theta}d^{\theta}$

The probability that a shower of given zenith angle has ϕ in range $\phi \rightarrow \phi + d \phi = \frac{d \phi}{2 \pi}$. The probability that a shower has zenith angle in the range $\Theta \rightarrow \Theta + d\Theta$ and ϕ in the range $\phi \rightarrow + d \phi$ is thus $p(\Theta, \phi) d\Theta d \phi = const cos^{n+1}\Theta sin \Theta d\Theta \frac{d \phi}{2 \pi}$ $= K cos^{n+1}\Theta sin \Theta d \Theta d\phi$ Requiring $\int_{0}^{\pi/2} \int_{0}^{2\pi} p(\Theta, \phi) d\Theta d \phi = 1$

$$\frac{\pi/2}{K} \int_{0}^{\pi/2} \int_{0}^{\pi+1} \cos \theta \cdot \sin \theta \, d \, \theta d \, \phi = 1$$

$$K \int_{0}^{2} \frac{(n+1)}{\cos \theta} \sin \theta d\theta \int_{0}^{1} d\phi = 1$$

$$\cos \theta = 1$$

$$K \int \cos^{n+1} \theta \quad d(\cos \theta) \cdot 2\pi = 1$$

$$\cos^{n} \theta = 0$$

 $\cos \theta = 0 \qquad \cos \theta = 1$ $K \qquad \frac{\cos \theta + 2}{\theta + 2} \qquad \cdot 2\pi = 1$

$$K = \frac{1}{n+2} \qquad 2\pi = 1 \longrightarrow K = \frac{n+2}{2\pi}$$

$$p(\Theta, \phi) d\Theta d\phi = \frac{n+2}{2\pi} \cdot \cos^{-1} \Theta \Theta d\Theta d\phi$$

The probability of a shower being incident at Θ , ϕ .

$$p(\theta, \phi) = \frac{n+2}{2\pi} \frac{n+1}{\cos} \cdot \sin \theta radian^{-2}$$

(b) For N showers randomly distributed in a total sensitive time T_s of sidereal time the number expected in an interval t to t + dt of sensitive time t_s is N. t_s^{s}/T_s . For these showers the number $n(0,\phi)d0d\phi$ expected in the zenith angle range 0 to θ + d θ and ϕ to ϕ +d ϕ is

$$n(\Theta, \phi) \ d \Theta \ d\phi = \frac{n+2}{2\pi} \ \cos \Theta \ \sin \Theta \ d\Theta \ d\phi \ N \ ts/T_s$$

Lonverting from azimuthal angle, zenith angle, sidereal time to right ascension and declination and then to galactic coordinates the expected number of showers in given ranges of galactic coordinates can be calculated. Most of the calculation was carried out by computer and Figure 8.3 shows an example of the print-out obtained. For the 2,608 events producing both inner and outer ring triggers of the Durham EAS array, Figure 8.10 can be used to show that for an isotropic distribution of EAS in sidereal time the number of showers expected in the sidereal time range 16.00-17.00 hrs The computer print-out gives the expected number is 260.8. of these events that should have the galactic coordinates shown. With similar information for the whole 24 hour period of sidereal time, the total expected number of events in given cells of galactic longitude and latitude can be calculated and this is how the expected number of EAS shown in brackets in figures 8.14, 8.15 and 8.16 have been calculated.

Figure 8.3 : Illustrative print-out of the computer program used to calculate the expected number of showers with the state average galactic latitude and longitude for an expected number of showers occurring in a given interval of sidereal time. For the example shown, the time interval is 16.00 - 17.00 hrs, mean = 16.50 hrs. The sum of the probabilities in the fifth column is 1.00. The total number of showers in the sixth column is 260.7998.

AVERAGE OF TWO SIDEREAL TIME RANGES (IN HOURS) = 16.50 NO. OF EXPECTED SHOWERS IN ONE HR. SIDEREAL TIME = 260.7998 PROB.. OF SHOWERS BEING INCIDENT AT THETA AND PHI ANGLES

	Theta Average	PHI Average	G.Latit	G.Longt	Probability of shower	Expected Number
	TN DEG	REES	TN DEGR	EES		
2473	5.0	18.0	39.32	89.01	0.0150	3.9233
2474 2475	5.0	54.0	37.34	85.99	0.0150	3.9233
2476 2477	5.0	90.0	37.01	82.15	0.0150	3.9233
2478 2479	5.0	126.0	38.43	78.69	0.0150	3.9233
2480	5.0	162.0	41.15	76.78	0.0150	3.9233
2482	5.0	198.0	44.25	77.31	0.0150	3.9233
2484	5.0	234.0	46.46	80.37	0.0150	3.9233
2486	5.0	270.0	46.84	84.83	0.0150	3.9233
2489	5.0	306.0	45.22	88.61	0.0150	3.9233
2490	5.0	342.0	42.33	90.11	0.0150	3.9233
2492 2493 2494	15.0	18.0	33.42	99.04	0.0336	8.7588
2495 2496	15.0	54.0	28.05	90.39	0.0336	8.7588
2 497 2 498	15.0	90.0	27.16	80.09	0.0336	8.7588
2 499 2500	15.0	126.0	30.99	70.55	0.0336	8.7588
2501 2502	15.0	162.0	38.54	64.20	0.0336	8.7588
2503	15.0	198.0	47.76	63.81	0.0336	8.7588
2505	15.0	234.0	55.16	72.53	0.0336	8.7588
2507	15.0	270.0	56.55	88.71	0.0336	8.7588
2510	15.0	306.0	50.89	100.94	0.0336	8.7588
2512	15.0	342.0	41.90	103.58	0.0336	8.7588
2514	+			+		
2515 2516	25.0	18.0	26.81	107.73	0.0304	7.9354
2517	25.0	54.0	18.64	94.07	0.0304	7.9354
2518 2519	25.0	90.0	17.29	78.37	0.0304	7.9354
2520	25.0	126.0	23.12	63.63	0.0304	7.9354
						[

	7	r	+·	†	r	· ·····
2523	25.0	162.0	34.70	52.69	0.0304	7.9354
2524 2525	25.0	198.0	49.49	48.89	0.0304	7.9354
2526 2527	25.0	234.0	63.08	60.55	0.0304	7.9354
2528 2529	25.0	270.0	66.05	95.23	0.0304	7.9354
2530 2531 2532	25.0	306.0	54.94	116.05	0.0304	7.9354
2532 2533	25.0	342.0	39.94	116.52	0.0304	7.9354
2534 2535 2536	35.0	18.0	19.78	115.35	0.0162	4.2287
2537 2538	35.0	54.0	9.17	97.36	0.0162	4.2287
2539 2540	35.0	90.0	7.41	76.82	0.0162	4.2287
2541 2542	35.0	126.0	14.98	57.48	0.0162	4.2287
2543 2544	35.0	162.0	29.88	42.33	0.0162	4.2287
2545 2546	35.0	198.0	49.22	33.53	0.0162	4.2287
2547 2548	35.0	234.0	69.31	40.94	0.0162	4.2287
2549 2550	35.0	270.0	74.95	109.00	0.0162	4.2287
2551 2552	35.0	306.0	56.76	133.81	0.0162	4.2287
2553 2554	35.0	342.0	36.68	128.59	0.0162	4.2287
2555 2556	45.0	18.0	10.24	122 44	0.0051	1 2201
2558	45.0	54.0	-0.21	100 44		1 2291
2559 2560 2561	45.0	90.0	-2.49	75 34	0.0051	1 3381
2562 2563	45.0	126.0	6 68	51 80	0.0051	1.3381
2564 2565	45.0	162.0	24.32	32,98	0.0051	1.3381
2565 2566	45.0	198-0	46.99	18,91	0.0051	1.3381
2568 2569	45-0	234.0	71,98	11.54	0.0051	1,3381
2570 2571	45.0	270.0	81,18	149.43	0.0051	1.3381
2572 2573	45.0	306.0	56,01	151.75	0.0051	1.3381
2574 2575	45.0	342.0	32.20	139.55	0.0051	1.3381
2576 2577						
2578 2579	55.0	18.0	4.80	129.13	0.0009	0.2239
2580 2581	55.0	54 . 0	-9.88	103.69	0.0009	0.2239
	1	1				

2582 2583	55.0	90.0	-12.36	73.84	0.0009	0.2239
2583 2584 2505	55.0	126.0	-1.68	46.30	0.0009	0.2239
2585	55.0	162.0	18.25	24.45	0.0009	0.2239
2587 2588	55.0	198.0	43.08	5.87	0.0009	0.2239
2589 2590	55.0	234.0	69.64	341.65	0.0009	0.2239
2591 2592	55.0	270.0	78.71	207.55	0.0009	0.2239
2593 2594	55.0	306.0	52.66	168.14	0.0009	0.2239
2595 2596	55.0	342.0	26.95	149.33	0.0009	0.2239
2597 2598						
2599	65.0	18.0	-2.81	135.61	0.0001	0.0147
2600 2601	65.0	54.0	-19.33	106.95	0.0001	0.0147
2602 2603	65.0	90.0	-22.24	72.22	0.0001	0.0147
2604 2605	65.0	126.0	-10.02	40.76	0.0001	0.0147
2606 2607	65.0	162.0	11.82	16.52	0.0001	0.0147
2608 2609	65.0	198.0	37.88	354.63	0.0001	0.0147
2610 2611	65.0	234.0	63.59	321.38	0.0001	0.0147
2612 2613 2614 2615	65.0	270.0	70.62	230.59	0.0001	0.0147
	65.0	306.0	47.61	181.56	0.0001	0.0147
2616 2617	65.0	342.0	21.10	158.20	0.0001	0.0147
2618 2619						
	_					l

8.4 ANALYSIS OF THE DATA AND RESULTS

A total number of 3577 events were recorded in the time period March to July 1977. Showers were selected initially Using an outer ring trigger and later a combined inner or outer ring trigger of the Durham EAS array.

The size distribution and the measured 0 and ϕ distributions for all the data, the outer ring trigger data and the combined inner and outer ring trigger data, are given in Figure (8.4) to (8.8), where the measured zenith and azimuthal angle distributions are also shown in the figures. For the measured 0 distribution the function of the form $I(0)=I(0) \cos^{n}0$ where I(0) is the vertical intensity and $I(\theta)$ the intensity at zenith angle0 was fitted to the data. The best values of n were calculated to be 8.2 for all the data, 8.5 for the outer ring trigger data and 8.0 for the combined inner and outer ring trigger data.

The next step in the analysis was to investigate any anisotropy in sidereal time. For the present data the operational time distributions and frequency-time variations of events in solar and sidereal time are given in Figures (8.9°), (8.10), and (8.11). The dotted lines are the expected distributions which were calculated assuming a uniform distribution in sidereal time. χ^2 probability tests between the measured and expected number of events in different intervals of side-real time showed that they are not far from being randomly distributed. An interesting point arises from the comparison of the combined inner and outer ring trigger data (events with $\bar{N} = 3.10^5$ pts) with the outer ring trigger data (events with $\bar{N} = 1.11.10^6$ particles). The χ^2 test shows that the








Shower size distributions for different triggering systems







Figure 8.7 : Zenith and azimuth angle distribution of showers selected by the outer ring trigger. Dotted lines are the predicted distribution.



Figure 8.8 : Zenith and azimuth angle distribution of showers selected by the combined inner and outer ring triggers. Dotted lines are the predicted distributions.





The operational time distributions and frequency time variations of E.A.S. in solar and sidereal time for all the data. Dotted line is predicted distribution if it is isotropic in sidereal time. •



Figure 8.10 : The operational time distributions and frequency-time variations of E.A.S. in solar and sidereal time for outer ring triggers. Dotted line is predicted distribution if it is isotropic in sidereal time.



Figure 8.11 : The operational time distributions and frequency-time variation of E.A.S. in solar and sidereal time for inner and outer ring triggers. Dotted line is predicted distribution if it is isotropic in sidereal time.

probability of the data in the two samples is consistent with a uniform distribution in sidereal time decreases from 30% to 5% as \bar{N} increases from 3.10^5 to $1.11.10^6$. Thus the measurements suggest an anisotropy of primary particles in sidereal time which increases with their primary energy.

The next step was the analysis of the data in galactic coordinates. The right ascension and declination distributions of the observed showers are shown in Figures (8.12) and (8.13). The galactic latitude and longitude of the showers were obtained from their declination and right ascension producing the galactic frequency distributions of Figures (8.14), (8.15) and (8.16). As shown in the figures, the number of observed showers in 30 by 20 degree longitude-latitude cells are summed and shown in the corresponding squares. The figures in the brackets are the expected number of showers assuming they are isotropically distributed in space (Section 8.3.3.). The same data is also presented graphically in Figures 8.17 to 8.22). Inspection of Figure 8.14, which is based on all the 3577 observed showers, shows that overall there is good agreement between observation and expectation assuming a uniform distribution in sidereal time except for the cells marked * and **. In the first case the observed number of events 43 exceeds the expected number of events 19.67 by 3.6 standard deviations and in the second case the observed number of events 229 exceeds the expected number 158.65 by 4.6 standard deviations. Ιn both cases the major contribution to the excess comes from the combined inner and outer ring trigger data (Figure 8,15) rather than the outer ring trigger data (Figure 8.16). The combined inner and outer ring trigger data has lower average energy

93



Figure 8.12 : Distribution of E.A.S. in celestial coordinates for inner ring and outer ring triggers.



Figure 8.13 :

Distribution of E.A.S. in celestial coordinates for outer ring triggers,

Figure 8.14 : The observed and expected frequency distribution of E.A.S. in galactic coordinates for all the data. The expected distribution is calculated assuming it is isotropic in the galaxy.

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true ates = 99.	258(267.96)	807(835.87)	1100(1068.72)	784(785.63)	408(427.17)	187 (164.03)	32(26.23)	o(1.32)	3577(3577)
X ² if cordin	4 (6.39)	4 (2.48)	3(0.05)	1 (<10 ³)	0(0.0)	0(0.0)	0.0)0	0(0.0)	36.
le of tic c	5 (2.57)	1 (0.54)	1(<10 ³)	0(<10 ³)	0(0,0)	0.00	0.0)0	0.0)0	e e e e e e e e e e e e e e e e e e e
s valu galac	9(8.21)	1 (0.35)	0(0.012)	0(<10 ³)	(0°0)0	(0 0) 0	0(0.0)	0(0,0)	30 M
ue > thi ropic in	4 (4.89)	4 (2.77 [^])	2 (0.38)	0(5.4.10 ⁻³)	0(<10 ³)	0(<10 ³)	c(0.0)	0(0,0)	270
is isot:	14 (5.56)	14(11.34)	2(2.74)	3(1.1)	0(0.18)	0(2.4.10 ³)	0(<10 ³)	0(<10 ³)	Lo 240
ility c oution	20(30.74)	40(49.67)	34(31.66)	17(21.01)	4 (6.12)	0(0.82)	0(0.037)	o(3.10 ⁴)	2
Probab. distrib	28(36.43)	106(102.09)	108(134.97)	74(62.41)	23(24.75)	9(5.73)	1(1.01)	0(0.018)	130
73 73	43(19.67)	180(175.63)	** 229 (158 - 65)	64(80.87)	65(57.42)	4C(34.78)	6(6.13)	0(0.54)	150
×× 2 ≡ 33	47(74.34)	214(239.2)	337(345.37)	305 (270.14)	167(179.93)	89(85.15)	22(15.62)	0(0.61)	120
. 3577	41(43.15)	159 (167.08)	282 (292.62)	276(295.03)	136(139.2)	45(35.43)	2(3.26)	0(0.15)	06 06
• of events (expected)	31(28.31)	75(67.45)	95(96.69)	41 (54.6)	13(19.55)	2(2.12)	2(0.17)	0(6.5.10 ³)	
Total no. observeđ	12(7.7)	9(17.23)	8(5.69)	4 (0.47)	0(0.02)	2(2.10 ³)	0(<103)	0(<10 ³)	
60		ç, ç,	'd ,9buti	tal sitsafi	2 ₽ .			R	-70

Figure 8.14

Galactic longituãe, ĉ'(^o)

Figure 8.15 : The observed and expected frequency distribution of E.A.S in galactic coordinates for inner and outer ring triggers.

Thtal no. of events = 2608

Inner and Outer Ring Trigger

		~	~	~	2		r	1
202(207.6)	585(639.89	843(789.09	570(564.41	269(283.26	116(106.88	23(16.07)	0(0.8)	2608(2603) 50
3(5.3)	3(1.95)	3 (0-04)) 1 (<10 ³)	0(0.0)	0(0.0)	0.0)0	0(0.0)	30
5(1.53)	0(0.43)	1 (<10 ³)	0(<10 ³)	0.0,0)	0(0.0)	0(0.0)	0.0)0	
7(6.47)	1 (0.33)	0(0.01)	0(<10 ³)	0(0.0)	0.0.0)	0.0)0	0.0.0)	Ř
3(3.7)	2(2.05)	2 (0.18)	0(2.4.10 ³)	0(<10 ³)	0(<10 ³)	0.0.0)	0(0.0)	40 270
11(4.53)	10(7.25)	2(1.27)	3(0.49)	0(0.07)	0(4.10 ⁴)	0(<10 ³)	0(<10 ³)	5,
13(22.9)	23(31.1)	21 (15.92)	7(8.98)	0(1.6)	0(0.15)	0(0.01)	o(<10 ³)	80 210
20(27.2)	72 (70.43)	57(77.9)	29(24.51)	5(5.97)	5(1,25)	1 (0. 29)	0(2.3.10 ³)	
* 33(15.03)	132 (130.2)	** 186(112.07)	41 (46.87)	35 (30.06)	16(19.33)	6(3.51)	0(0.35)	150
38(59.55)	161(193.3)	280(270.6)	245(209.7)	116(126.6)	60(58.6)	13(10.07)	0(0.36)	120
31 (33.9)	115(133.3)	205 (229.2)	212(230.9)	105(104)	32(25.78)	1 (2.06)	0(0,09)	06 ·
26(22.43)	58(54.35)	79(76.8)	29(42.6)	5(14.94)	1(1.77)	2(0.13)	0(4.5.10 ³)	ÿ
12 (6.06)	8(15.2)	8(5.1)	4 (0.36)	0(0.02)	2(<103)	0(<10 ³)	0(<10 ³)	30
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Figure 8.15

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Galactic longitude, l'' (°) \rightarrow

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Figure 8.16 : The observed and expected frequency distribution of E.A.S in galactic coordinates for outer ring triggers.

Total no. of events = 969

Outer ring trigger

00	0(1.64)	5 (5.88)	10(9.25)	9(15.79)	* 10(4.64)	8(9.23)	7(7.84)	3(1.03)	1(1.19)	2(1.74)	0(1.04)	1(1.09)	56(60.36)
	1 (2.03)	17(13.1)	44(33.78)	53(45.9)	48 (45.43)	34 (31.66)	17(18.57)	4(4.09)	2(0.72)	0(0.02)	1 (0.11)	1 (0.53)	222(195.98)
)	0(0.59)	16(19.89)	77 (63.42)	57(74.77)	** 43(46 . 58)	51 (57.07)	13(15.74)	0(1.47)	0(0.2)	0(2.9.10 ³)	0(<10 ³)	0(0.01)	257(279.7)
e m	0(0.11)	12(12.0)	64(64.13)	60(60.44)	23(34)	45 (37.9)	10(12.03)	0(0.61)	0(3.10 ³)	0(<10 ³)	0(<10 ³)	0(<10 ³)	214(221.22)
9	0(3.1.10 ³)	5(4.61)	31(35.2)	51 (53.33)	30(27.36)	18(18.78)	4(4.52)	0(0.11)	0(<10 ³)	0(0.0)	0(0.0)	0.0.0)	139(143.91)
	0(2.10 ³)	1 (0. 35)	13(9.65)	29 (26.55)	24 (15.45)	4 (4.48)	0(0.67)	0(2.10 ³)	0(<10 ³)	0(0.0)	0(0.0)	0.0.0)	71 (57.15)
	0(<10 ³)	0(0.04)	1(1.2)	9(5.55)	0(2.62)	0(0.72)	0(0.027)	o(<10 ³)	0.0,0)0	0(0,0)	0(0.0)	0.0.0)	10(10.16)
s S	o(<10 ³)	0(2.10 ³)	0(0.06)	0(0.25)	0(0.19)	0(0.016)	0(3.104)	0(<10 ³)	0.0,0)0	0(0.0)	0(0.0)	0.0.0)0	0(0.52)
0	30	ف	06	120	0 150	Calacti	0 21 r leaditu	0 24 de.	to 270	300	м С	360	969 (969) J

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(°) '' (°) Galactic latitude, b Figure 8.16

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Total no of showers (all the data) = 3577

Figure 8.17 : Variation of the expected number of showers with galactic longitude for different ranges of galactic latitude. The observed number of events in cells containing > 10 showers are plotted.



Figure 8.18 : Variation of the expected number of showers with galactic latitude for different ranges of galactic longitude. The observed number of events in cells containing > 10 showers are plotted.



Figure 8.19 : Variation of the expected number of showers with galactic longitude for different ranges of galactic latitude. The observed number of events in cells containing > 10 showers are plotted.



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Figure 8.20: Variation of the expected number of showers with galactic latitude for different ranges of galactic longitude. The observed number of events in cells containing > 10 showers are plotted.



Figure 8.21 : Variation of the expected number of showers with galactic longitude for different ranges of galactic latitude. The observed number of events in cells containing > 10 showers are plotted.



Figure 8.22 : Variation of the expected number of showers with galactic latitude for different ranges of galactic longitude. The observed number of events in cells containing $\geqslant 10$ showers are plotted.

 $(\bar{N} = 3.1u^5)$ than the outer ring trigger data $(\bar{N} = 1.11.10^6)$. 8.5 CONCLUSION

Overall the arrival directions of EAS seem to be isotropically distributed in space. Some evidence is found for a possible increase in intensity from two directions with galactic longitude and latitude $(135^{\circ} \pm 15^{\circ}, 40^{\circ} \pm 10^{\circ})$ and $(135^{\circ} \pm 15^{\circ}, 80^{\circ} \pm 10^{\circ})$.

The galactic coordinates of the two galactic cells shown in Figure 8.14 which contain a significantly larger number of events than expected have been compared with the galactic coordinates of supernova remnants, pulsars, guasars, X and Y-ray sources which are shown in Figures (8.23.) to (8.27). It is seen from the figures that there are no observed X, γ or supernova remnants (they are mostly in the galactic plane) in our excess regions of events (represented by squares). However, there is some correlation with pulsar and guasar sources. The properties of these sources has been investigated in spite of not every pulsar or quasar having all the required information at the present time. The ones known are shown in Figures 8.28 and 8.29. The ones in the square regions for quasars show no sign of any anomalous property whereas the pulsar (PU809 + 74) shows the interesting property of having one of the longest ages and shortest distance from earth of known pulsars.



Figure 8.23 : Known supernova remnants in galactic coordinates, (From "Astrophysical Formulae", Lang (1974)).

N.S







Known γ ray sources in galactic coordinates, (Europhysics Study Conference, (1979), Gamma ray Astronomy after Cos-B). Figure 8.25 :











Figure 8.28 : Flux density distribution of known quasars (from "Astrophysical Formulae", Lang (1974)).





Lang (1974)).

CHAPTER 9

CONCLUSION

The Durham E.A.S. array and a large flash tube chamber were used to study the details of E.A.S.phenomena, that give an understanding of elementary particles, nuclear interactions and also the nature and origin of E.A.S.

The study of the electron component and the age parameter, s, of individual E.A.S. in the size range of 10^4 - 10^7 particles showed that they do not all obey the same structure function. The mean and the standard deviation of the age parameter distribution of the showers showed that on average they are independent of zenith angle. The observed large fluctuation of the age parameter distribution indicates no significant fraction of heavy nuclei in primary cosmic rays since these would produce a negligible fluctuation.

A measurement of the size spectrum was obtained taking into account the age parameter of E.A.S. and the results showed that it is not quite consistent with previous work. The difference is at large sizes $>10^7$ pts and is due to an increase of age parameter with shower size which results in a larger average size.

A correlation between the electron and muon component was also found. The results showed on average that old showers have more muons and a flatter lateral distribution of muons than young showers (i.e. $\frac{\Delta_{\mu} (s > 1.2)}{\Delta_{\mu} (s < 1.2)} = 1.24 \pm 0.05$). In the search for quarks two candidates were found but these are believed to be due to background muons which simulate e/3 quark-like tracks. This gave the ratio of penetrating charge e/3

95

particles to penetrating e particles as $< \frac{1}{1,136}$ for the present experiment.

An analysis of the arrival directions of E.A.S. in galactic coordinates has been made. Evidence for an excess of events from galactic directions with latitude b'' = (30-50) and b''(70-90) and both having galactic longitude of $''(120^{\circ}-150^{\circ})$ were observed.

APPENDIX A

EVALUATION OF THE FRACTION OF PARTICLES WHICH FALL BEYOND A DISTANCE FROM THE SHOWER AXIS DIRECTION IN PURE ELECTRON PHOTON CASCADES

The fraction of electrons that fall at core distance >r is given by $F({}^{>}r,s) = \int_{r}^{\infty} 2\pi r S(r,s) dr$ where $S(r,s) = c(s) r^{s-2} (1 + r)^{s-4 \cdot 5}$ is the electron structure function for showers of age parameter s, r is the core distance in Moliere units (79 m at sea level) and c(s) is a normalisation factor such that $\int_{0}^{\infty} 2\pi r S(r,s) dr = 1$. F(>r,s) is evaluated in two parts for $0 < r \le k$ and r > k. k is the distance beyond which the structure function tends to a straight line on a log-log plot so it is well approximated by $\frac{A}{r}^{\alpha}$. The parameters A and α are simply obtained, so for any r > k, the integral

$$F(>r,s) = \int_{r}^{\infty} 2\pi r \ S(r,s) dr = \int_{r}^{\infty} 2\pi A \ \frac{r}{r^{\alpha}} = 2\pi A \int_{r}^{\infty} r^{1-\alpha} dr$$

is calculated. Because of the complexity of the function S(r,s) the formula $S(r,s) = \frac{A}{\alpha}$ cannot be used for 0< r<k and r is evaluated numerically. The results are shown in Figures Al and A2.



Figure Al : The fraction of electrons F(>r,s) that fall at core distance >r in pure electron photon showers for r in the range O-1 Moliere unit. s is the age parameter of the shower.



APPENDIX B

A COPY OF THE CERN MINUIT PROGRAM USED TO MINIMIZE THE N.K.G.

FUNCTION FOR THE AGE PARAMETER AND SHOWER SIZE

TERMINAL	SYSTEM	FORTRAN G (21.8) FCN
0001		SUBROUTINE FCN (NPAR, G, F, X, IFLAG)
0002		DIMENSION G(150), X(150), R(15), DR(14), CHISQ(14), VR(14),
		*E(14),AH(14),XD(15),YD(15),ZD(15),SY(15),Y(15)
0003		DIMENSION FC(14)
0004		COMMON/KEEP/K,DTIT,R
0005		GO TO(1,2,2,2), IFLAG
0006	1	CONTINUE
0007		DATA AH/0.75,2.0,2.0,2.0,2.0,2.0,2.0,0.8,0.8,1.0, *1.0,1.2,1.0,1.6/
8000		DATA XD/0.0,-12.3,-45.0,14.0,45.0,0.3,-5.0,-24.0,
		*-24.0,25.5,22.0,39.5,-0.5,-7.9,-9.5/ DATTA VD 0 -5 64 29 5 3 5 14 0 -26 8 -58 5 7 5
		*7.5,8.5,-17.0,-36.5,-17.0,-5.11,-6.2/
0010		DATA ZD/0.0,-4.83,-13.46,0.16,0.21,0.18,-8.67,
		*-12./5,-12./5,0./5,-11.4,-8.2,0.6,-4./,0.0/
0011		READ(5, 100) (K, (DR(1), I=1, 10))
0012		READ(5, 150)((DR(1), I=11, 14), DTIT, FA, XE, YE)
0013	100	FORMAT(18, 10F6.1)
0014	150	FORMAT(8F 6.1)
0015		TIT=DTIT*3.14/180.
0016		FA=FA*3.14/180.
0017		DO 30 I=1,14
0018		VR(I) = ABS(DR(I) * AH(I))
0019		E(I) = SORT(1.436 * VR(I) + SORT(VR(I)) + 0.25)
0020	30	CONTINUE
0021	2	CONTINUE
0022	-	HN = X(1)
0023		$S = \mathbf{Y}(2)$
0023		F = 0
0024		r = 0.00
0025		TE(DD(1)) T=17+7
0026		$\frac{11}{100} \frac{11}{100} \frac{11}{100} \frac{1000}{1000} \frac{1000}{1$
0027		Y(1) = ABS(((XD(1) - XE) **2 + (YD(1) - YE) **2 + (2D(1) **2) - (SIN(TIT) **((XD(1) - XE) *COS(FA) + (YD(1) - YE) *SIN(FA)) + (2D(1) *COS(TIT))) **2))
0028		SY(I) = ABS(SQRT(Y(I)))
0029		$IF(SY(I) \cdot LT \cdot O \cdot 5) SY(I) = O \cdot 5$
0030		FO(I) = (HN/79**2)*AH(I)*0*366*(S**2)*((2*077-S)**1*25)*
		*(((SY(I))/79.)**(S-2.))*((SY(I))/79.+1.)**(*S-4.5)
0031		CHISQ(I) = ((FC(I) - VR(I)) / E(I)) * * 2
0032		F=F+CHISQ(I)
0033	200	CONTINUE
0034		IF(IFLAG.NE.3)GO TO 24
0035		DO 40 I=1,15
0036		A = XD(I) - XE
0037		B=YD(T)-YE
0038		C = ZD(I)
0039		DBC=D**2+B**2+C**2
0035		ABC = A = 2 + B + C + C + C + C + C + C + C + C + C
0040		$SI = A^{*}COS(rA) + B^{*}SIN(rA)$
0041		51-51*51N (TIT) #C*CO5 (TIT)
0042		
0043		SUB1=ABS(ABC-S1)
0044		R(I) = SQRT(SUBI)
0045	40	CONTINUE
0046		WRITE (6,77) K
0047	77	FORMAT (18)
0048		DO 300 I=1,14
0049		IF (DR (1) .LT.O.O) GOTO 300
0050 0051 0052	400 300	WRITE(6,400)R(I),VR(I),DR(I),CHISQ(I),FC(I),E(I) FORMAT(2X,F8.2,3X,F6.2,5X,F10.3,6X,F12.4,4X,2F12.4) CONTINUE
----------------------	------------	---
0053		WRITE $(6, 101) R(15), R(1)$
0054	101	FORMAT(4x, F8.4, 4x, F8.4)
0055	24	CONTINUE
0056		RETURN
0057		END

TERMINAL SYSTEM FORTRAN G (21.8)

STAND

0001		SUBROUTINE STAND
0002		DIMENSION A(1000), B(1000), EA(1000), EB(1000), R(15)
0003		DIMENSION KA(300), DTITA(300), RA1(300), RA15(300)
0004		DIMENSION DR(14), XD(15), YD(15)
0005		COMMON/MINIMA/AMIN, UP, NEWMIN, ITAUR, SIGMA/CONVER/EPSI, APSI, VTEST
		*NSTEPQ,NECN,NFCNMX
0006		COMMON/PAREXT/U(150),W(150),WERR(150),MAXEST,NU/PARINT/
		<pre>*X(55),XT(55),DIRIN(55),MAXINT,NPAR/LIMITS/ALIM(150),</pre>
		*BLIM(150),LCODE(150),
		*LOORSP(150),LIMSET/TITLE/TITLE(55),ISW(7),NBLOCK
0007		COMMON/KEEP/K, DTIT, R
8000		DIMENSION G(150)
0009		ITER=151
0010		DO 10 I=1,ITER
0011		ITAUR=0
0012		CALL FCN (NPAR, G, AMIN, U, 4)
0013		CALL SEEK
0014		NFCNMX=4000
0015		EPSI=0.01
0016		VTEST=0.04
0017		APSI=EPSI
0018		NFCN=0
0019		CALL SIMPLX
0020		NFCN=O
0021		CALL MIGRAD
0022		IF(ISW(2).GT.2) GOTO11
0023		CALL HESSE
0024	11	CONTINUE
0025		CALL FCN (NPAR, G, AMIN, U, 3)
0026		A(I) = U(1)
0027		B(I) = U(2)
0028		KA(I) = K
0029		DTITA(I) = DTIT
0030		RA1(I) = R(1)
0031		RA15(I) = R(15)
0032		IF (I.FQ.ITER) GOTO20
0033	_	CALL FCN (NPAR, G, AMIN, U, 1)
0034	10	CONTINUE
0035	20	CONTINUE
0036		DO 1951 II=1,ITER
0037		PRINT 66
0038	1050	PRINT 1952, II, KA(II), DTITA(II), RA1(II), RA15(II), B(II), A(II)
0039	1952	FORMAT(1X,'I',15,' I ',18,4(' I ',F8.2),' I ',E10.3,
	6.6	*' I ',8X,'I',8X,'I')
0040	66 1051	FURMAT(1X,96('-'))
0041	1921	
0042		PRUTUDN PRUTUDN
0043		
0044		END

.

APPENDIX C

THE EFFECT OF SAMPLING DENSITY FLUCTUATIONS ON THE COLLECTING AREA FOR SHOWERS OF A GIVEN SIZE FOR A GIVEN E.A.S.SELECTION TRIGGER

Consider the collecting area for shouers of size 3.10^5 selected by an outer ring trigger, $\Lambda_{\rm c}(\gg 4~{\rm m}^{-2})$. $\Delta_{13}(\gg 2~{\rm m}^{-2})$. $\Delta_{33}(\gg 2~{\rm m}^{-2})$. $\Lambda_{53}(\gg 2~{\rm m}^{-2})$ where the area of detector C is 0.75 m² and the areas of detectors 13, 33 and 53 are 2 m². Suppose the showers are incident vertically and the electron lateral distribution is given by the Greisen average electron lateral distribution function (s = 1.25). This means that the collecting area is calculated for a minimum number of particles = 3 at C and 4 at the other three triggering detectors, which is the area of the spherical triangle shown in Figure C₁. To get a more exact estimate of the collecting area the effect of sampling density fluctuations at the detectors should be taken into account. Taking the fluctuations as Poissonian,

$$p(r) = \frac{e^{-z} z^{r}}{r!}$$

where p(r) is the probability of observing r when the mean number expected is z. For any core position (x,y) in the array at which a shower of size 3.10^5 falls, the core distance from a triggering detector and therefore the average number of particles through it can be calculated.

s = 1.25 selected by an outer ring trigger Δ_c (> $4m^{-2}$). Δ_{13} (> $2m^{-2}$), Δ_{33} (> $2m^{-2}$) and assuming no sampling density fluctuations. 6 radius vectors on which the effect of Figure C.1 : Scale diagram showing the collecting area for a vertical shower of size 3.10⁵ with sampling density fluctuations on collecting area are also shown in the figure.



For the case of the outer ring detectors p(r) is

$$\mu(r) = e^{-z} \left(1 + \frac{z^{1}}{1!} + \frac{z^{2}}{2!}\right) \quad \text{for detector } C$$
$$= e^{-z} \left(1 + \frac{z^{1}}{1!} + \frac{z^{2}}{2!} + \frac{z^{3}}{3!}\right) \text{ for detectors}$$
$$13.33 \text{ and } 53$$

where z is the mean number of particles through the detector and the first term is the probability of there being zero, the second term being the probability of there being 1, etc. The detection probability for a shower falling at the position (x,y) is the sum of all the detector probabilities or

$$P(r) = \sum_{i} p_{i}(r) : i = 0,13,33 \text{ and } 53$$

In the present case P(r)-r for each of 6 radius vectors (as chosen in Figure C.1) was evaluated and the results are given for the case of fluctuations and no fluctuation in Figure C.2. The collecting area A is given by

$$A = \int_{\Theta=0}^{2\pi} \int_{r=0}^{\infty} r d_{\Theta} dr P(r)$$

A measure of the effect of fluctuation on the collecting area





Figure C.2 : The detection probability for a shower of size 3.10⁵ pts with s = 1.25 selected by the outer ring trigger as a function of core distance from the central detector r for each of 6 radius vectors as shown in figure C.1. The detection probability assuming no sampling density fluctuations are shown by the solid line and the dashed line shows the effect of sampling density fluctuations.

for each radius vector is

$$\int_{0}^{\infty} r \, dr \, P(r) = \int_{0}^{\infty} r \, dr \, P(r)$$

$$\frac{\int_{0}^{r} r \, dr}{\int_{0}^{r} r \, dr} = \frac{\frac{r_{max}^{2}}{2}}{\frac{r_{max}^{2}}{2}} = \frac{fluctuation \ collecting \ area}{fluctuation \ collecting \ area} = F$$

Table C.2 shows the values of F for the 6 radius vectors together with the mean value of \overline{F} which shows the effect of sampling density fluctuations on collecting area for a shower of size 3.10^5 particles. It is seen that $\overline{F} = 0.95 \pm 0.15$ which indicates the effect is small. The collecting area assuming no sampling density fluctuation for a vertical shower of size 3.10^5 with s = 1.25 is $3.2.10^3$ m² (see Figure C.3). A more exact estimate of the collecting area taking the sampling density fluctuations factor \overline{F} into account is

 $3.2.10^3 \text{ m}^2 \text{ X} 0.95 = 3.04.10^3 \text{ m}^2$

The coordinates of the centres of the detectors used in the present work (see Table Cl) were slightly different to those given by Abdullah et al (1979).

			L
52	-0.5	-17	9°0
41	22	-17	-11.4
32	25.5	ی. م	0.75
62	-43.1	-18.3	-10.3
61	-7.9	-5.11	-4.7
42	39°5	- 36. 5	- 8.2
12	-24	7.5	-12.75
53	ы Г	- 58.5	- 8.67
51	0.3	-26.8	0.18
33	45	14	0.21
31	14	3.5	0.16
13	-45	29.5	-13.46
11	-12.3	- 5.64	- 4.83
U	0	0	0
Detector	χ Coordinate (m)	Y Coordinate (m)	Z Coordinate (m)

TABLE C.1 : The detector's coordinates of the Durham E.A.S. Array.

Hadius Vector	F
1	1.57
2	0.52
3	1.30
4	U. 6ő
5	1.04
б	0.64
Average	F =0.95 <u>+</u> 0.15

Table C.2 : The value of the ratio of fluctuationcollecting area to the no fluctuationcollecting area, F for a shower of size 3.10^5 with s = 1.25 selected by the outerring selection trigger for the 6 radiusvectors shown in Figure C.1. The averagevalue \overline{F} is also given.



Figure C.3 : The collecting area as a function of shower size for E.A.S. selected by an outer ring trigger. For size 3.10⁵ pts the no. fluctuation collecting area is compared with the fluctuation collecting area which is marked by a solid circle.

APPENUIX D

THE EFFICIENCY OF DETELTING SINGLE PENETRATING CHARGED PARTICLES TRAVERSING A SHIELDED FLASH TUBE CHAMBER AS A FUNCTION OF CORE DISTANCE IN EXTENSIVE AIR SHOWERS

In order to obtain the efficiency of the chamber the effect of burst production (i.e. hadron interactions in the shielding lead and iron) should be considered. The efficiency of the chamber depends on each individual event and decreases with increasing burst size which occurs in the chamber. The possibilities of burst production could be of four types as given in Figure D1. For each type the efficiency of detecting a single penetrating particle is measurable as formulated below each type shown in Figure Dla to Figure Dld. The efficiency of all events described in Chapter 7 have been individually measured accordingly and grouped into core distance ranges of 0-5, 5-10, 10-20 and 20-30 meters from the chamber where shower size ranges of less and bigger than the median size of the data (Ne=3.10 5 pts) were chosen for analysis. The shower size distributions of events for the above mentioned core distances are given in Figure D2 and their corresponding average efficiency -core distance results are given in Figure D3. It is noted that these measurements are for the basic data and should be corrected for the effect of core location errors. Assuming that the core location errors are Gaussian with a standard deviation of 6.0 m(see Chapter 3) and also that the detection -r/r_o, a simulation work efficiency, η has the form $\eta = 1 - e$

was performed which showed that the best values of r_0 that fit the measurements for $10^4 < N < 3.10^5$ and $N > 3.10^5$ pts are $r_0 = (1.55 \pm 0.15)m$ and $r_0 = (3.25 \pm 0.65)m$ respectively as given in Table U1. These functions are plotted in Figure D3. It is seen that the efficiency n of detecting single penetrating particles decreases as the core distance decreases, due to high energy hadrons interacting in the shielding material.



Aperture = solid angle x area = $\frac{Lx}{y^2}$. Lx = $\frac{L^2 x^2}{y^2}$

probability of detecting a single particle = 1 in this case



Aperture = solid angle x area = $\frac{l_1 x}{y^2}$. $l_2 x$ = $l_1 l_2 \frac{x^2}{y_2}$

probability of detecting a single particle = $l_1 l_2 \frac{x^2}{y^2} / \frac{L^2 x^2}{y^2} = \frac{l_1 l_2}{L^2}$



(d)

Probability of detecting a single particle = $\frac{1}{L^2} \frac{1_3}{L^2} \frac{1_4}{L^2}$ Probability of detecting a single particle $\simeq \frac{l_1 l_2}{L^2}$

Figure D1 : Typical burst production occurring in the chamber, affecting the efficiency for detecting a single penetrating charged particle.



Figure D2 : Size distribution of showers falling in different ranges of orthogonal core distance R_H from the centre of the flash tube chamber used in the present analysis.

r_{0} in $\eta = 1-e$	(1.55 <u>+</u> 0.15) m	(3.25 <u>+</u> 0.65) m
Shower size range	10 ⁴ < N < 3.10 ⁵	N > 3.10 ⁵

Values of \mathbf{r}_{o} in the efficiency-core distance function for detecting a single penetrating charged particle, for different ranges of shower size. TABLE D 1 :



orthogonal core distance.---raw measurements uncorrected for core location error The efficiency η of detecting a penetrating particle as a function of --- true variation for a core location error of 6.0 m. Figure D3 :

r Ta

APPENDIX E

CONSISTENCY OF THE PRESCOTT (1977) AND THE CLARK ET AL (1958) FORMULAE FOR DETERMINING THE RIGHT ASCENSION AND DECLINATION

FROM THE MEASURED ARRIVAL DIRECTION OF AN E.A.S.

In Chapter Eight the formulae given by Prescott (1977) were used to determine the right ascension and declination of a shower with a measured zenith angle 0 and azimuthal angle ϕ (measured in a clockwise direction from geographic north) occurring at a given local sidereal time. Alternative formulae have been given by Clark et al (1958) in terms of the direction cosines of the arrival direction and this appendix is to show that the two sets of formulae are consistent.

Consider a shower arriving at the point O in Figure El and suppose the shower makes direction cosines l,m,n with the axes x,y,z. Ground level is the plane x,y and the y axis points in the direction of geographic north.

Prescott, I.C., "A study of the muon and electromagnetic components of E.A.S", Ph.D. Thesis, Nottingham University, May, 1977. (See Figure 3.4)

Clark, G., Earl, J., Kraushaar, W., Linsley, J., Rossi, B., and Scherb, F., 1958, Supplements AP Volume VIII, Serie X del Nuovo Cimento, No.2, pp 622-652 (see page 644).



Figure El.

$$\ell = \cos \mathbf{T} \circ \mathbf{x} = \frac{\mathbf{x}}{\mathbf{o} \mathbf{T}} = \frac{\mathbf{o} \mathbf{T} \sin \theta \sin \phi}{\mathbf{o} \mathbf{T}} = \sin \theta \sin \phi$$
 (1)

$$m = \cos Toy = \frac{y}{oT} = \frac{oT \sin\theta \cos\phi}{oT} = \sin\theta \cos\phi$$
 (2)

$$n = \cos Toz = \frac{z}{oT} = \cos\theta$$
(3)

(4)

From (1) and (2)
$$\ell^2$$
 and $m^2 = \sin^2 \Theta \left(\sin^2 \phi + \cos^2 \phi \right) = \sin^2 \Theta$
 $\sin \Theta = \sqrt{\ell^2 + m^2}$

The equations given by Prescott (1977) are

$$\sin\delta = \sin\delta \cos\theta + \cos\delta \sin\theta \cos\phi$$
(5)

$$\sin H = \frac{\sin \Theta \sin \phi}{\cos \delta} \tag{6}$$

$$RA = \gamma + \sin^{-1} \left(\frac{\sin\theta \sin\phi}{\cos\delta} \right)$$
(7)

Using equation (4) and equation (2), equation (5) becomes ,

$$\sin \delta = \sin \delta_{0} \cdot \left[1 - \ell^{2} - m^{2} \right]^{2} + \cos \delta_{0} \cdot m$$
 (8)

1

Substituting from (1) in (7) gives

$$RA = \gamma + \sin^{-1} \frac{\ell}{\cos\delta}$$
(9)

Equations (4),(8) and (9) are the equations given by Clark et al (1958), for determining the right ascension and declination of a shower with arrival direction given by direction cosines(l,m,n) at local sidereal time γ at a station situated at a latitude δ_{Ω} .

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